

# **Plasmonics in random media**

**Cid B. de Araújo**

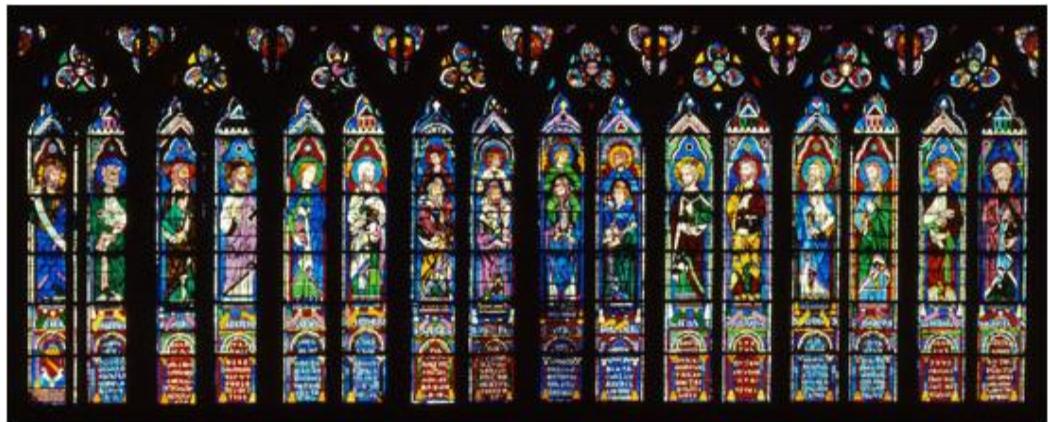
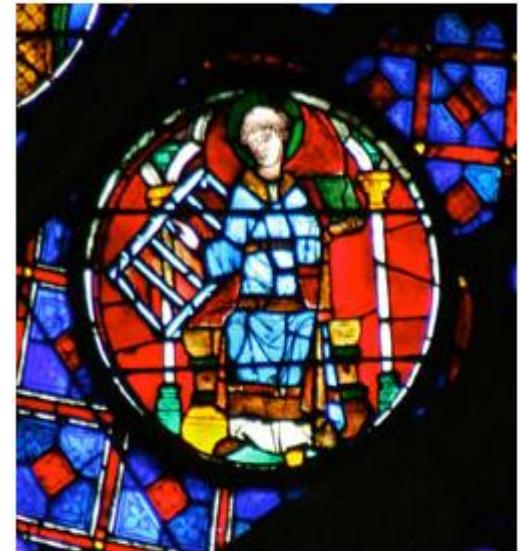
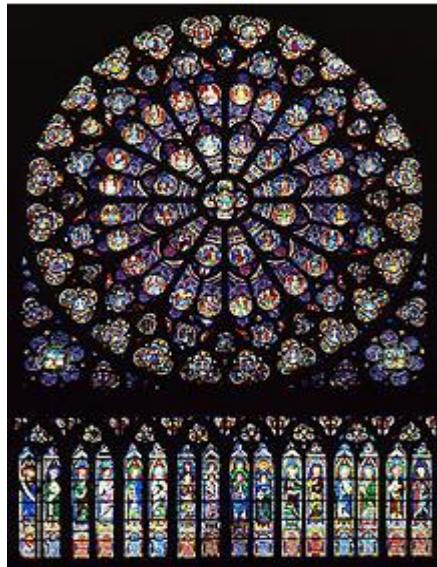
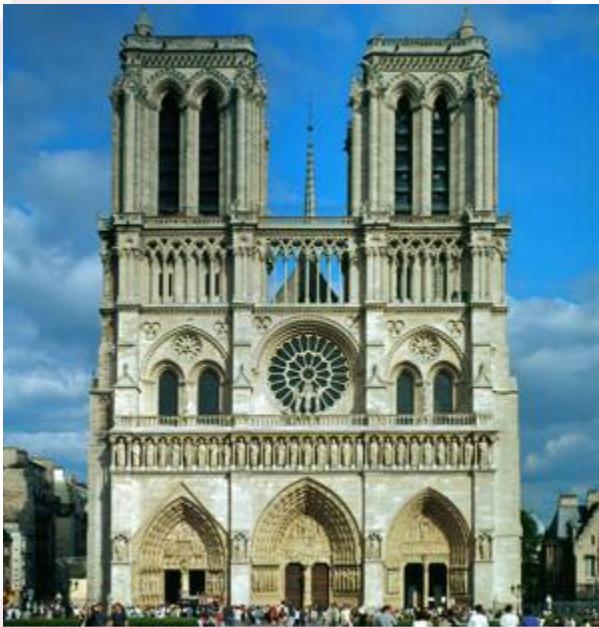
Departamento de Física  
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Recife  
Brazil

