

An artistic rendering of a supermassive black hole. At the center is a bright, glowing blue-white point representing the event horizon. Surrounding it is a thick, swirling accretion disk with a color gradient from dark blue at the inner edge to deep red and orange at the outer edge. A powerful, narrow blue jet of light and gas extends vertically from the center of the disk towards the top of the frame.

Supermassive Black Holes in Active Galactic Nuclei

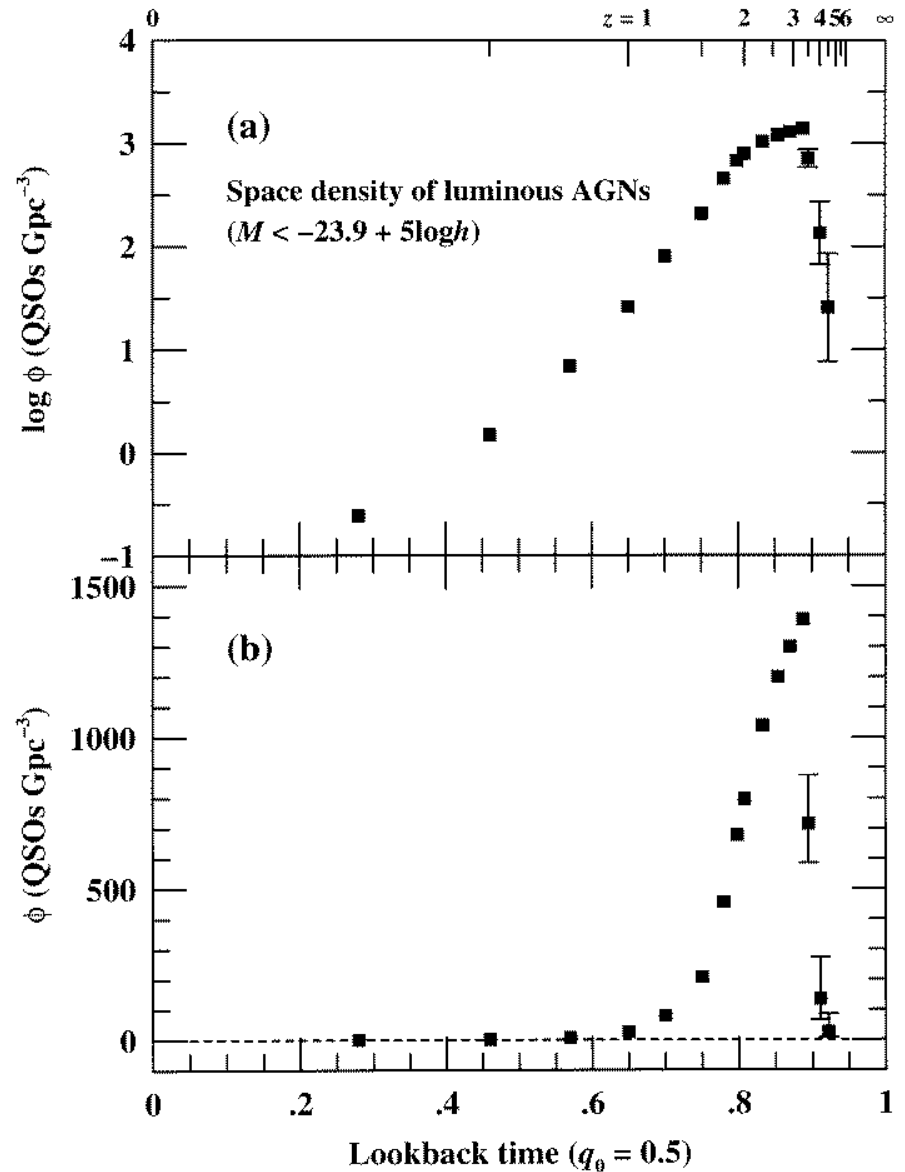
Bradley M. Peterson
The Ohio State University

Topics to be Covered

- *Lecture 1:* AGN properties and taxonomy, fundamental physics of AGNs, AGN structure
- *Lecture 2:* The broad-line region, emission-line variability, reverberation mapping principles, practice, and results, the radius–luminosity relationship, AGN outflows and disk-wind models
- *Lecture 3:* AGN luminosity function and its evolution, role of black holes, direct/indirect measurement of AGN black hole masses, relationships between BH mass and AGN/host properties, “industrial scale” reverberation mapping

Cosmic Evolution of AGNs

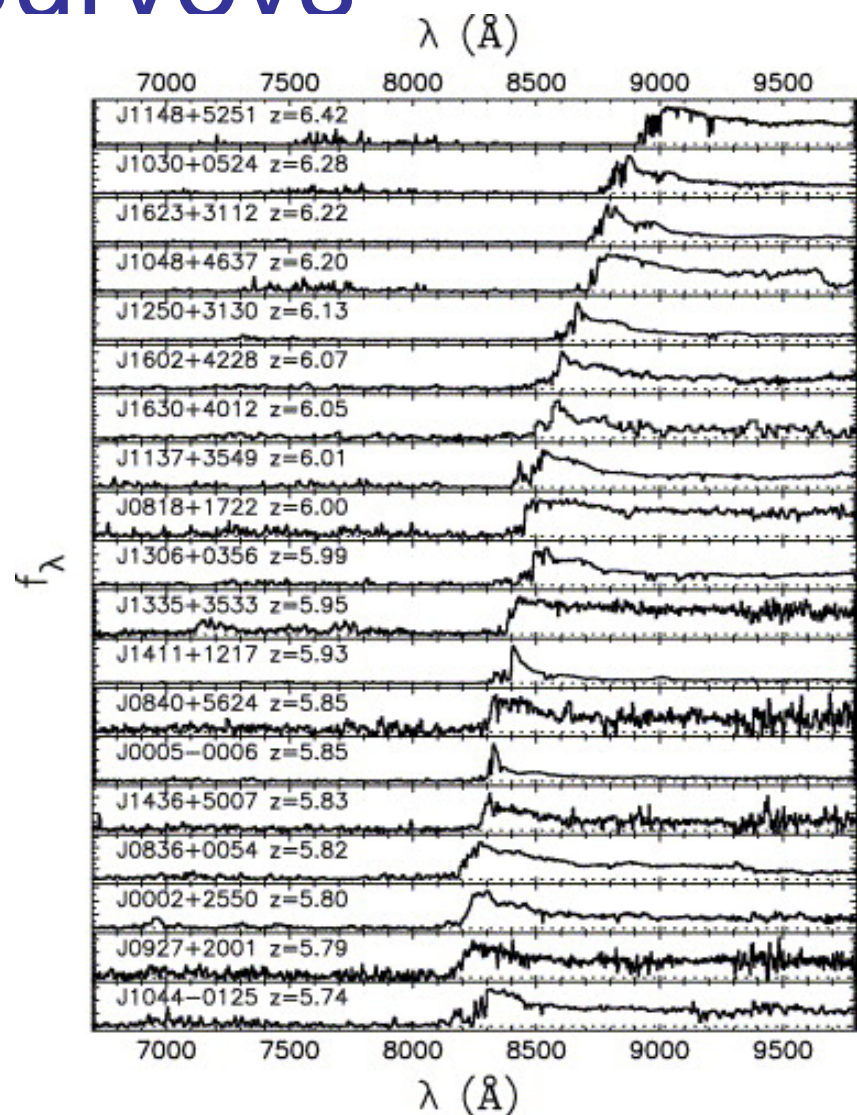
- Very luminous AGNs were much more common in the past.
- The “quasar era” occurred when the Universe was 10-20% its current age.



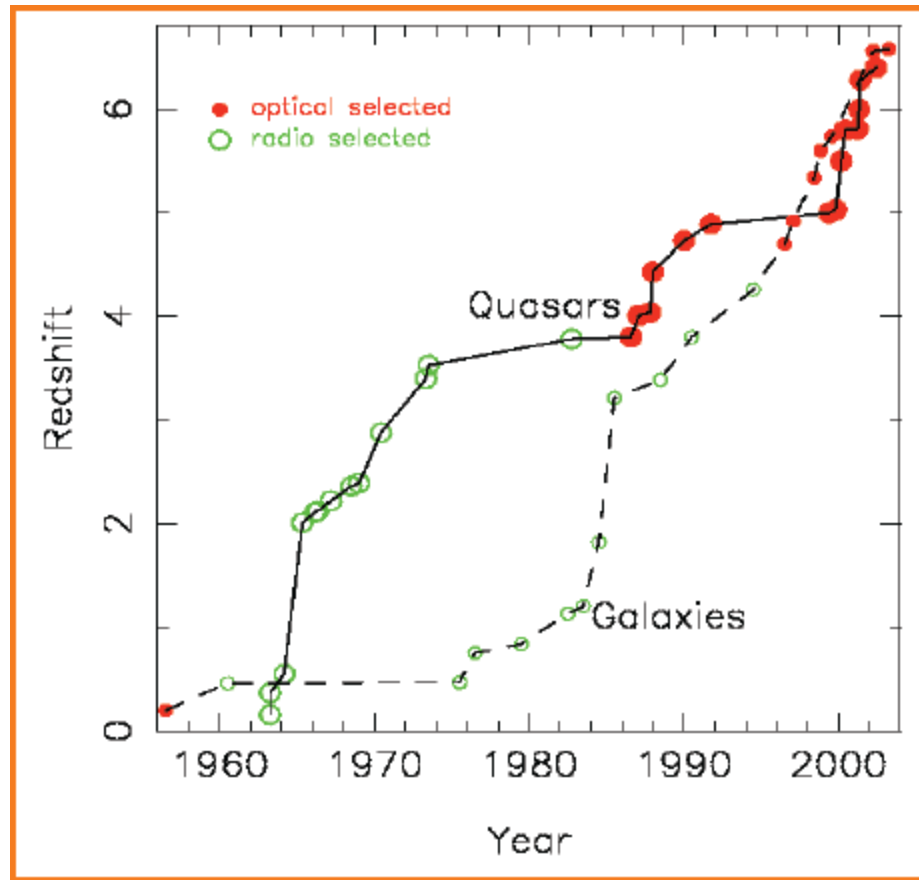
Modern Surveys

- Recent surveys are detecting luminous AGNs at very high redshift and large numbers of quasars at intermediate redshift.

**SDSS quasars
with $z > 5.7$
Fan 2006**

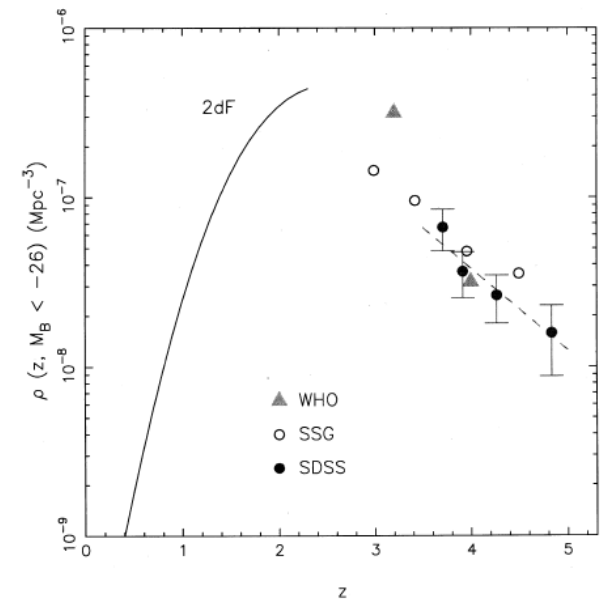


Largest Known Redshifts

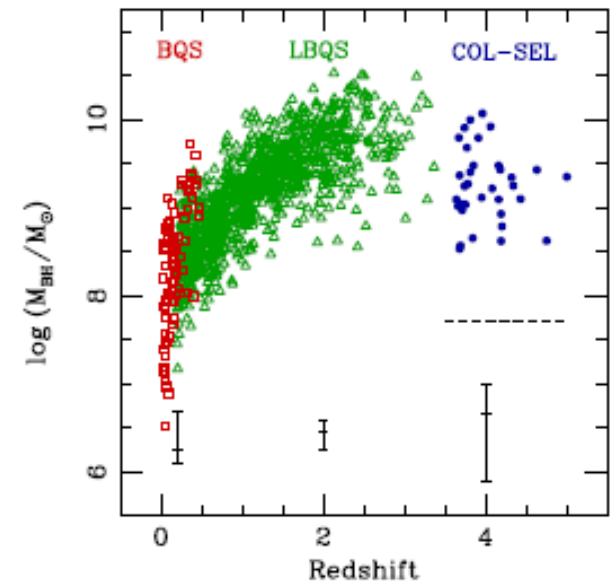


High- z Quasars

- Current highest quasar redshift $z \approx 7.1$
 - Supermassive black holes appeared within a few hundred million years of the Big Bang
 - Metals in their spectra indicate processing in stars already occurred.



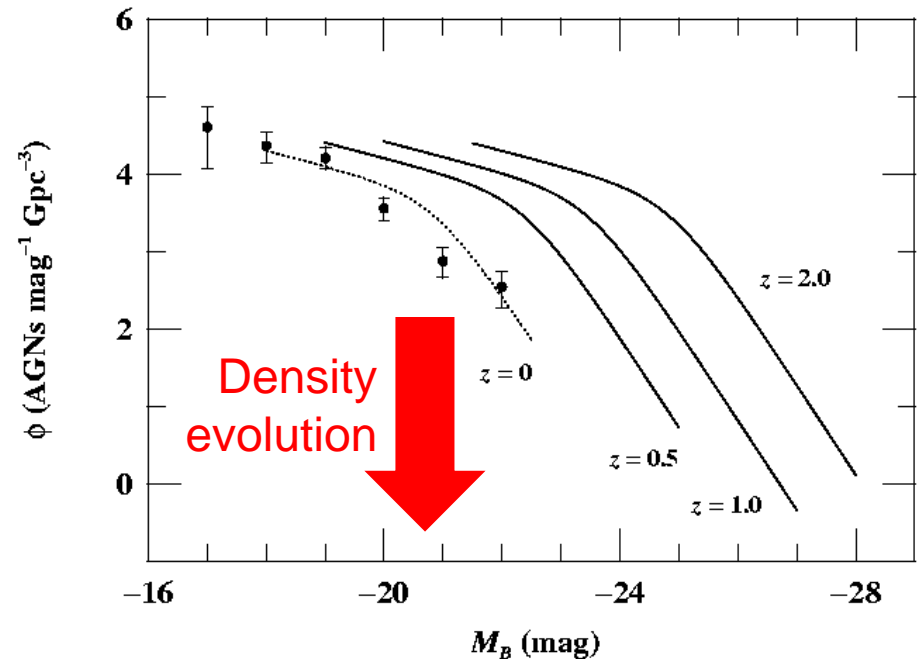
Fan et al. 2001



Vestergaard & Osmer 2009

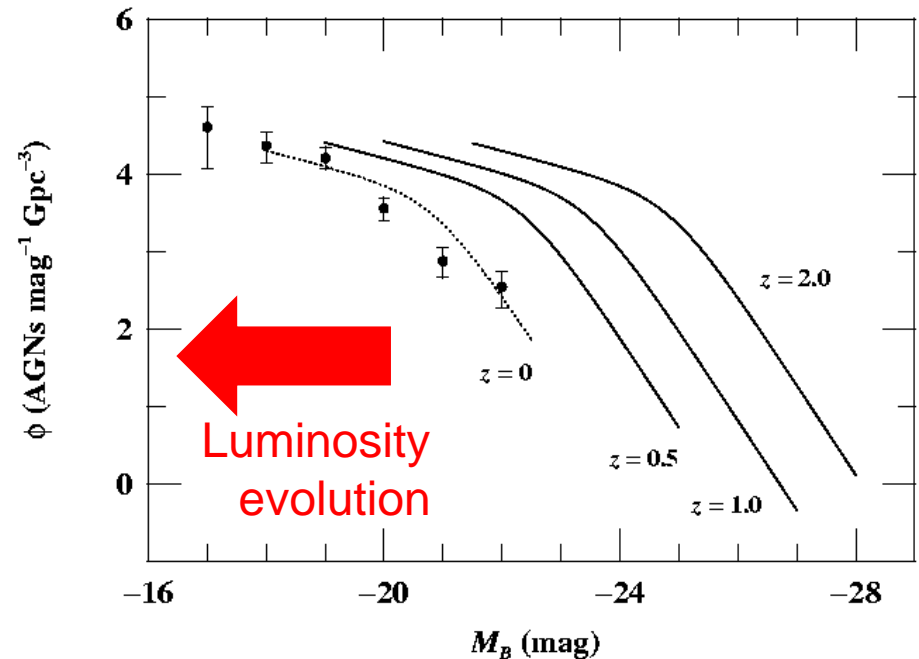
Evolution of the QSO Luminosity Function

- **Density evolution:** quasars “turn off” and luminosity function translates downward.
- Several problems, most importantly that local density of very luminous quasars is overpredicted.