# Plasmonics



“Science and technology that deals with the generation, control, manipulation, and transmission of plasmon excitation in metal nanostructures”

# *Surface plasmons in nanoparticles*



Notre Dame de Paris

Cu, Ag, Au

# Michael Faraday's Recognition of Ruby Gold: the Birth of Modern Nanotechnology

His 1857 Lecture to the Royal Society in London

**David Thompson**

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From the paper in *Philosophical Transactions* entitled 'Experimental relations of gold (and other metals) to light' (1), based on his Bakerian lecture to the Royal Society in London on 5 February 1857, it is clear that Michael Faraday was fascinated by the ruby colour of colloidal gold. The objective of his investigations was to examine the interaction of light with metal particles, but much of this paper focused on various

**Figure 1**

*Faraday's colloidal ruby gold. Reproduced by Courtesy of the Royal Institution of Great Britain*



solution such as phosphorus in carbon disulfide in a two phase system. The yellow colour of sodium chloroaurate ( $\text{NaAuCl}_4$ ) changes within minutes to the deep ruby colour of colloidal gold. Faraday concluded that the ruby fluid was gold dispersed in the liquid in a very finely divided metallic form not visible in any of the microscopes available in his day. Nearly 100 years later Turkevich et al (2, 4) used electron microscopic

# Gold-Doped Glass: A Maxwell-Garnett Composite

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Developmental Glass, Corning Inc.



Red Glass Caraffe  
Nurenberg, ca. 1700

Huelsmann Museum, Bielefeld

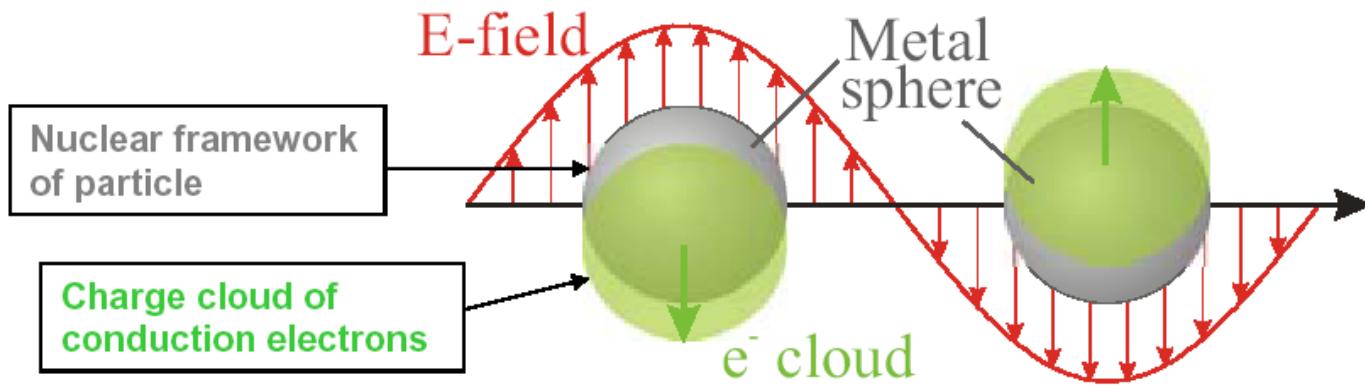


gold volume fraction approximately  $10^{-6}$   
gold particles approximately 10 nm diameter

- Composite materials can possess properties very different from those of their constituents.
- Red color is because the material absorbs very strong in the blue, at the surface plasmon frequency

# Surface Plasmon Resonance

collective excitation of the conduction electrons



Plasmon excitation influences the absorption and scattering of light from the surfaces of metals.

# Surface plasmon frequency (depend on shape, size and material)

$$E_{in} = \frac{3\epsilon_0}{\epsilon_{in} + 2\epsilon_0} E_0$$

← applied electric field  
nanosphere

$$\epsilon_{in} = 1 - \frac{\omega_p^2}{\omega^2}$$

Drude dielectric function

SP frequency is therefore:

$$\omega = \frac{\omega_p}{\sqrt{1 + 2\epsilon_0}}$$

(This assumes particle is small compared to wavelength.)

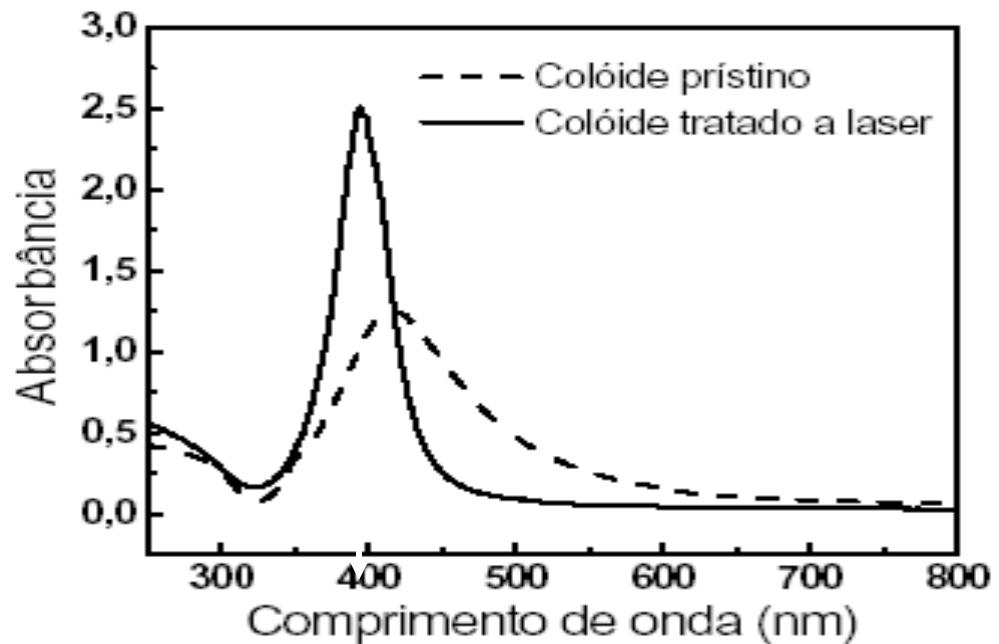
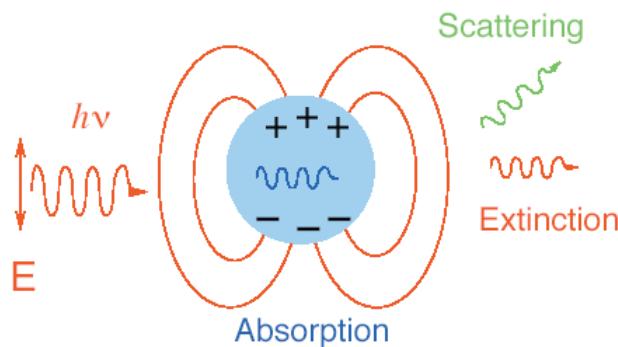
# Extinction coefficient

$$C_{ext} = 9 \frac{\omega}{c} \varepsilon_m^{3/2} V \frac{\varepsilon_2}{[\varepsilon_1 + 2\varepsilon_m]^2 + \varepsilon_2^2}$$