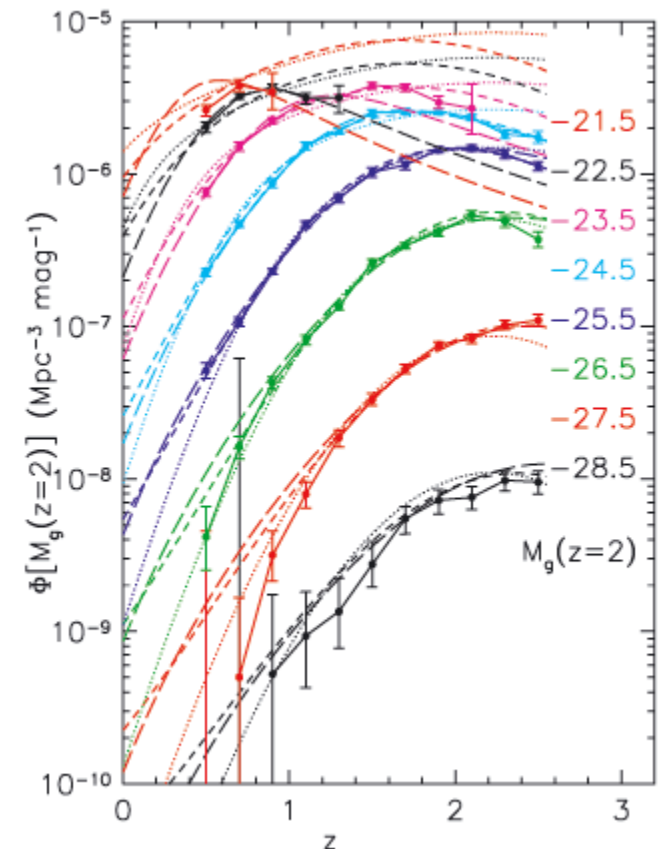
Evolution of the QSO Luminosity Function

- **Luminosity evolution:** quasars just become fainter with time.
- Does not agree with observation that most quasars are emitting near the Eddington limit: the typical nearby quasar is about 50 times fainter than it would have been at $z \approx 2$.



Evolution of the AGN Luminosity Function

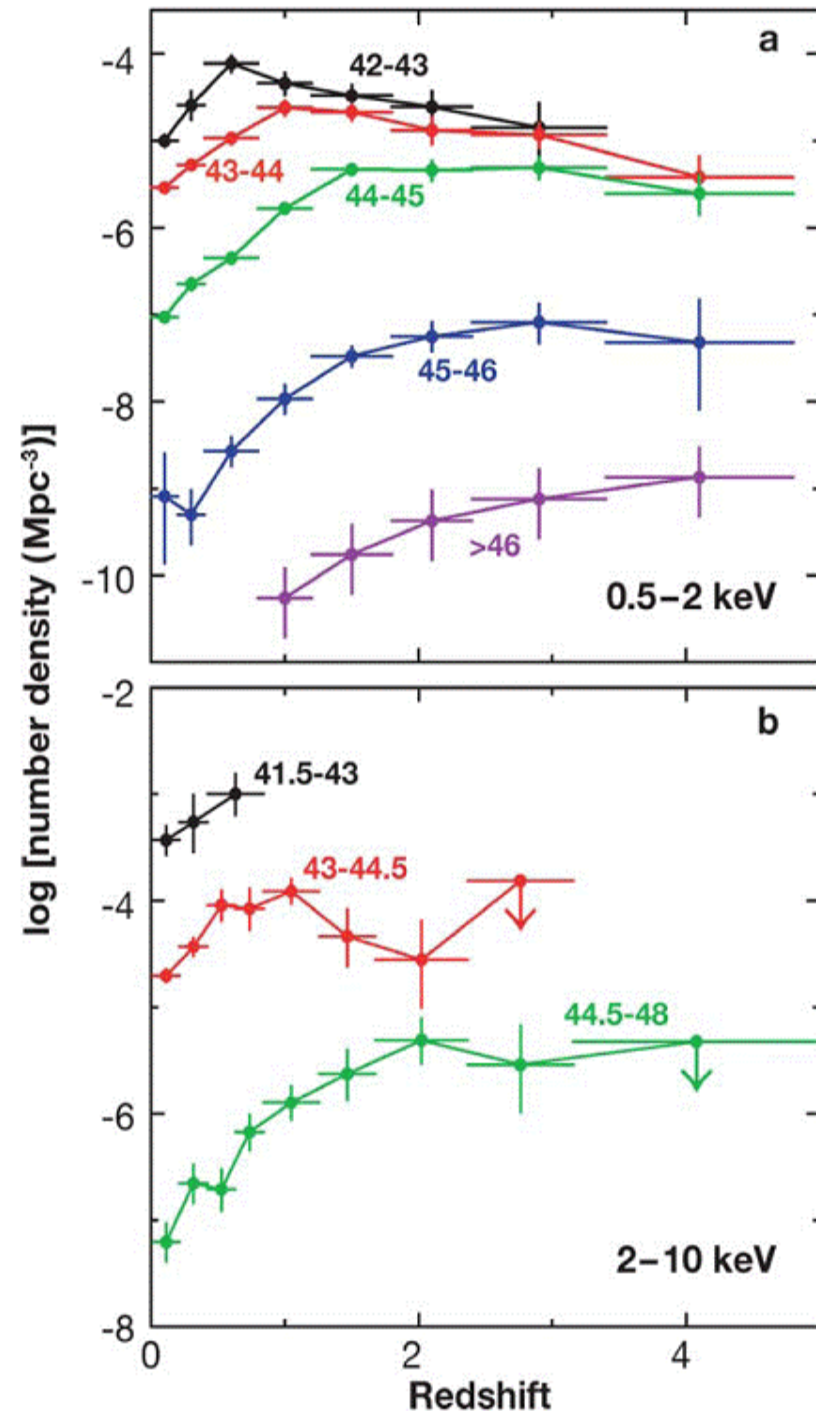
- Because we can now observe lower-luminosity AGNs at high- z , our view of evolution of the luminosity function has changed in the last decade.
- Preferred scenario is now “luminosity-dependent density evolution” (LDDE) or “cosmic downsizing.”



**Comoving density of
2dF+SDSS quasars at different
luminosities.
Croom et al. 2009**

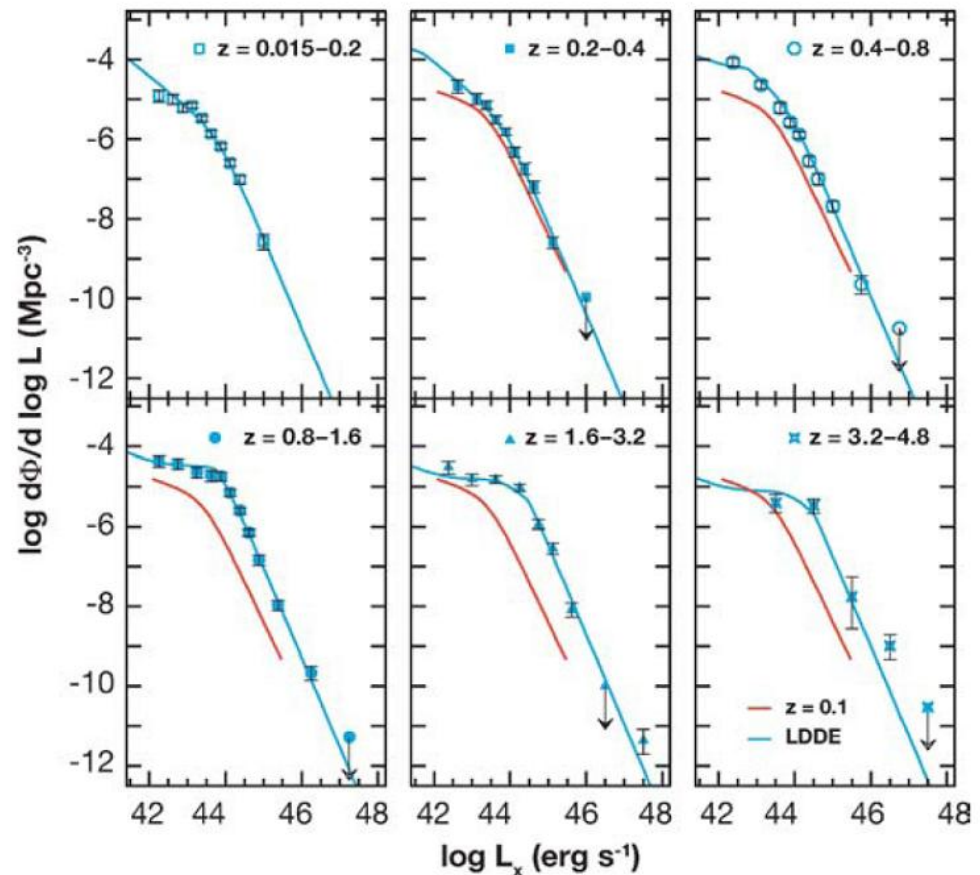
Cosmic Downsizing

- The space density of lower-luminosity AGNs peaks later in time than that of luminous AGNs.



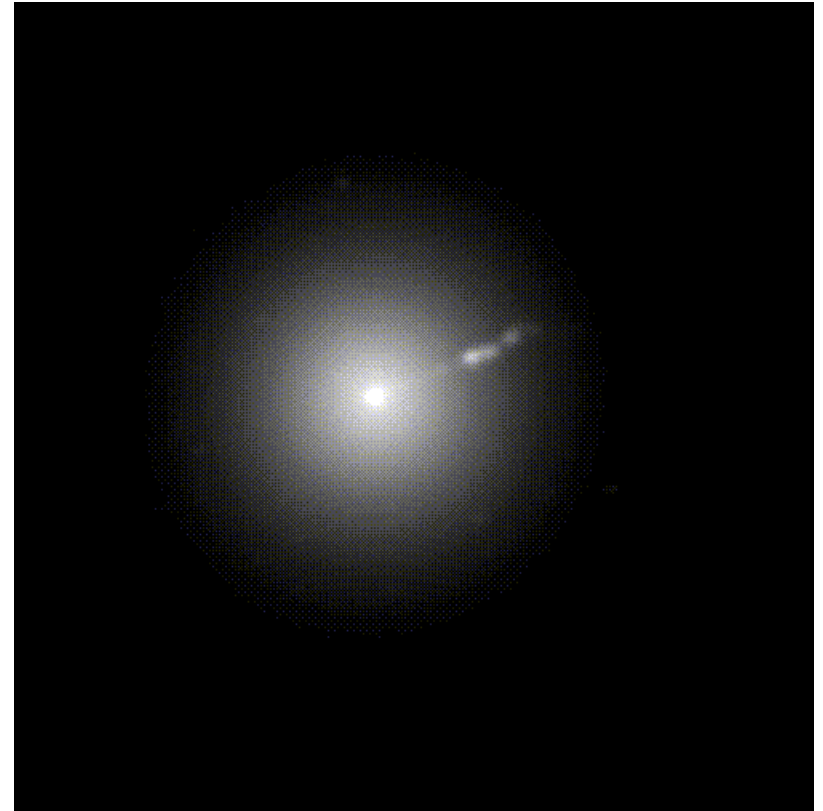
Evolution of the AGN Luminosity Function

- Luminosity-dependent density evolution is most clearly seen in the X-rays
 - Low-luminosity systems are accessible at high z in X-rays



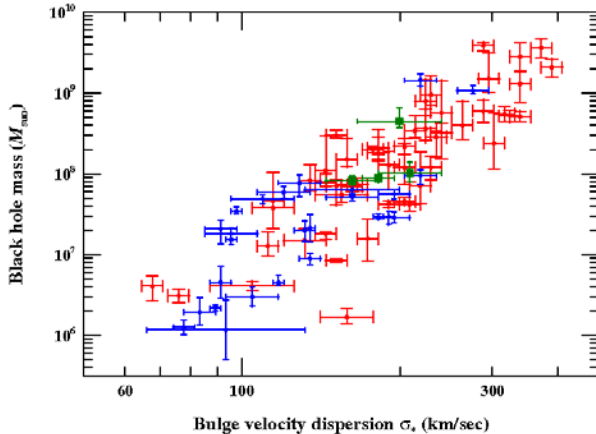
Supermassive Black Holes Are Common

- Supermassive black holes are found in galaxies with large central bulge components.
- These are almost certainly remnant black holes from the quasar era.
- To understand accretion history, we need to determine black-hole demographics.

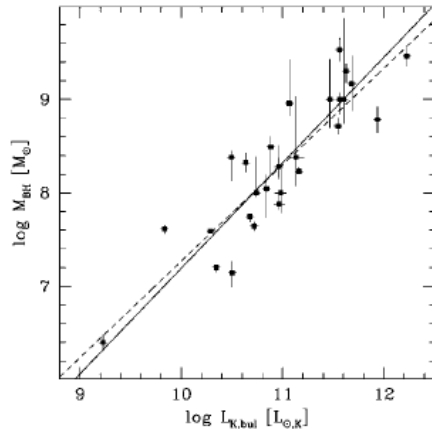


**M 87, a giant elliptical
SMBH $> 3 \times 10^9 M_{\odot}$**

Relationship Between Black Hole Mass and Host Galaxy Properties



$M_{\text{BH}} - \sigma_*$ relationship



$M_{\text{BH}} - L_{\text{bulge}}$ relationship

Marconi & Hunt 2004

- Remarkable since BH constitutes 0.5% of the mass of the bulge.
- Indicates a close (evolutionary?) relationship between BH growth/bulge formation?
 - Do these evolve over time?
- Do supermassive black holes affect their host galaxies?

A Current Paradigm: Feeding and Feedback

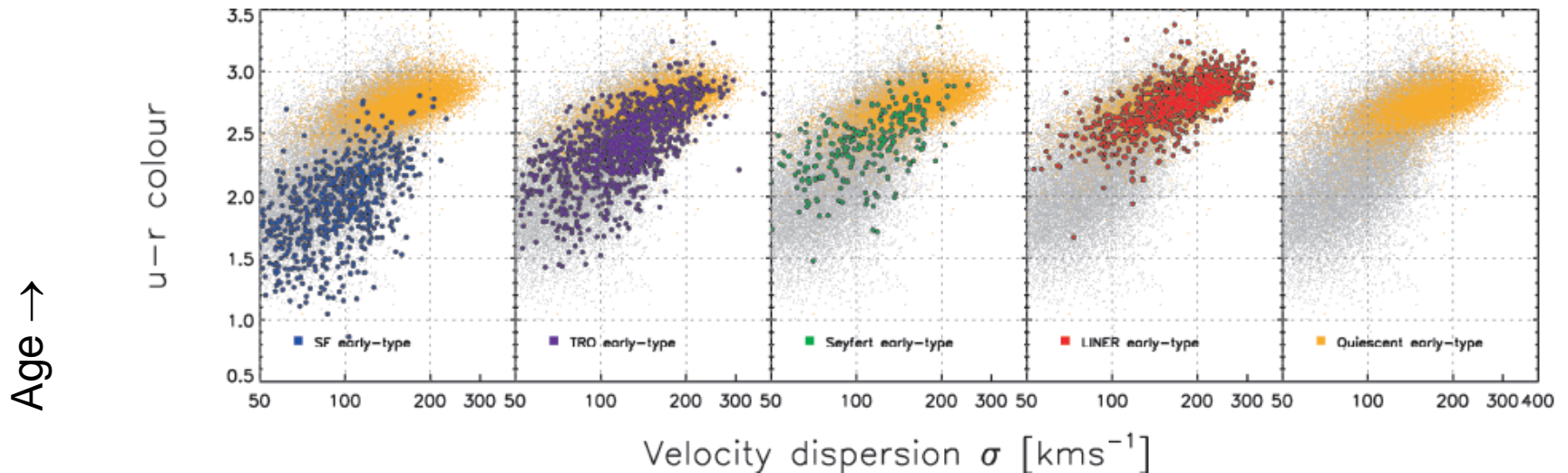
- Supermassive black holes are “active” if there is a large reservoir of gas to “feed” them.
 - Quasars were more common in the past because less gas was locked up in stars; galaxies were gas rich.
- Once a quasar reaches a high-enough luminosity, energetic “feedback” (radiation, winds, jets) from quasars (and massive stars?) heats or removes the ISM, shutting down star formation.
 - There is thus a close correlation between black hole mass and galaxy mass.