nanospheres

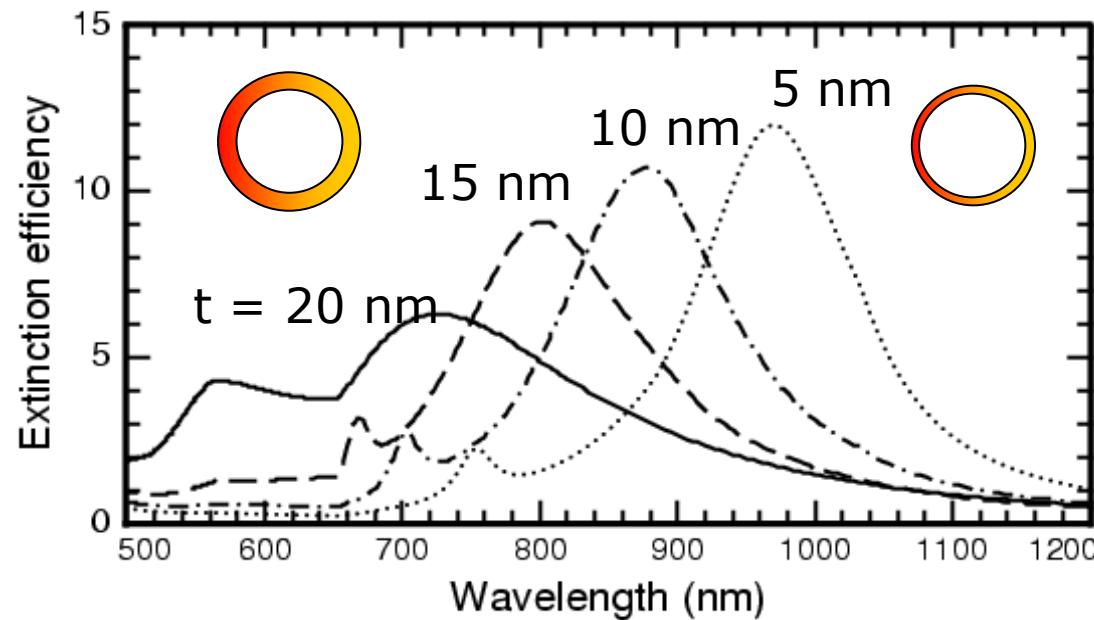
Mie theory 1908 (dipole approximation)

Silver in  
aqueous colloid



# Metal nanoshell colloids

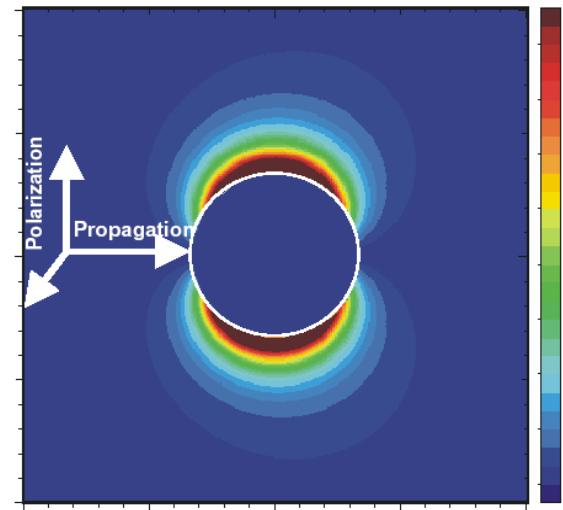
Plasmon resonance tunable by core and shell dimensions



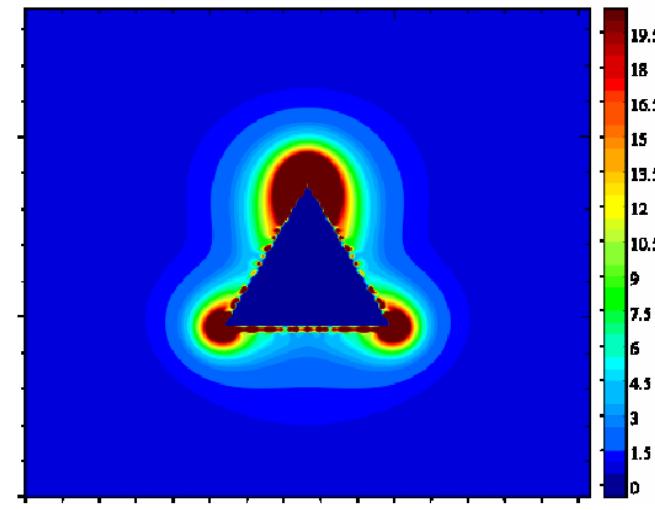
# Near-field intensity

## Shape Dependence

Calculated Electric Field:  
20 nm diameter Ag Sphere in vacuum



Calculated Electric Field:  
100 nm Ag Triangle in vacuum

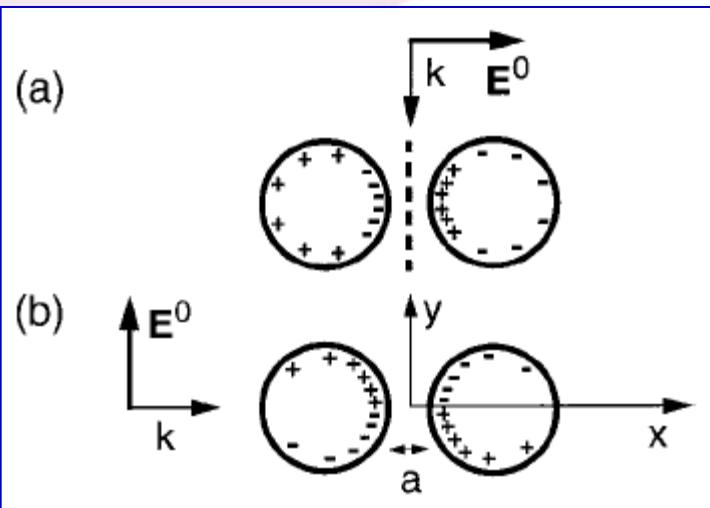


Schatz et al.