Role of Quasars in Galaxy Formation

(or why galaxy formation theorists suddenly like quasars...)

- Models of galaxy formation predict that massive galaxies should still have large reservoirs of gas and active star formation.
- Feedback from accretion onto supermassive black holes might provide the energy necessary to regulate cooling and subsequent star formation.

Does This Represent an Evolutionary Sequence?



Mass →

Schawinski et al. 2007

Orange dots: Quiescent early-type galaxies

Gray dots: Non-early type galaxies

Evolution of the $M_{\text{BH}}-\sigma_*$ and $M_{\text{BH}}-L_{\text{bulge}}$ Relationships

- Some claims for evolution of the $M_{\text{BH}}-\sigma_*$ $M_{\text{BH}}-L_{\text{bulge}}$ relationships, other claims for no evolution, or even no causal relation.
- To test this, we must use (indirect) scaling methods for strong UV emission lines for luminous and distant quasars.
 - One direct (dubious) black hole mass measurement at $z = 2.17$ (Kaspi et al. 2007). No others at $z > 0.3$.

Measuring Central Black-Hole Masses

- Virial mass measurements based on motions of stars and gas in nucleus.
 - Stars
 - Advantage: gravitational forces only
 - Disadvantage: requires high spatial resolution
 - larger distance from nucleus \Rightarrow less critical test
 - Gas
 - Advantage: can be observed very close to nucleus, high spatial resolution not necessarily required
 - Disadvantage: possible role of non-gravitational forces (radiation pressure)

Virial Estimators

Source	Distance from central source
X-Ray Fe $K\alpha$	$3\text{--}10 R_S$
Broad-Line Region	$200\text{--}10^4 R_S$
Megamasers	$4 \times 10^4 R_S$
Gas Dynamics	$8 \times 10^5 R_S$
Stellar Dynamics	$10^6 R_S$

In units of the Schwarzschild radius
 $R_S = 2GM/c^2 = 3 \times 10^{13} M_8 \text{ cm}.$

Mass estimates from the virial theorem:

$$M = f (r \Delta V^2 / G)$$

where

r = scale length of region

ΔV = velocity dispersion

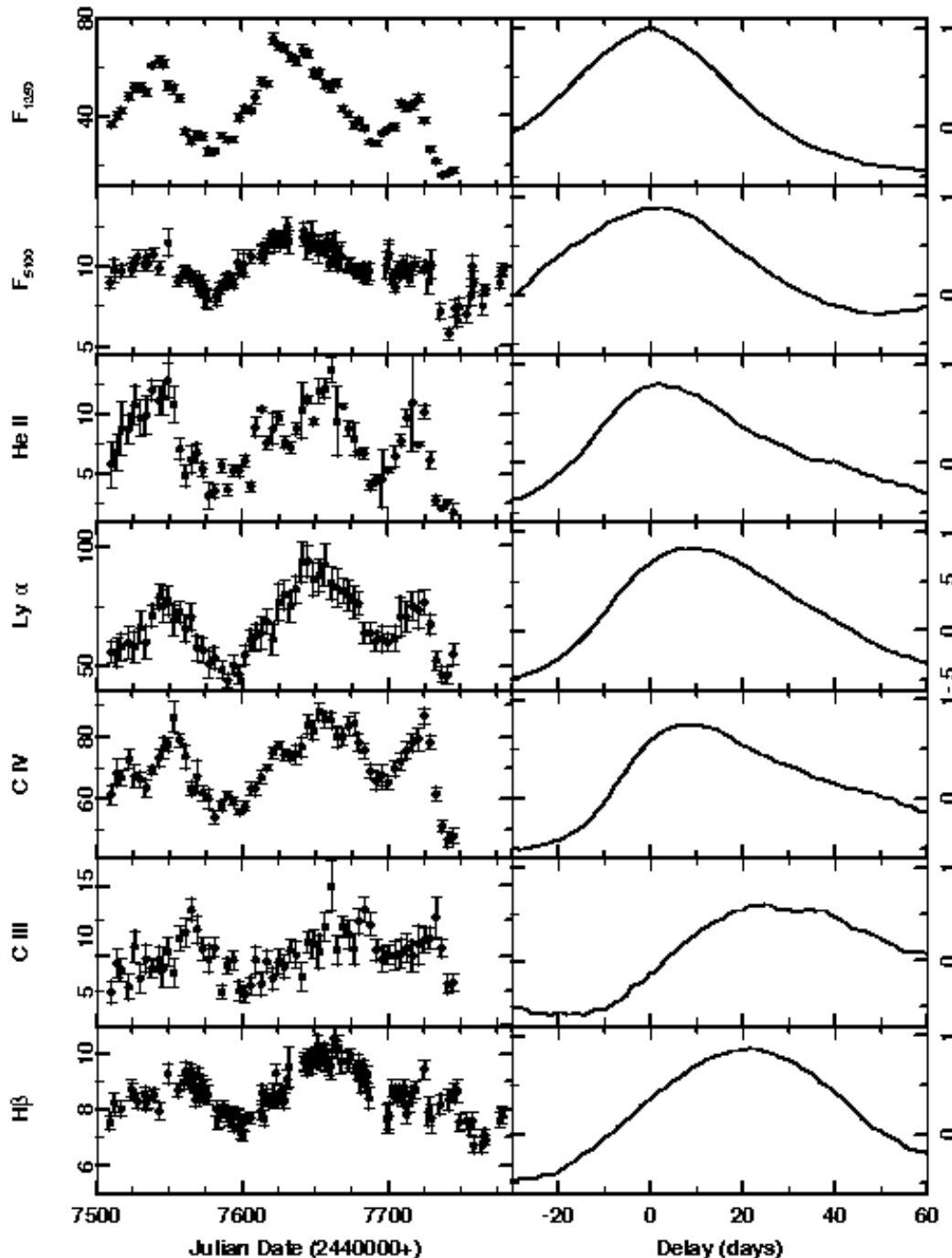
f = a factor of order unity, depends on details of geometry and kinematics

Direct vs. Indirect Methods

- **Direct methods** are based on dynamics of stars or gas accelerated by the central black hole.
 - Stellar dynamics, gas dynamics, reverberation mapping
- **Indirect methods** are based on observables correlated with the mass of the central black hole.
 - $M_{\text{BH}}-\sigma_*$ and $M_{\text{BH}}-L_{\text{bulge}}$ relationships, fundamental plane, AGN scaling relationships ($R_{\text{BLR}}-L$)

“Primary”, “Secondary”, and “Tertiary” Methods

- Depends on model-dependent assumptions required.
- Fewer assumptions, little model dependence:
 - Proper motions/radial velocities of stars and megamasers (Sgr A*, NGC 4258+)
- More assumptions, more model dependence:
 - Stellar dynamics, gas dynamics, reverberation mapping
 - Since the reverberation mass scale currently depends on other “primary direct” methods for a zero point, it is technically a “secondary method” though it is a “direct method.”

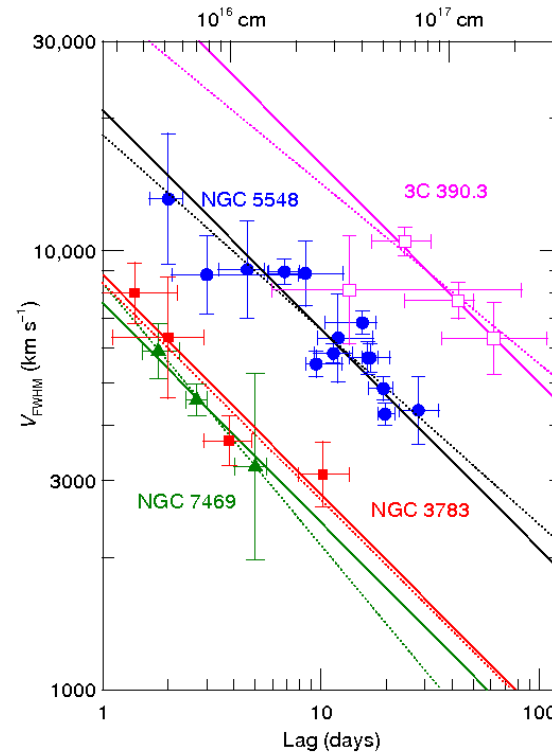


Reverberation Mapping Results

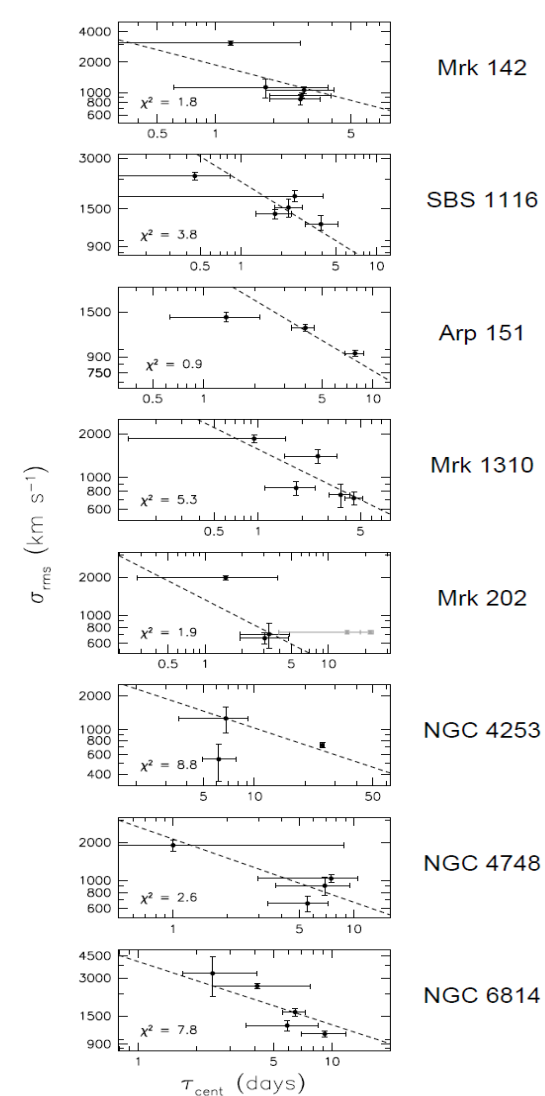
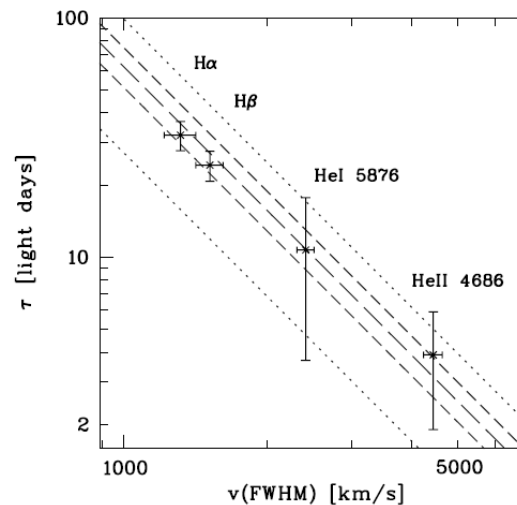
- Reverberation lags have been measured for ~ 50 AGNs, mostly for $\text{H}\beta$, but in some cases for multiple lines.
- AGNs with lags for multiple lines show that highest ionization emission lines respond most rapidly \Rightarrow ionization stratification
 - Highest ionization lines are also broadest!

A Virialized BLR

- $\Delta V \propto R^{-1/2}$ for every AGN in which it is testable.
- Suggests that gravity is the principal dynamical force in the BLR.
 - Caveat: radiation pressure!



Peterson & Wandel 2002



Bentz+ 2009

Kollatschny 2003

Reverberation-Based Masses

“Virial Product” (units of mass)

$$M_{\text{BH}} = f \frac{r \Delta V^2}{G}$$

Observables:

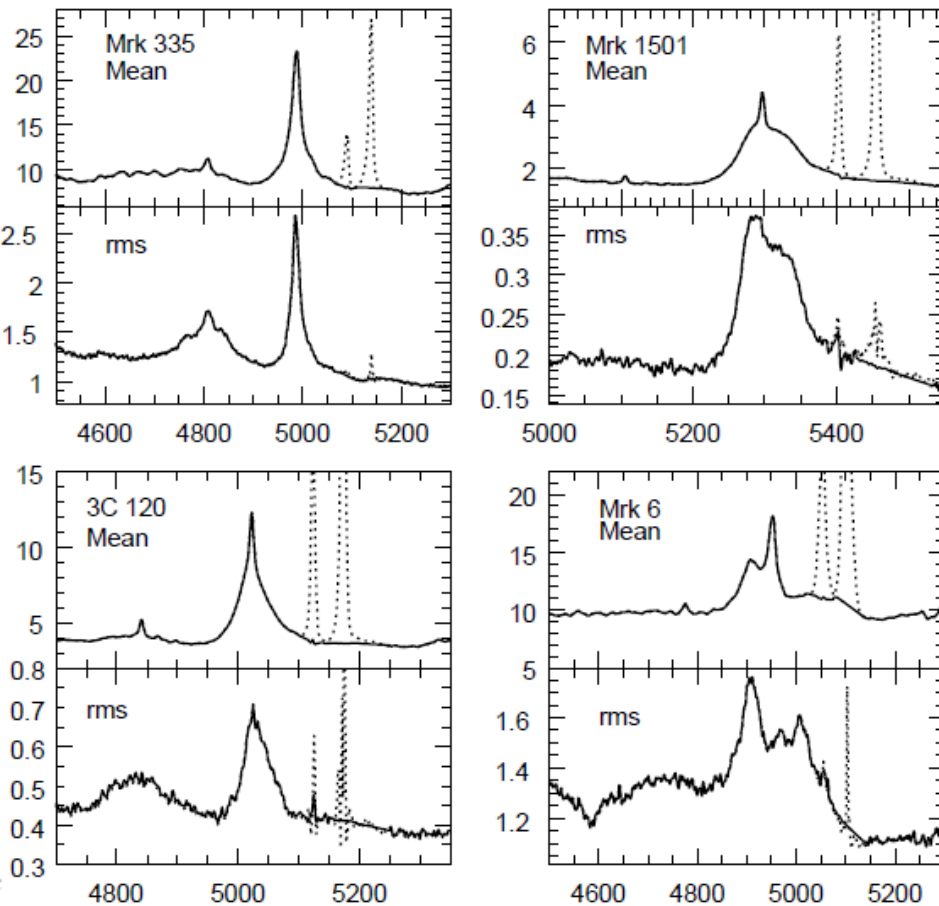
r = BLR radius (reverberation)

ΔV = Emission-line width

Set by geometry and inclination
(subsumes everything we don't know)

If we have independent measures of M_{BH} , we
can compute an ensemble average $\langle f \rangle$

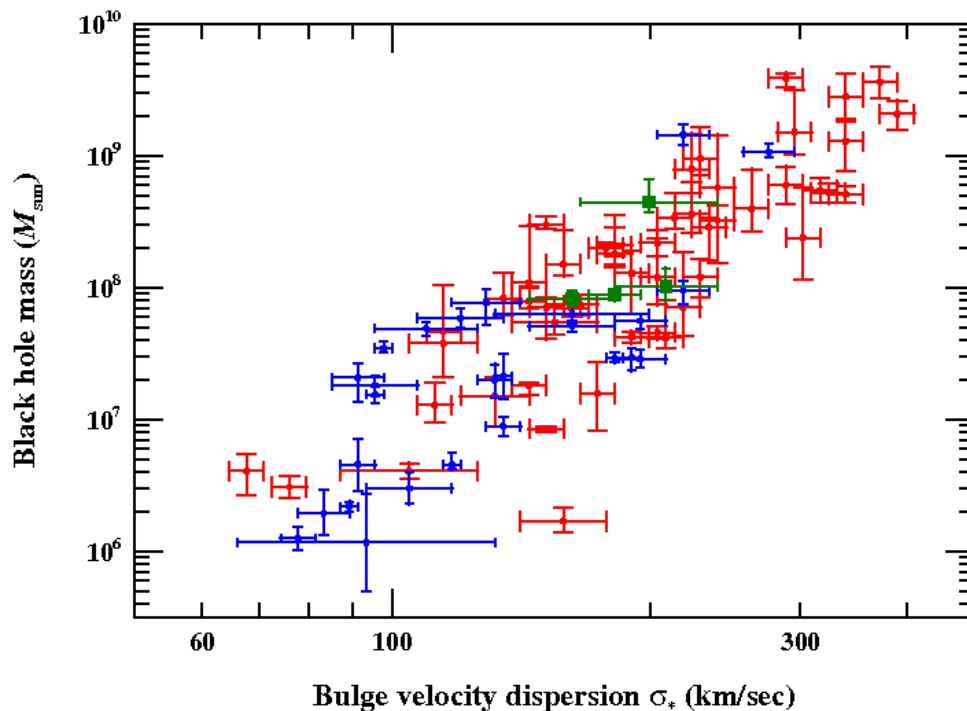
Measuring the Emission-Line Widths



- We preferentially measure line widths in the rms residual spectrum.
 - Constant features disappear, less blending.
 - Captures the velocity dispersion of the gas that is responding to continuum variations.