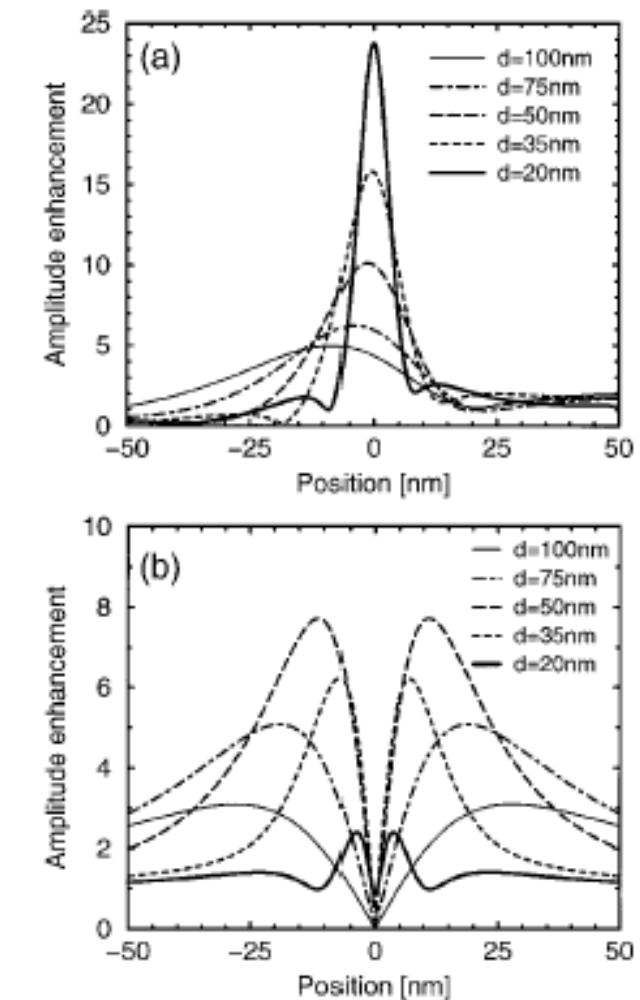
Spatial extension: 10-50 nm

# Coupled nanoparticles

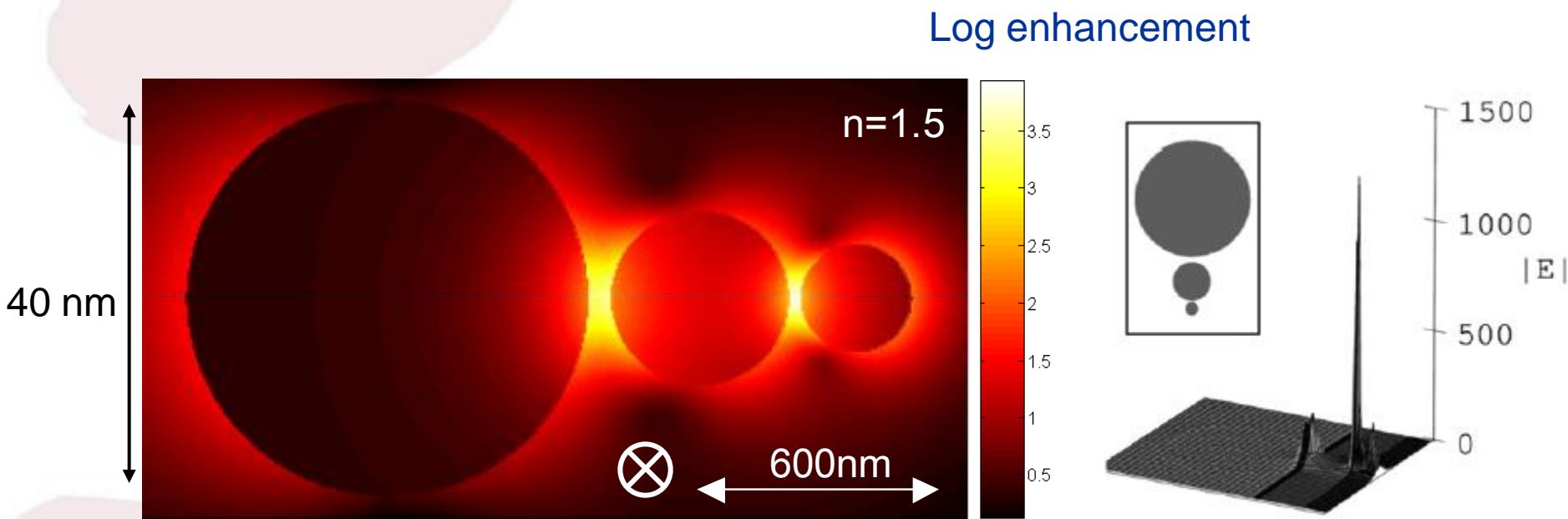
Kottmann, Martin Opt. Lett 2001



Field increases by 24 for particles with diameter of 20 nm.  
Intensity enhancement > 500



# More complex nano-structures



Plasmonic nanolens:

First proposed by Li, Stockman &  
Bergman, PRL (2003)