Grier+ 2012, ApJ, 755:60

AGN $M_{\text{BH}}-\sigma_*$ Relationship

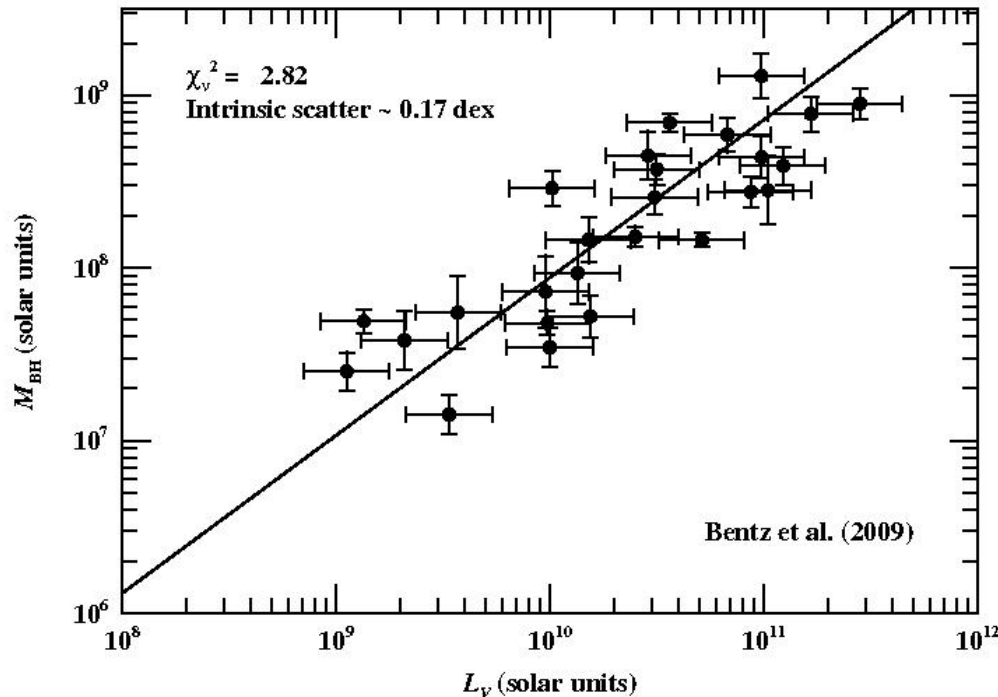


- AGN
- AGN, new H -band σ_*
- Quiescent galaxy

Grier+ 2013, ApJ, 773:90

- Assume zero point of most recent quiescent galaxy calibration.
 $\langle f \rangle = 4.19 \pm 1.08$
- Maximum likelihood places an upper limit on intrinsic scatter
 $\Delta \log M_{\text{BH}} \sim 0.40$ dex.
 - Consistent with quiescent galaxies.

The AGN $M_{\text{BH}}-L_{\text{bulge}}$ Relationship



- Line shows best-fit to quiescent galaxies
- Maximum likelihood gives upper limit to intrinsic scatter $\Delta \log M_{\text{BH}} \sim 0.17$ dex.
 - Smaller than quiescent galaxies ($\Delta \log M_{\text{BH}} \sim 0.38$ dex).

Black Hole Mass Measurements

(units of $10^6 M_{\odot}$)

Galaxy	NGC 4258	NGC 3227	NGC 4151
Direct methods:			
Megamasers	38.2 ± 0.1	N/A	N/A
Stellar dynamics	33 ± 2	7–20	47^{+11}_{-14} †
Gas dynamics	25 – 260	20^{+10}_{-4}	$30^{+7.5}_{-22}$
Reverberation	N/A	7.63 ± 1.7	46 ± 5

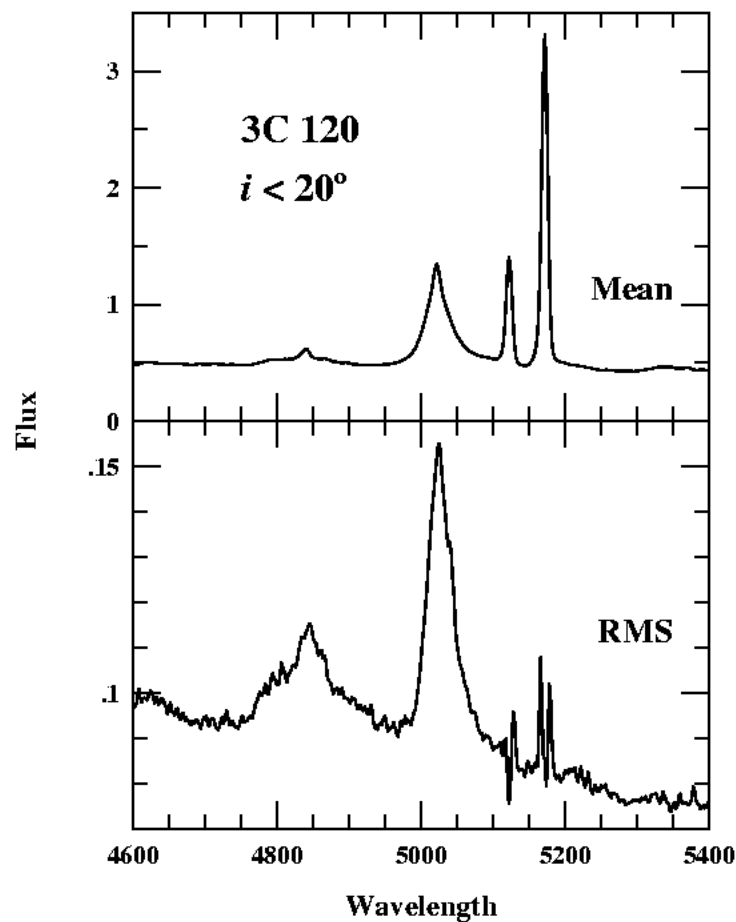
Quoted uncertainties are statistical only, not systematic.

References: see Peterson (2010) [arXiv:1001.3675]

† Onken et al., in preparation

Reverberation-Based Masses

- Combine size of BLR with line width to get the enclosed mass:
$$M_{\text{BH}} = f (r \Delta V^2 / G)$$
- Without knowledge of the BLR kinematics and geometry, it is not possible to compute the mass accurately or to assess how large the systematic errors might be.
 - Low-inclination thin disk ($f \propto 1/\sin^2 i$) could have a huge projection correction.



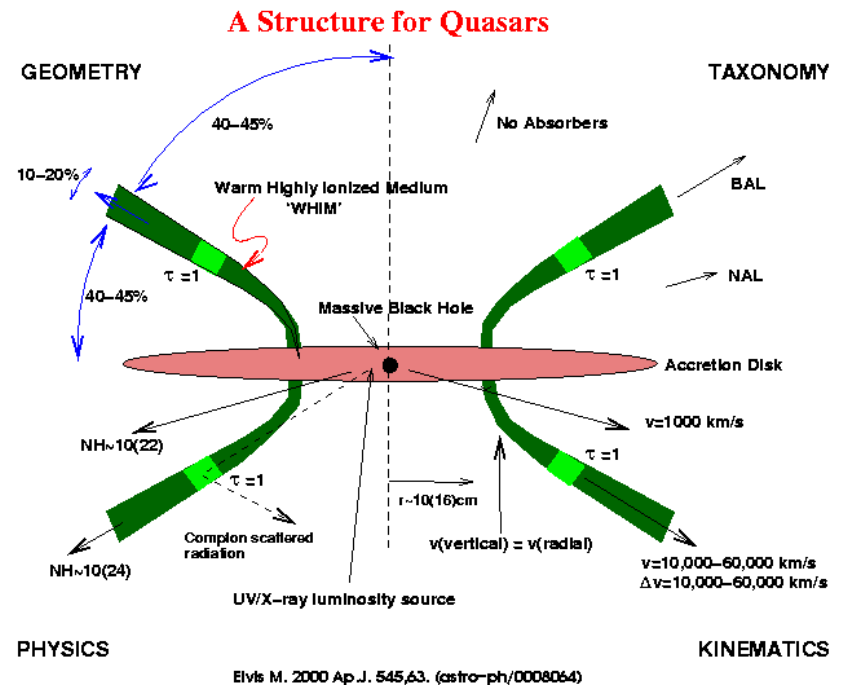
Plausible BLR Geometry

- Unified models suggest that Type 1 AGNs are observed at inclinations $0^\circ \leq i \leq \sim 45^\circ$.

- Lags are unaffected if axial symmetry and isotropic line emission
- Line widths can be severely affected by inclination.
 - A “generalized thick disk” parameterization:

$$f \propto \frac{1}{(a^2 + \sin^2 i)}$$

Collin et al. (2006)



A plausible disk-wind concept based on Elvis (2000)

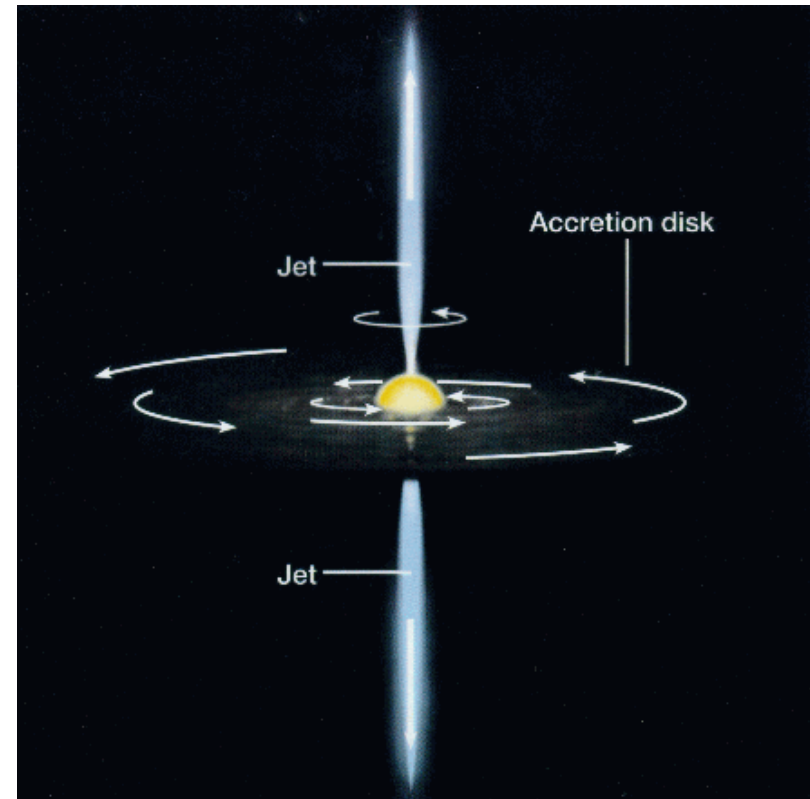
Evidence Inclination Matters

- Relationship between R (core/lobe) and FWHM.
 - Core-dominant are more face-on so lines are narrower.
- Correlation between α_{radio} and FWHM
 - Flat spectrum sources are closer to face-on and have smaller line widths

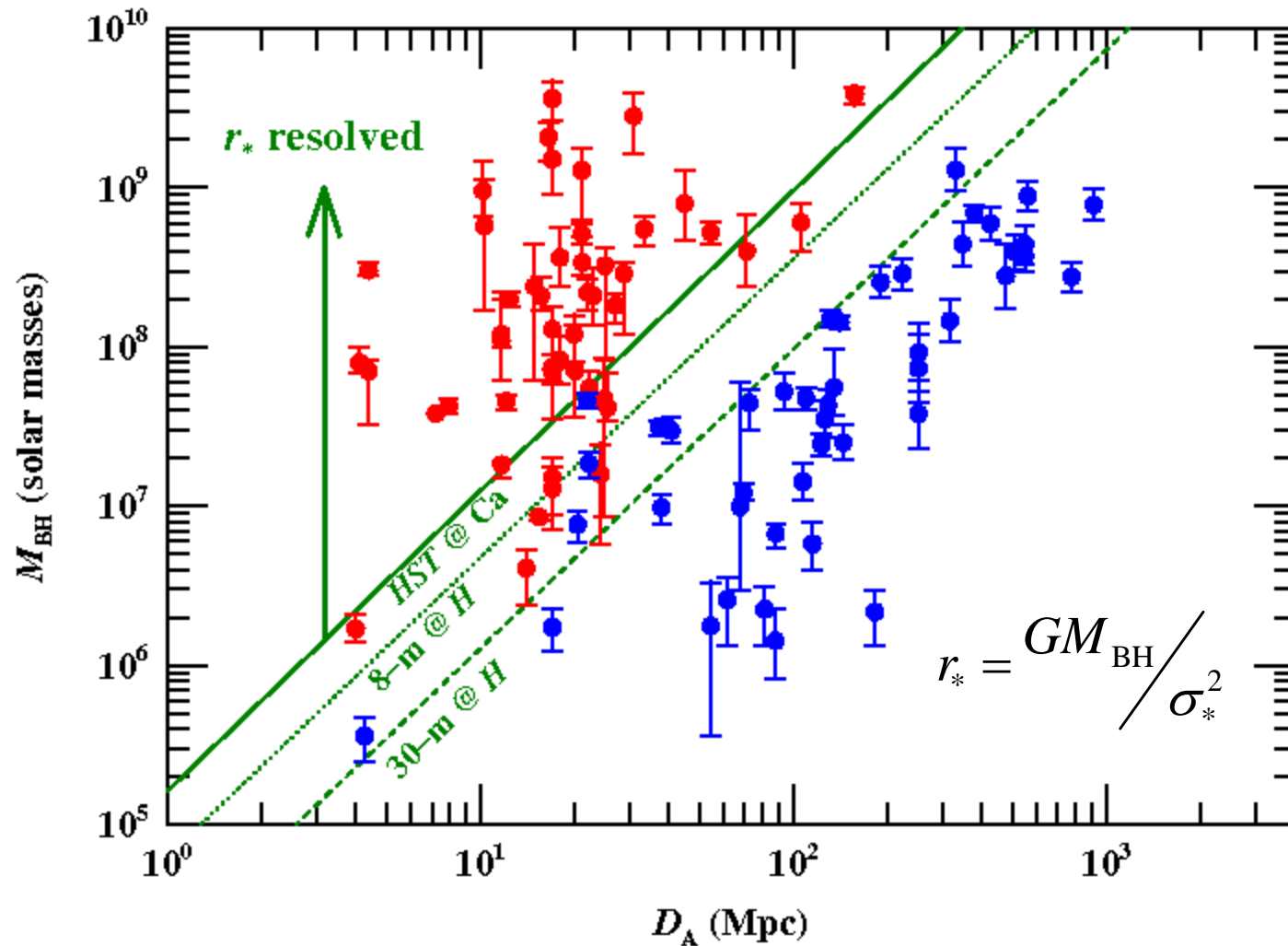
Wills & Browne 1986

- $\alpha_{\text{radio}} > 0.5$: Mean FWHM = 6464 km s^{-1}
- $\alpha_{\text{radio}} < 0.5$: Mean FWHM = 4990 km s^{-1}
- Width distribution for radio-quiet sources like flat spectrum sources (i.e., closer to face-on)

Jarvis & McLure 2006



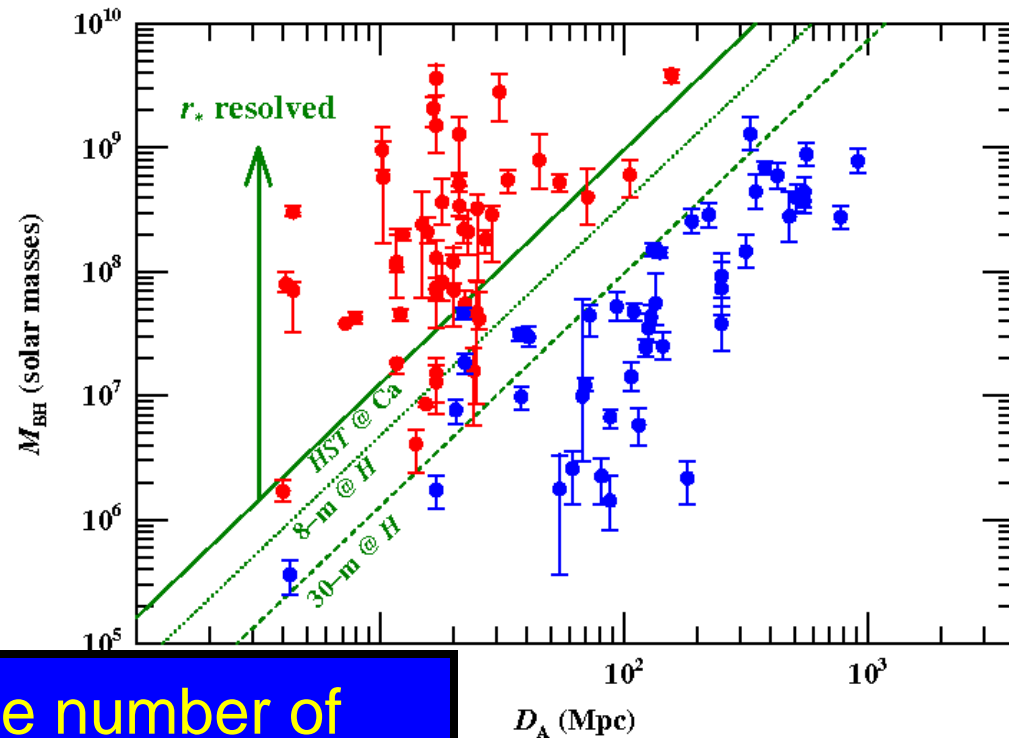
Stellar and gas dynamics requires resolving the black hole radius of influence r_*



- Quiescent galaxies (stellar, gas dynamics, megamasers)
- Reverberation AGNs

Masses of Black Holes in Quasars

- Stellar and gas dynamics requires higher angular resolution to proceed further.
 - Even a 30-m telescope will not vastly expand the number of AGNs with a resolvable r_* .
- Reverberation is the future path for direct AGN black hole masses.
 - Trade time resolution for

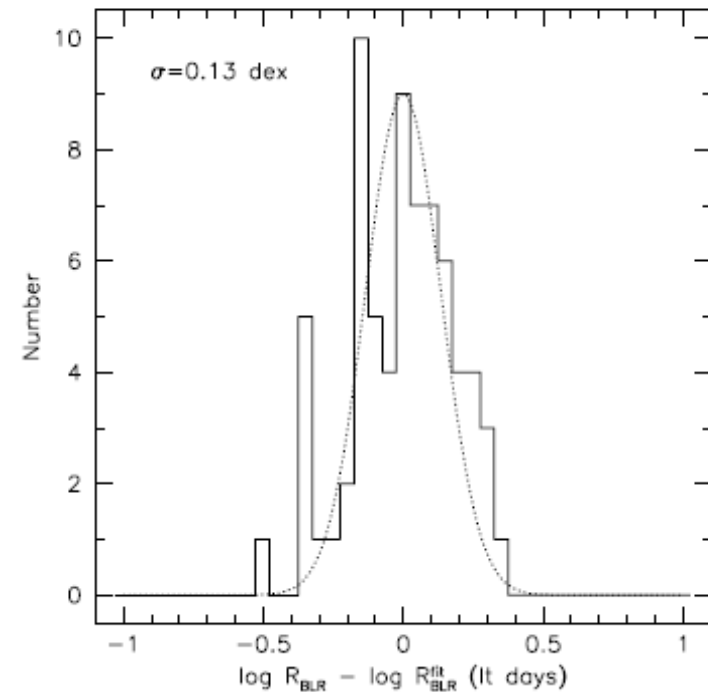
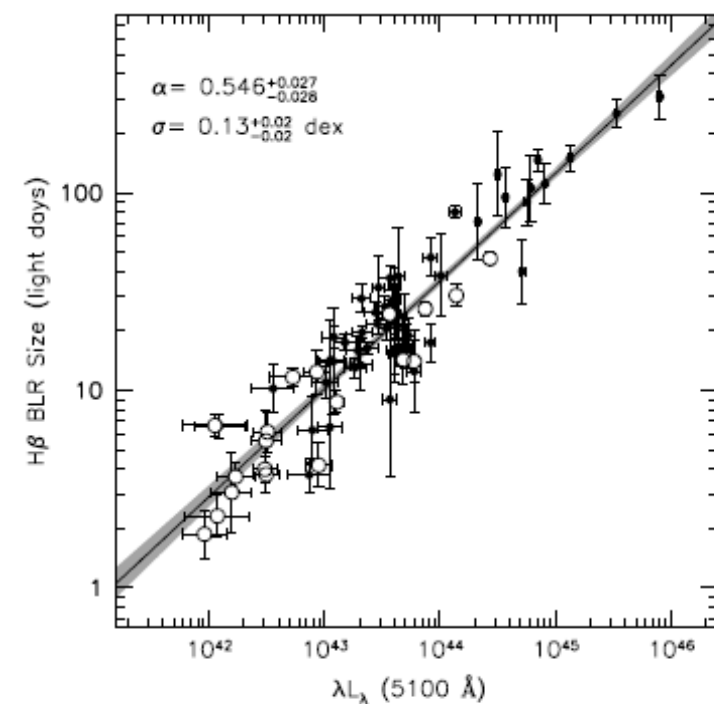


To significantly increase number of measured masses, we need to go to secondary methods.

quiescent galaxies
AGNs

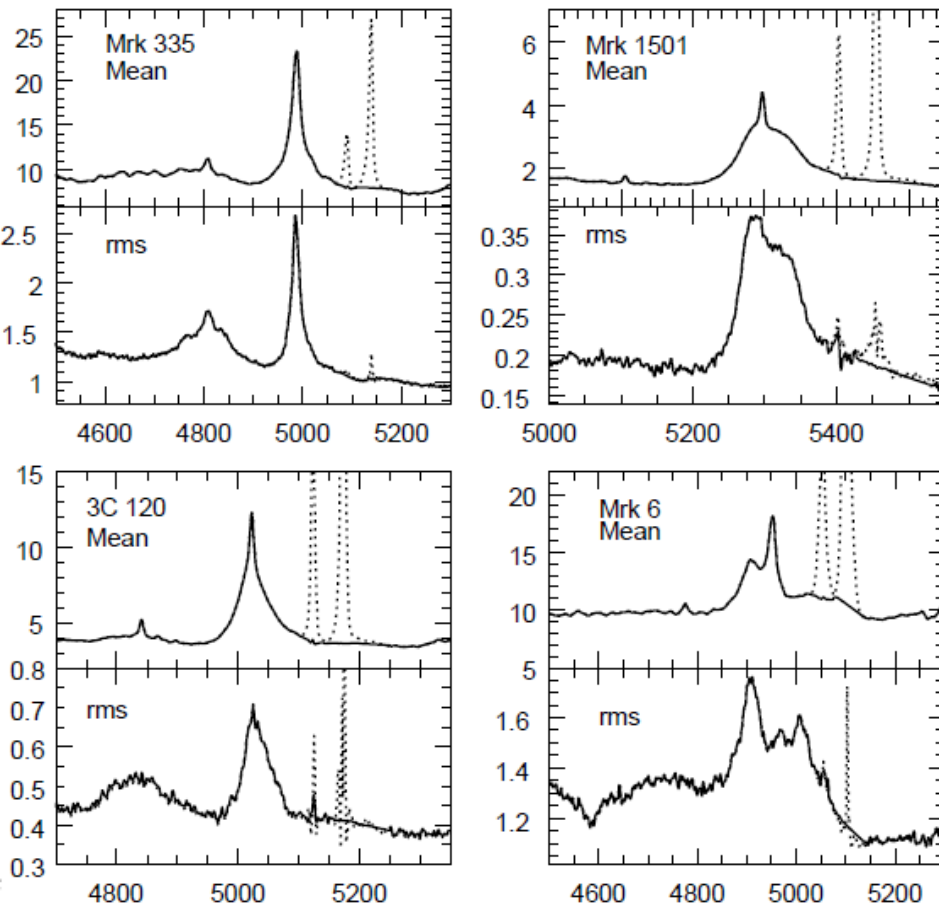
The $R-L$ Relation

- Empirical slope $\sim 0.55 \pm 0.03$
- For $H\beta$ over the calibrated range ($42 \leq \log \lambda L_{5100}$ (ergs s $^{-1}$) ≤ 46 at $z \approx 0$), $R-L$ is nearly as effective as reverberation.



Bentz+ 2013

Measuring the Emission-Line Widths



- Trickier in “mean” or “single-epoch” spectra because of blending.
- Another important issue is how to characterize the line width:
 - FWHM?
 - Line dispersion?

Grier+ 2012, ApJ, 755:60

Characterizing Line Widths

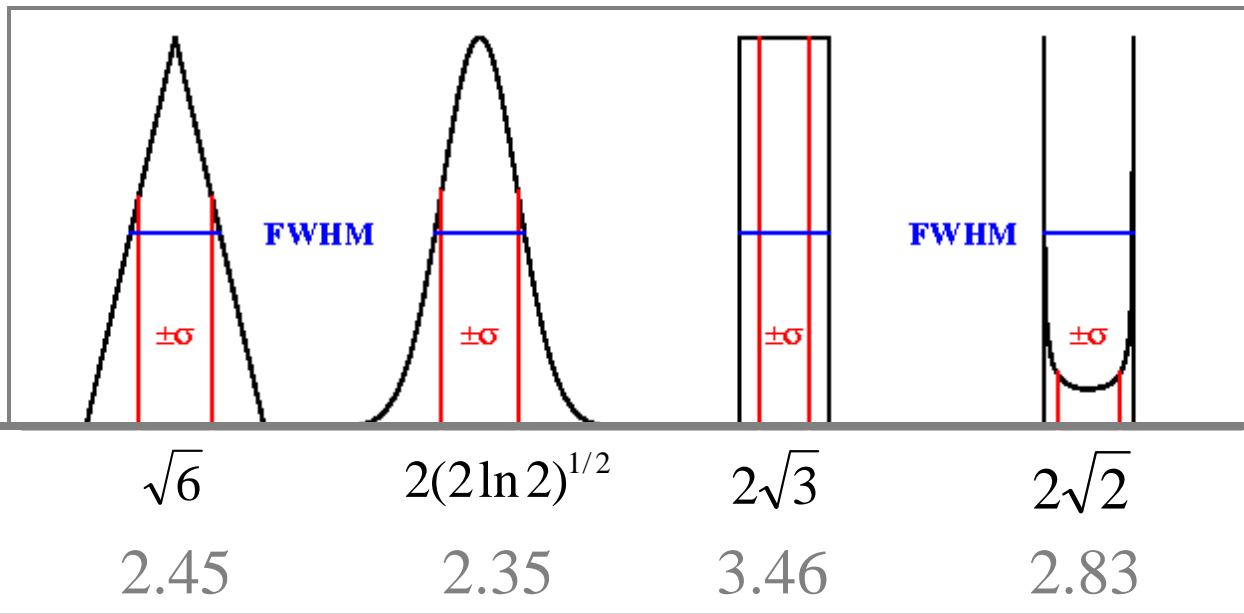
FWHM:

- Trivial to measure
- Less sensitive to blending and extended wings

Line dispersion σ_{line} :

- Well defined
- Less sensitive to narrow-line components
- More accurate for low-contrast lines

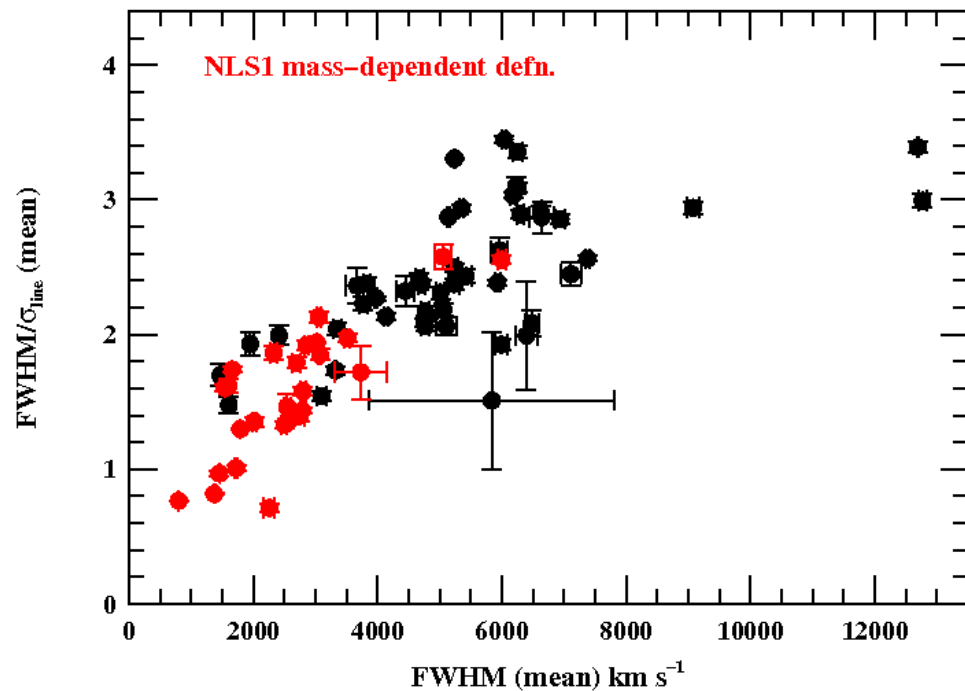
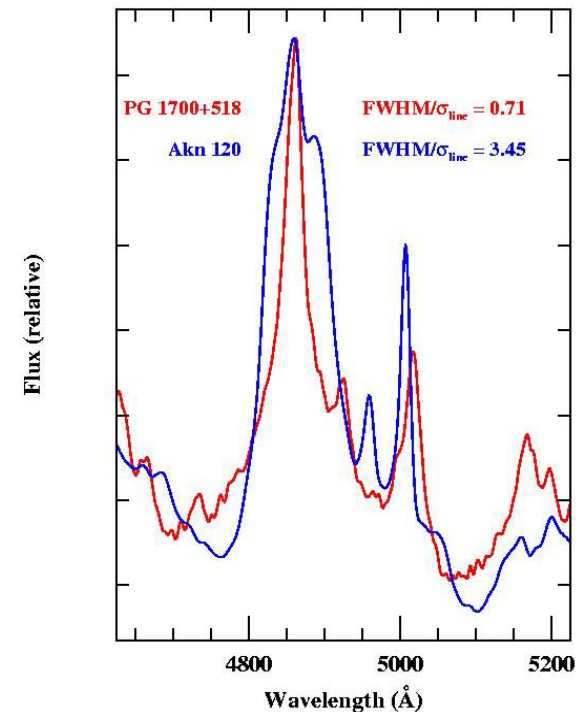
Some trivial profiles:



$$\sigma_{\text{line}} = \langle \lambda^2 \rangle - \lambda_0^2 = \left(\int \lambda^2 P_{\lambda} d\lambda / \int P_{\lambda} d\lambda \right) - \lambda_0^2$$

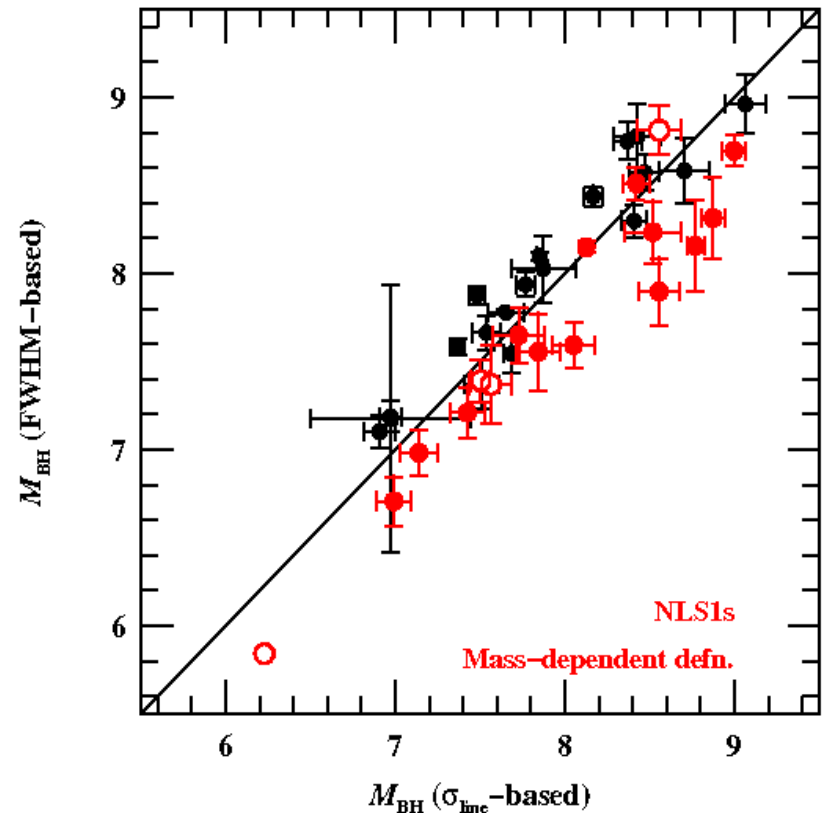
H β Profiles in NLS1s Have Low Values of $\text{FWHM}/\sigma_{\text{line}}$

- This matters because their black hole masses depend on the line width measure (squared!).
- Systematically shifts NLS1s away from other AGN masses.



Incorrect Choice Introduces Bias Based on Line Width

- The importance of this is that the masses are shifted *systematically*
 - In this case, the high-Eddington rate objects have smaller masses for FWHM than for σ_{line}
- Leads to incorrect BH mass function and other troubles...



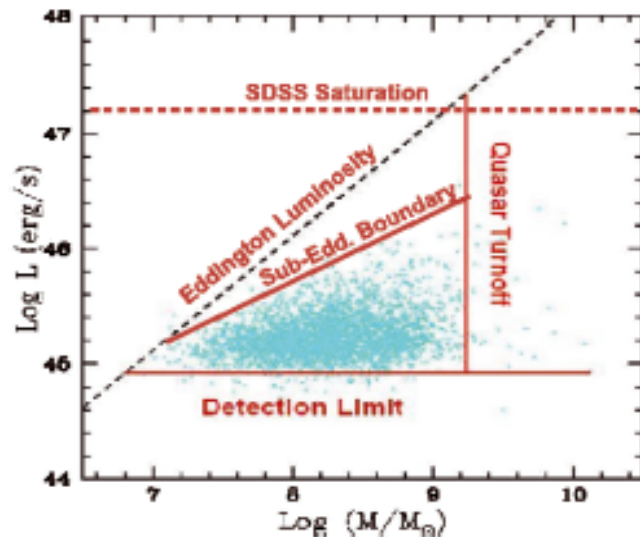
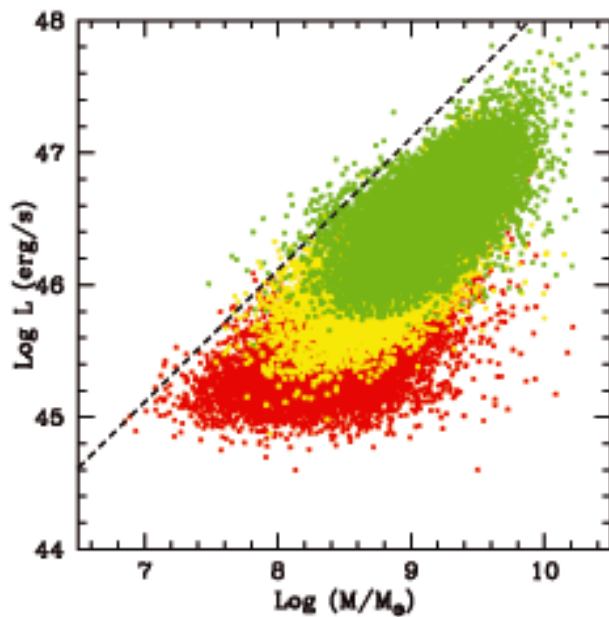
The Sub-Eddington Limit

- The most massive black holes seem to be unable to approach the Eddington limit.

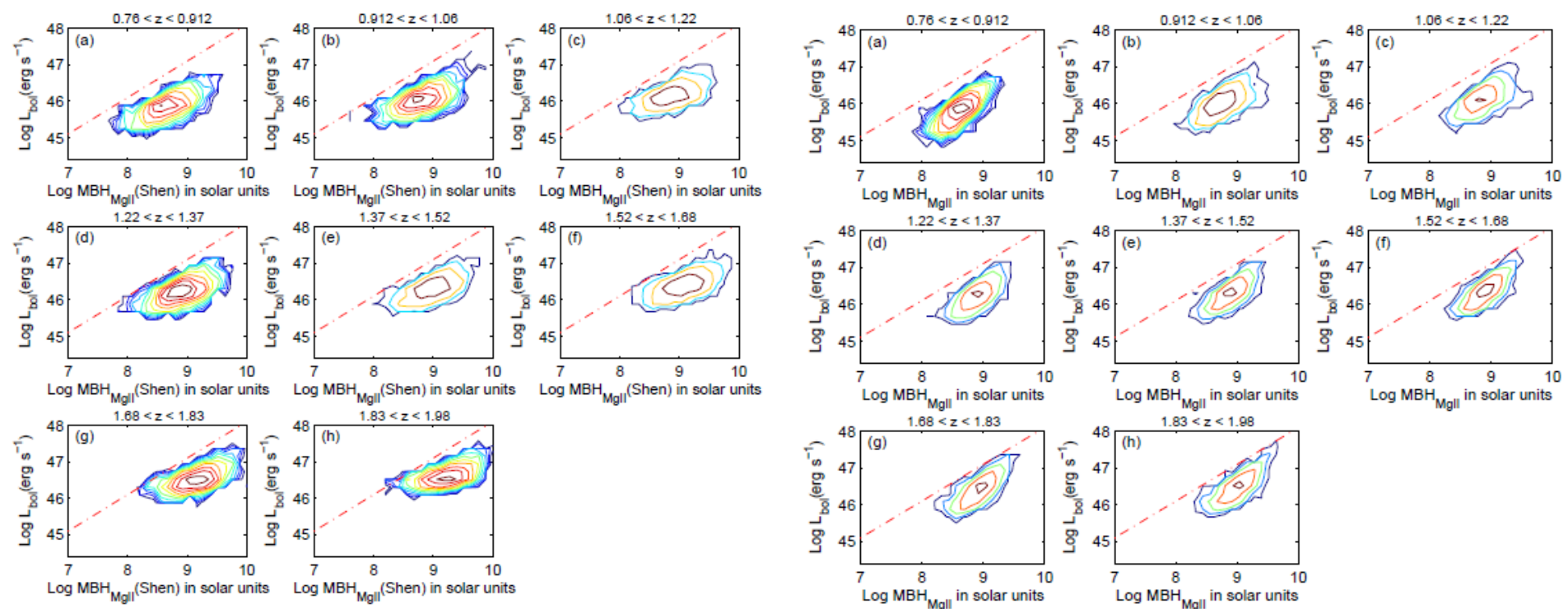
Steinhardt & Elvis 2010

- Line widths used were from Gaussian fits to broad emission lines.

Shen, Greene, et al. 2008



Steinhardt & Elvis 2010



FWHM-based

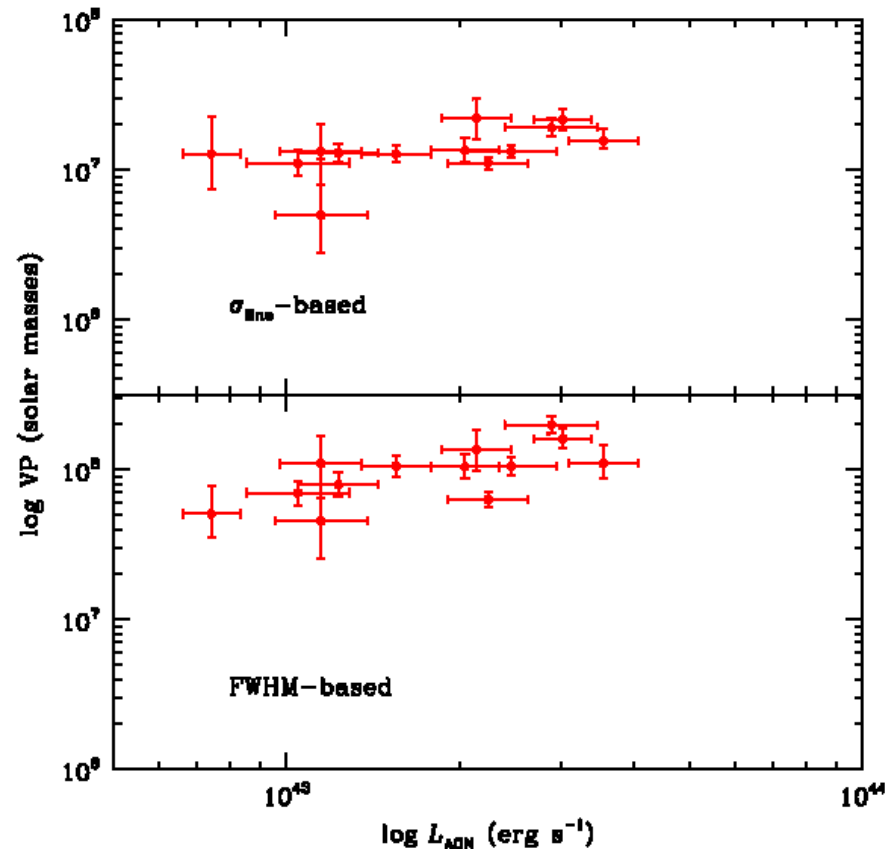
σ_{line} -based

Rafiee & Hall 2011

The sub-Eddington limit vanishes when the masses are based on σ_{line} measured directly from the spectra instead of FWHM from a Gaussian fit.

Direct Observational Test: Mass Must Be Constant

- Only NGC 5548 has much dynamic range
 - σ_{line} is slightly favored, but only slightly



Black Hole Mass Measurements

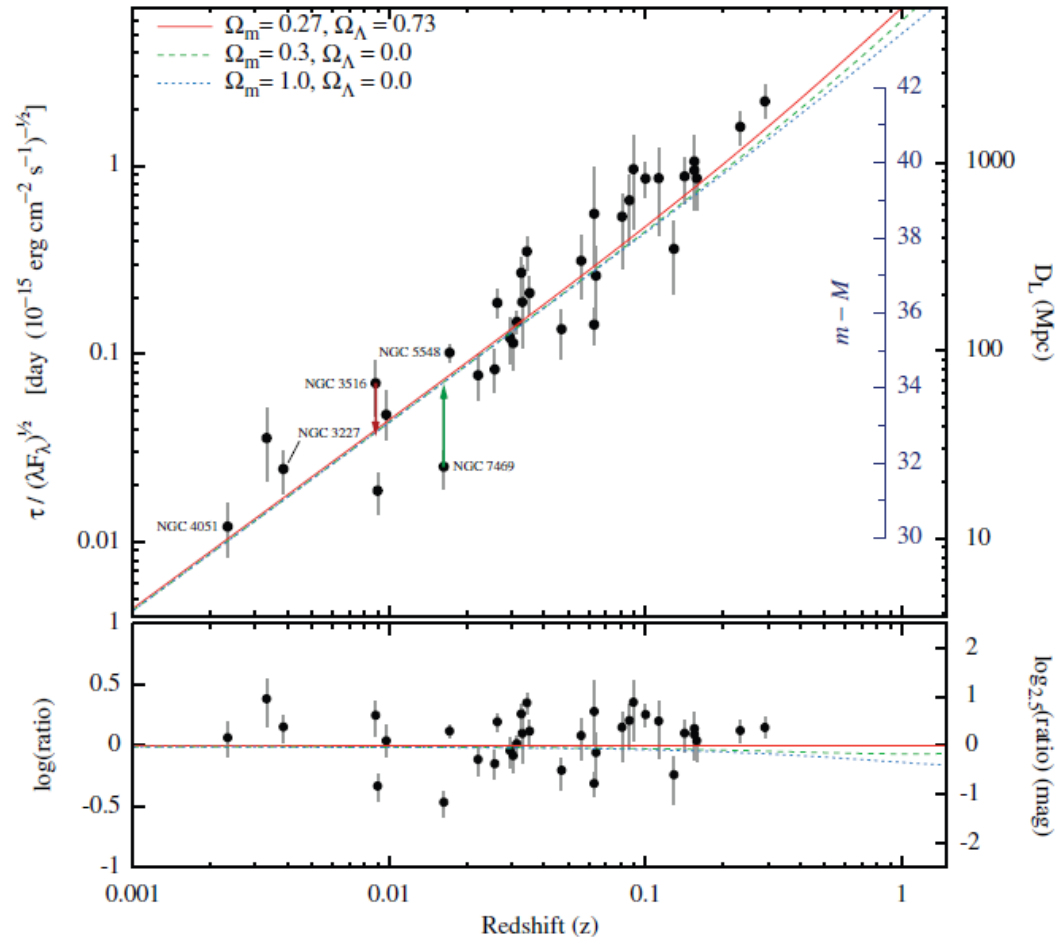
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Gas dynamics	25 – 260	20^{+10}_{-4}	$30^{+7.5}_{-22}$
Reverberation	N/A	7.63 ± 1.7	46 ± 5
Indirect Methods:			
$M_{\text{BH}}-\sigma_*$	13	25	6.1
$R-L$ scaling	N/A	15	65

References: see Peterson (2010) [arXiv:1001.3675]

Cosmological Applications

- Because the $R-L$ relationship has so little scatter, cosmological applications are possible.
- $R \Rightarrow L \Rightarrow D_L$



Watson, Denney, Vestergaard, & Davis 2011

Reverberation Mapping Goals

- Determine geometry and kinematics of BLR
- Determine black hole masses
- Calibrate scaling relationships for indirect black hole mass estimates
- Determine/confirm cosmological parameters

Reverberation Mapping Goals

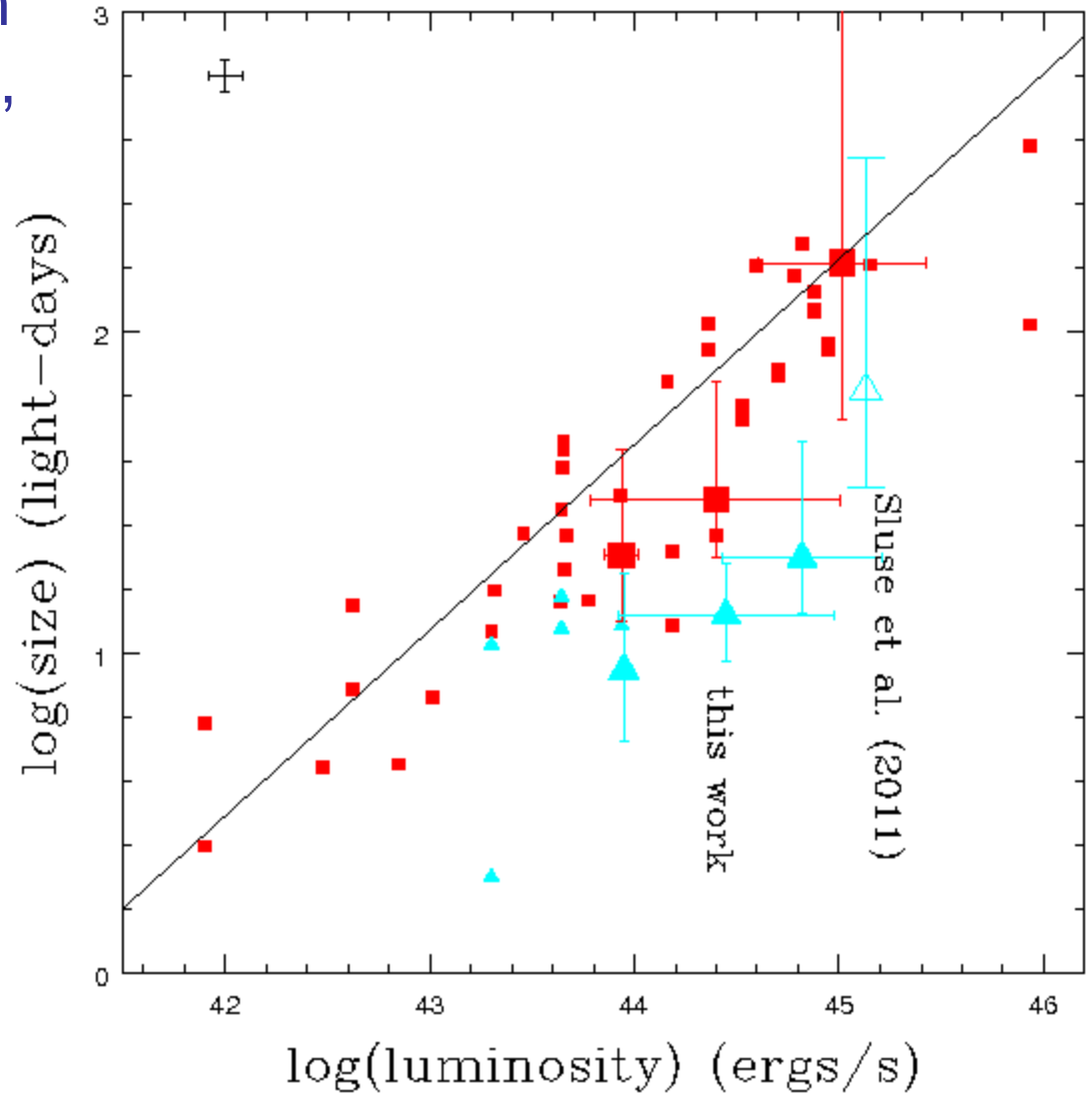
- Geometry and kinematics of BLR
 - Velocity-resolved RM (**expensive!**)
- Black hole masses
 - High accuracy ($\sim 50\%$ or better)
 - Velocity-resolved RM (**expensive!**)
 - Moderate accuracy (factor of $\sim 3\text{--}5$)
 - Mean lag measurement (**moderately expensive**)
 - High S/N single spectra + scaling relationships (**somewhat expensive**)
 - Low accuracy (order of magnitude)
 - Survey-quality single spectra + scaling relationships (**inexpensive. But you get what you pay for**)

Reverberation Mapping Goals

- Calibrate scaling relationships for indirect black hole mass estimates
 - H β $R-L$ well-characterized with intrinsic scatter ~ 0.13 dex
 - Still somewhat of an open issue for other lines
 - Or is it?

Independent confirmation
of $R-L$ from microlensing,
including high-ionization
lines.

- RM measurements,
low ionization lines
- Microlensing,
Low-ionization lines
- RM measurements,
high-ionization lines
- Microlensing,
high-ionization lines



Guerras, Kochanek + 2012

Reverberation Mapping Goals

- Calibrate scaling relationships for indirect black hole mass estimates
- Cosmological applications

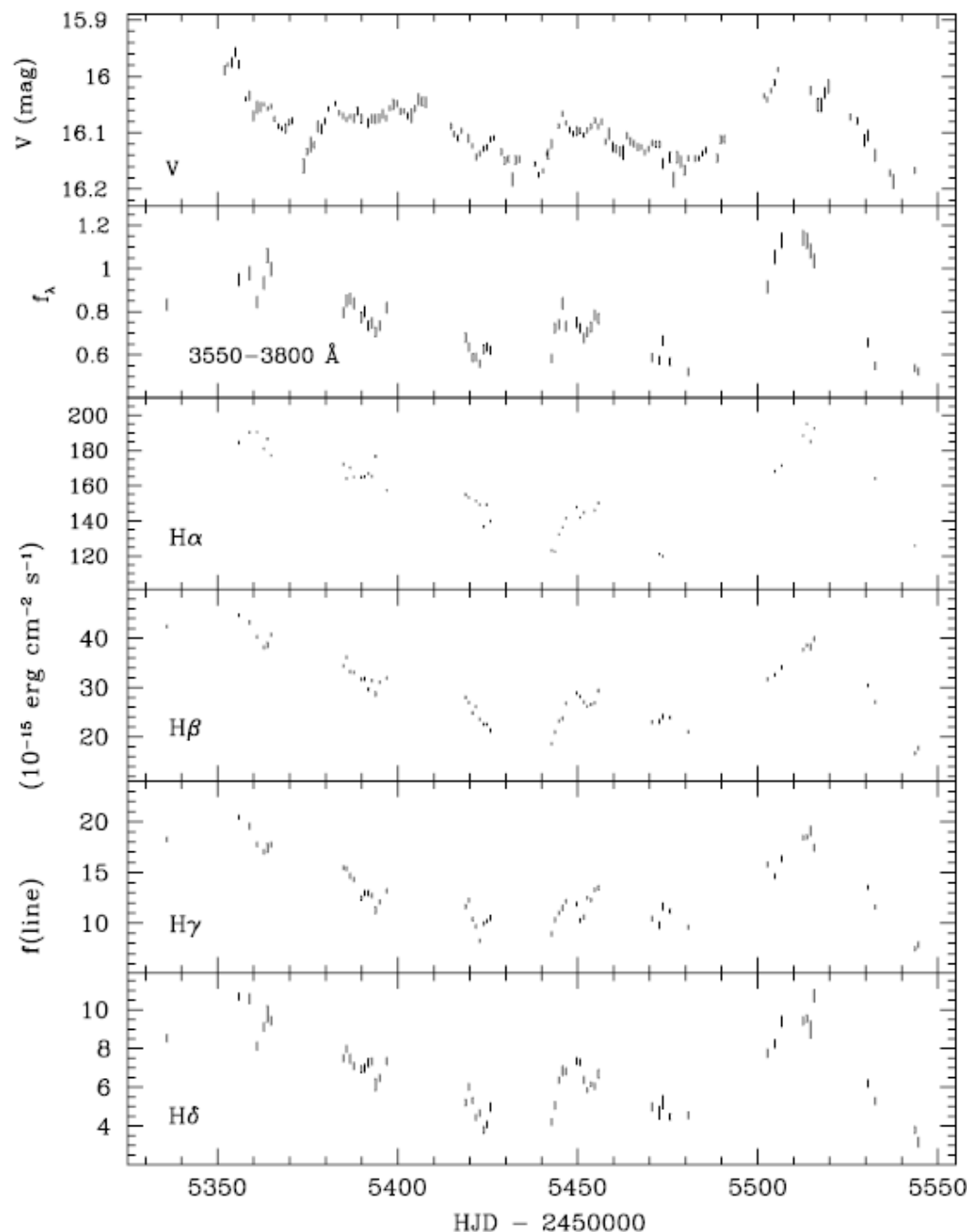
These require measurement of BLR size, preferably in a large number of sources. Are there less expensive ways to do this?

Sparse Sampling

- If you have a good continuum light curve, you can get by with more sparsely sampled line light curves
 - Especially if you use multiple lines with different lags

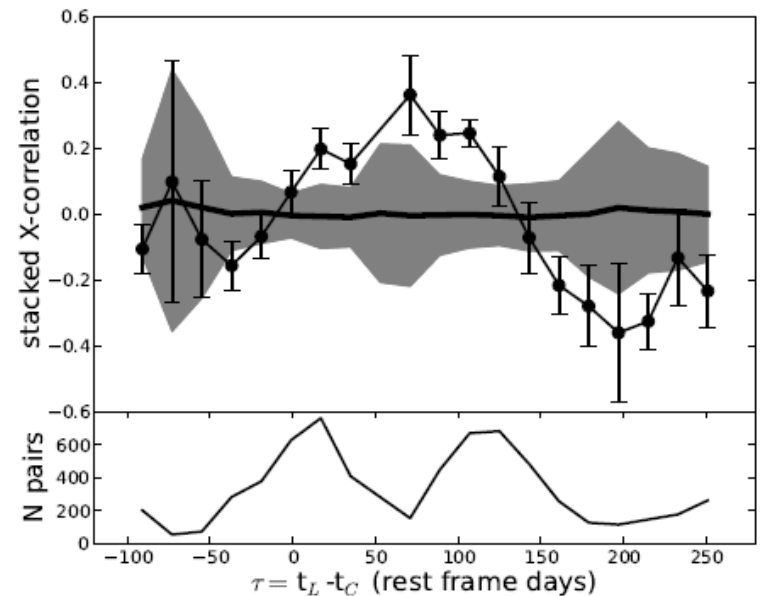
Barth+ 2011

Zw 229-015 (*Kepler* field)



“Stacked Spectra” or Extremely Sparse Sampling

- A minimal number of line measurements can be probabilistically matched to a particular lag with good continuum sampling.
 - Can be done with as few as two spectra, though fidelity low.



Fine+ 2013

Photometric Reverberation

- The Great Hope:
 - If we can get emission-line lags from ground-based broad-band data, we can get thousands of BLR radii and black hole masses efficiently.
 - With surveys like Pan-STARRS and LSST, we can get the monitoring data essentially for free.
 - *R-L* for cosmology for free!
 - Add one (high-quality) spectrum per target to get masses.

Photometric Reverberation

- The Great Challenge:
 - The line flux is typically a small part of the total waveband flux.
 - Line flux variations are relatively small.

$$\frac{\Delta F}{F} = \frac{EW_{\text{line}}}{FWHM_{\text{filter}}} \times F_{\text{var}}$$

Estimating these quantities for H β in Johnson *B*-band:

$$\frac{\Delta F}{F} \approx \left(\frac{60 \text{ \AA}}{940 \text{ \AA}} \right) \times (0.10 \pm 0.06) = 0.006 \pm 0.004$$

Typical photometric errors are $\sigma/F \sim 0.01$

Photometric Reverberation

- Approaches:

$$\frac{\Delta F}{F} = \frac{EW_{\text{line}}}{FWHM_{\text{filter}}} \times F_{\text{var}} \gg \frac{\sigma}{F}$$

Stronger line, e.g., H α

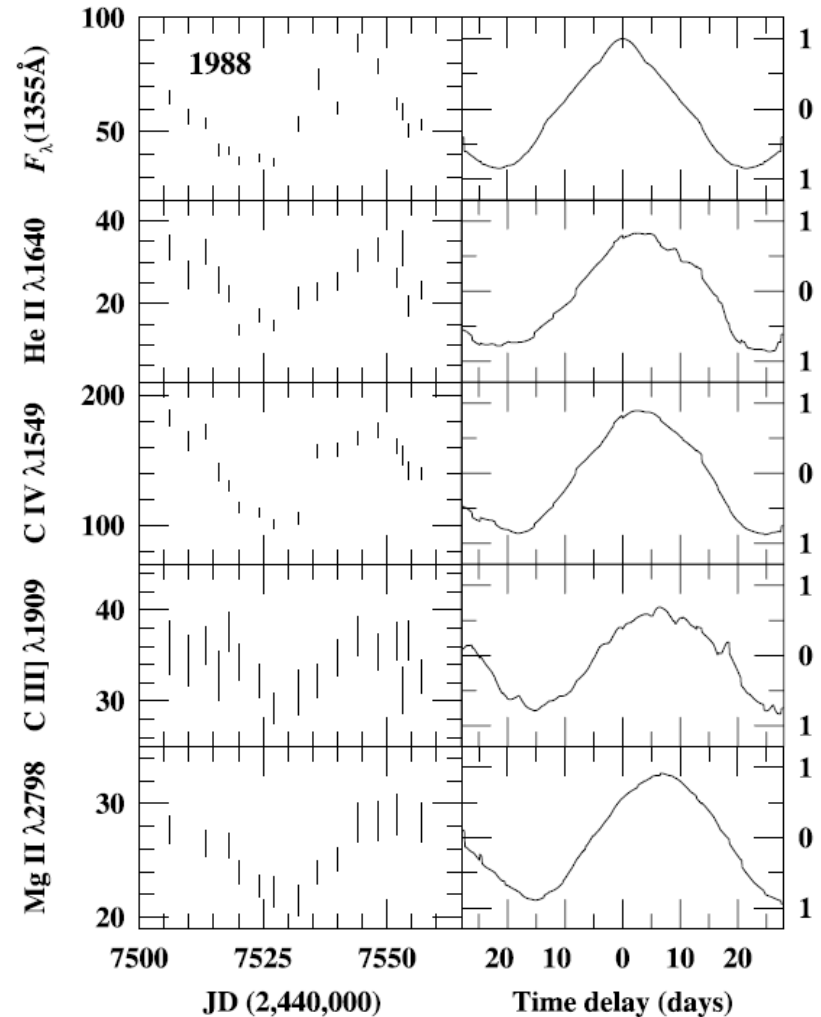
Narrower filter

Reduce photometric errors

Caution: As with spectroscopic reverberation, time sampling and duration remain important issues.

R-L Relationship for Mg II λ 2798

- Little reverberation data on Mg II λ 2798
 - Existing lag data ambiguous, particularly those that are contemporaneous with Balmer lines.
 - Relies on assumption that Mg II arises co-spatially with Balmer lines.



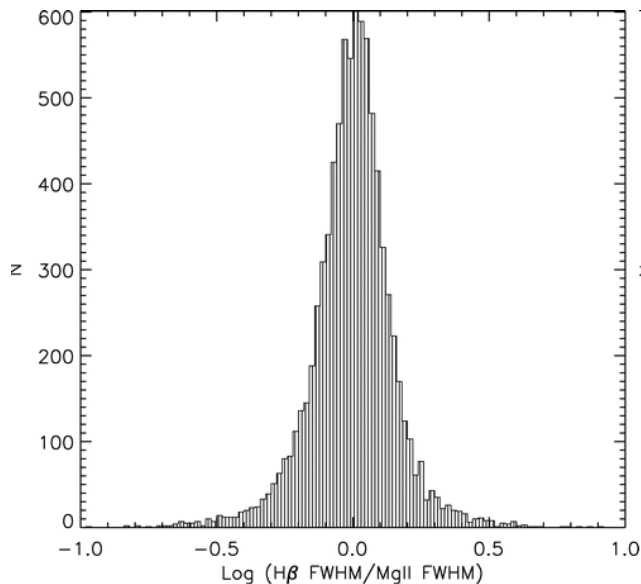
Metzroth, Onken, & Peterson (2006)

R-L Relationship for Mg II $\lambda 2798$

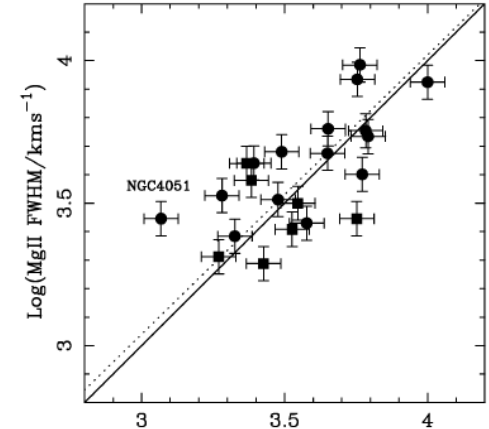
- From SDSS spectra, Shen et al. (2008) find

$$\log \left[\frac{\text{FWHM}(\text{H}\beta)}{\text{FWHM}(\text{Mg II})} \right] = 0.0062 \text{ dex}$$

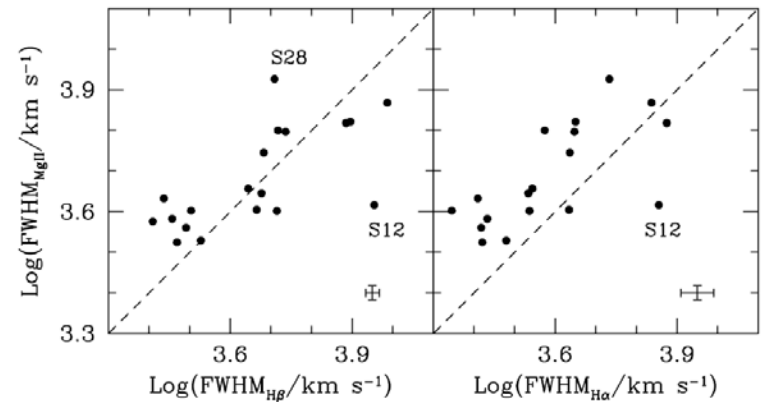
with scatter ~ 0.11 dex.



Shen et al. (2008)



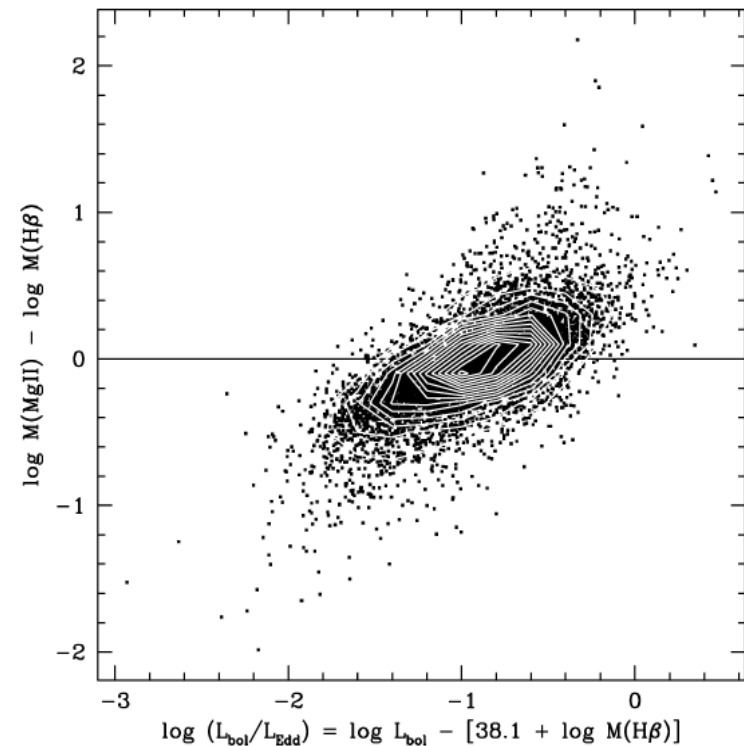
McLure & Jarvis (2002)



McGill et al. (2008)

R-L Relationship for Mg II $\lambda 2798$

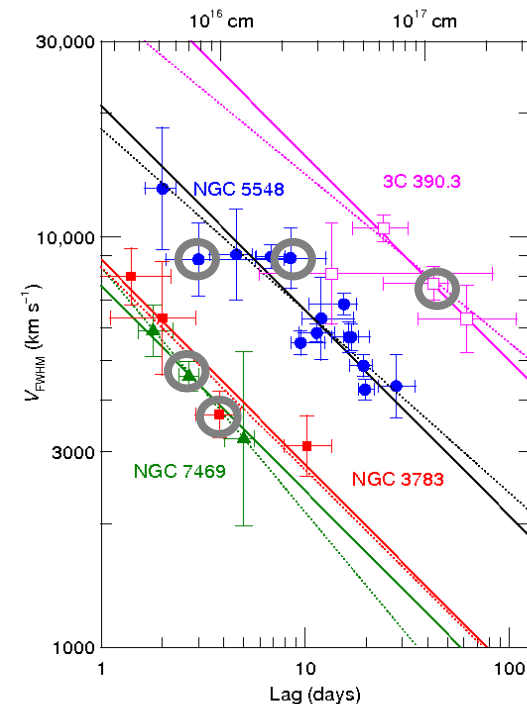
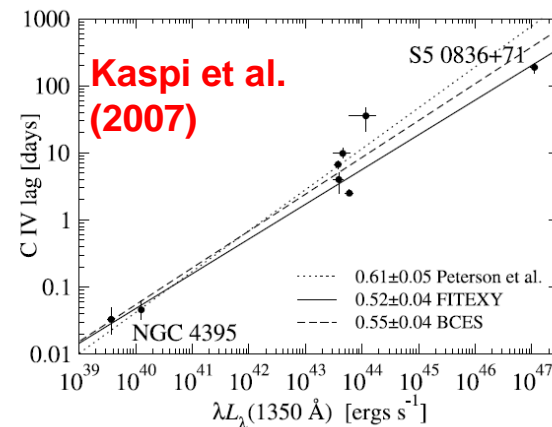
- Onken & Kollmeier find that the line width ratio has dependence on Eddington ratio and is correctable.



Onken & Kollmeier 2008

R - L Relationship for C IV $\lambda 1549$

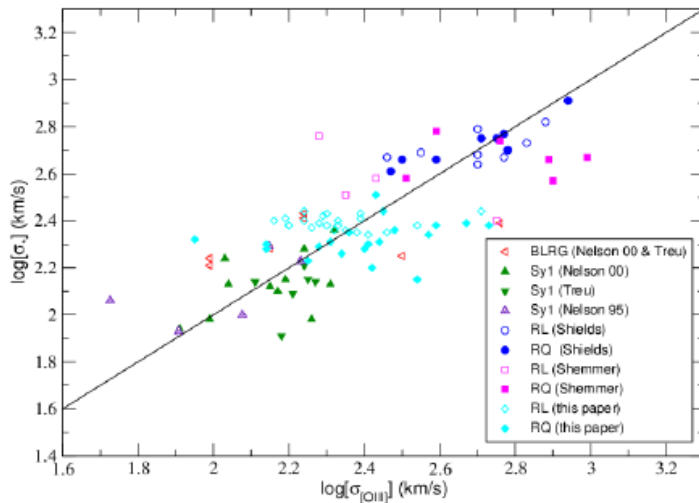
- First used by Vestergaard (2002) to estimate BH masses at high- z .
- Pros:
 - Limited data suggest same R - L slope as H β (despite Baldwin Effect).
 - Consistent with virial relationship, at least in low-luminosity AGNs.
- Cons:
 - Often strong absorption, usually in blue wing.
 - Extended bases (outflows), especially in NLS1s.



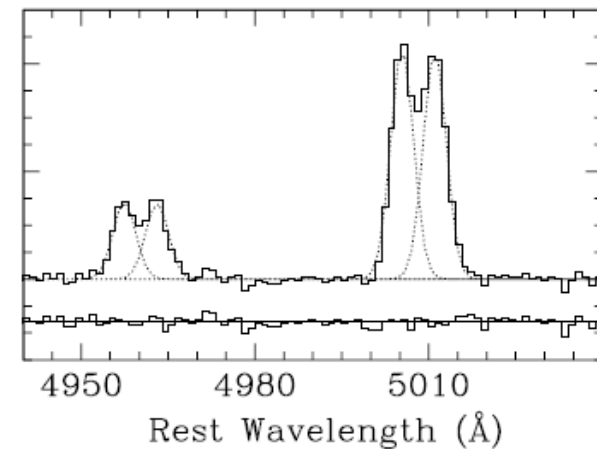
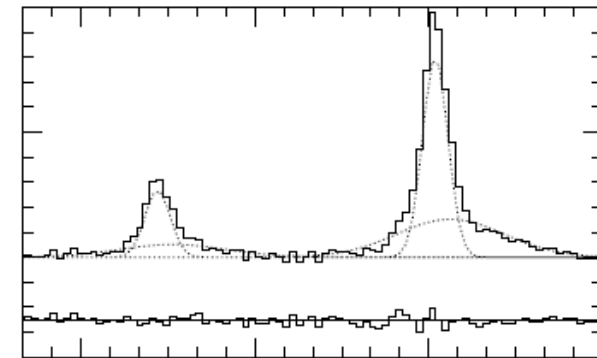
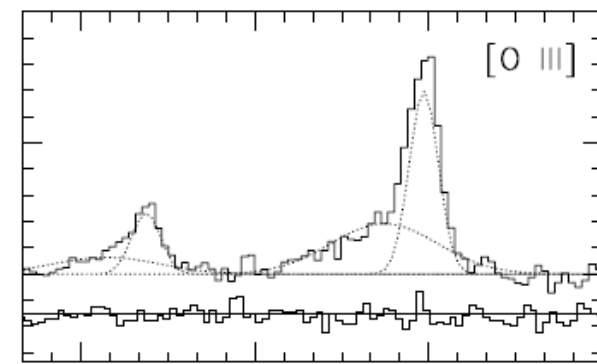
Other Scaling Relationships

- The width of the narrow [O III] $\lambda 5007$ line can be used as a surrogate for the stellar velocity dispersion.
- Intrinsic scatter: 0.10 – 0.15 dex.

Bonning et al. 2005, Gaskell 2009



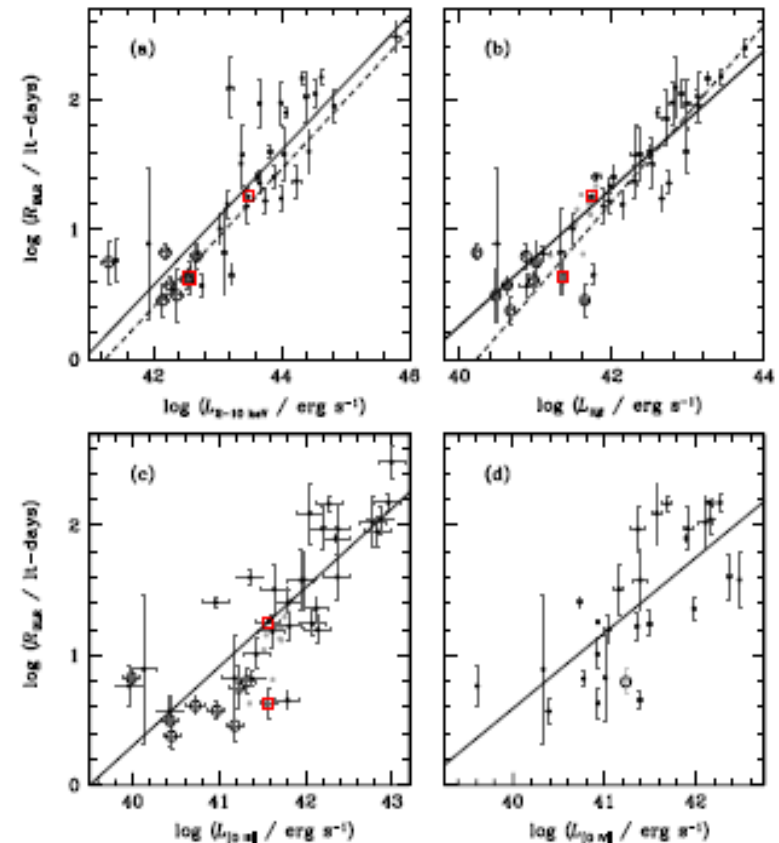
Bonning et al. 2005



Greene & Ho 2005

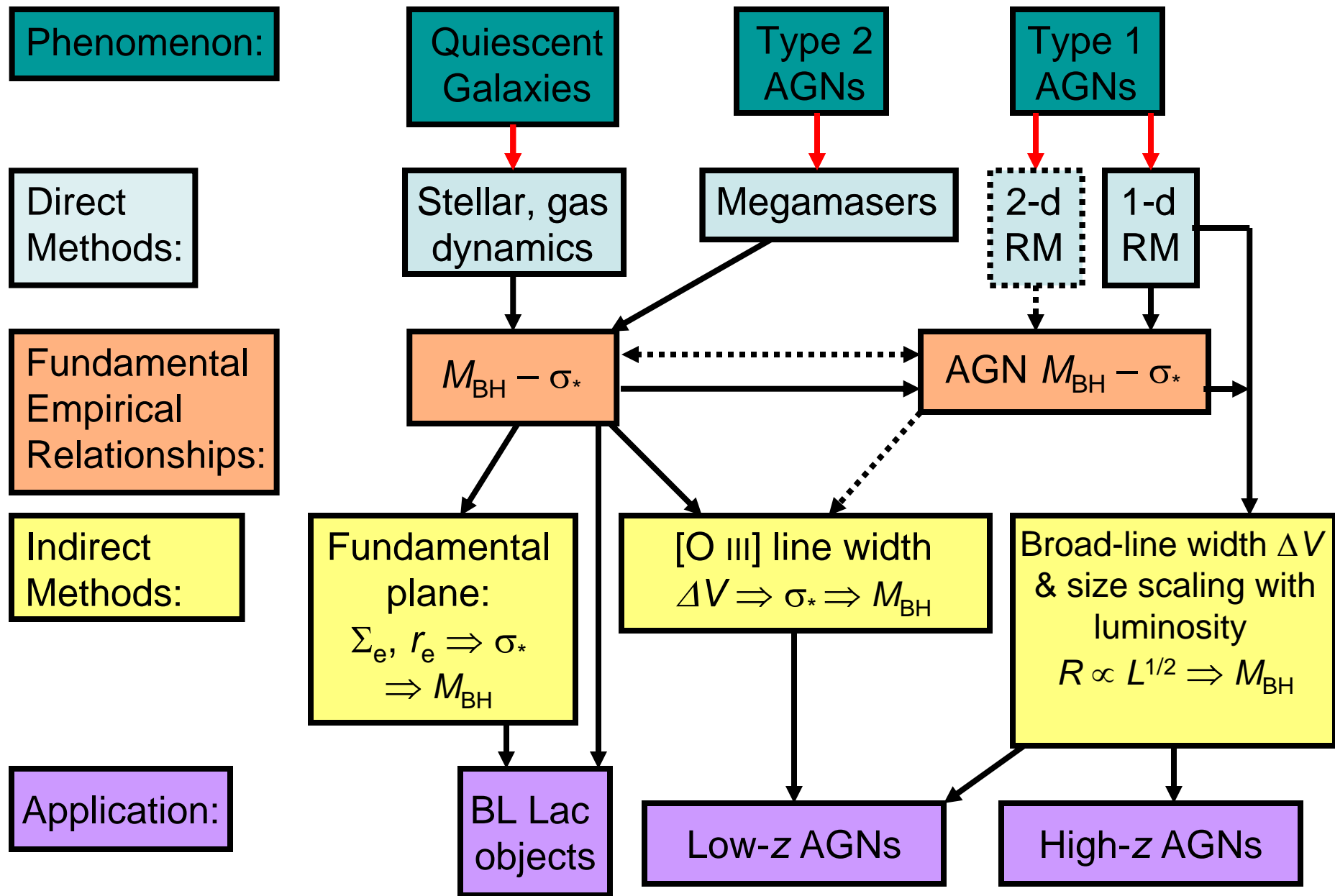
Other Scaling Relationships

- There are other luminosity indicators that can be used as proxies for R_{BLR} :
 - 2-10 keV flux. Scatter: 0.26 dex
 - Flux $\text{H}\beta$ broad component. Scatter: 0.22 dex.
 - Flux $[\text{O III}] \lambda 5007$. Scatter: 0.29 dex.
 - Flux $[\text{O IV}] \lambda 25.8\mu\text{m}$. Scatter: 0.35 dex.
- These are useful when uncontaminated continuum is difficult or impossible to measure.



Greene et al. 2010

Measurement of Central Black Hole Masses: The Mass Ladder



Scaling Relationships: Use with Caution

- When you think you're measuring mass, you're really measuring

$$M_{\text{BH}} \propto R(\Delta V^2) \propto L^{1/2}(\Delta V^2)$$

- When you think you're measuring Eddington ratio, you're really measuring

$$L/L_{\text{Edd}} \propto L/M_{\text{BH}} \propto L/L^{1/2}(\Delta V^2) \propto L^{1/2}/\Delta V^2$$

Summary of Key Points

- Direct methods of mass measurement:
 - Most dynamical methods are limited by angular resolution to nearest tens of Mpc.
 - Reverberation mapping is effective even at large distances, but currently limited by systematics and dependence on other methods for calibration.
- Indirect methods:
 - Can be used for large samples, but less reliable for individual sources.