Bidaut, JACS 2008

# Metal-dielectric nanocomposites

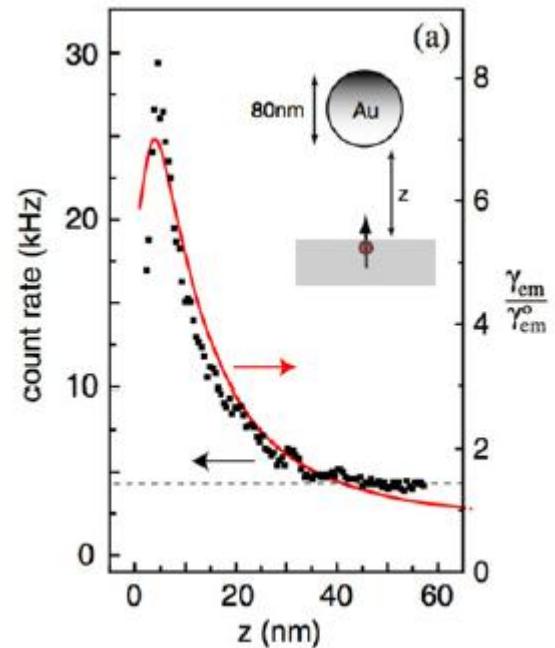
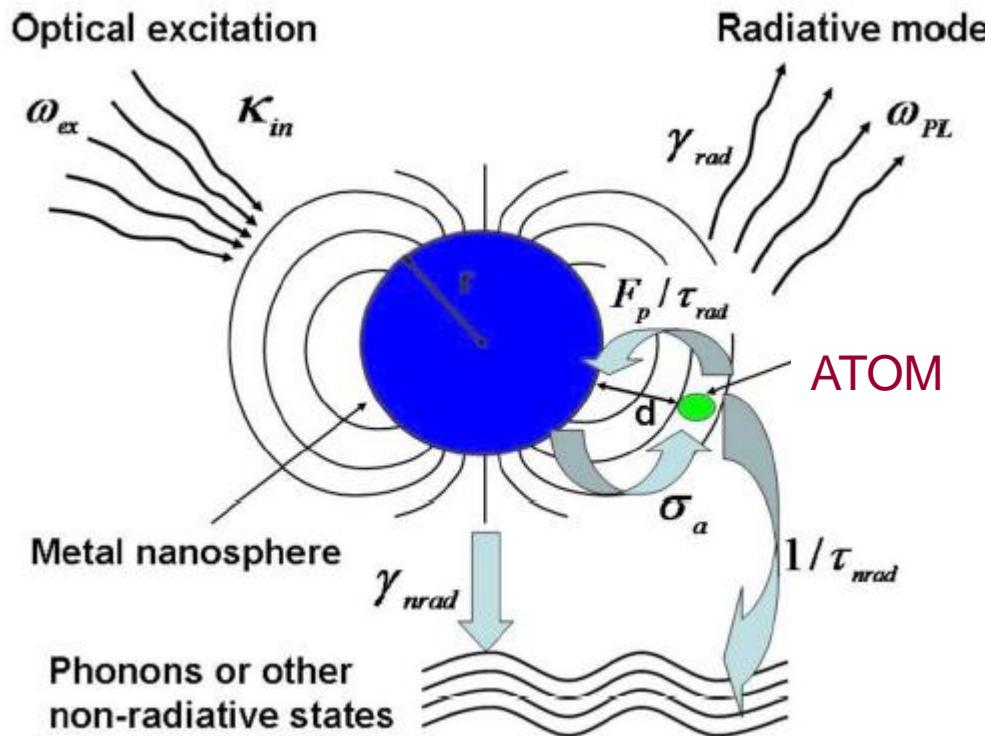
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- Plasmon enhanced fluorescence
- Third-order nonlinear optics in plasmonic materials
- Random lasers

Surface plasmon resonances may increase NL response

Scale size of inhomogeneities  $\ll$  optical wavelength  
Optical susceptibility can be described by volume averaged quantities

# Plasmon enhanced luminescence

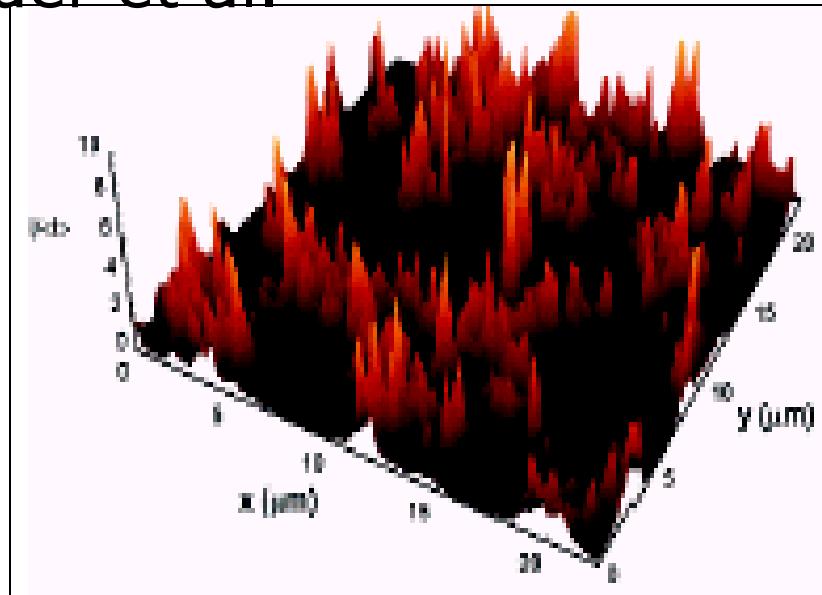
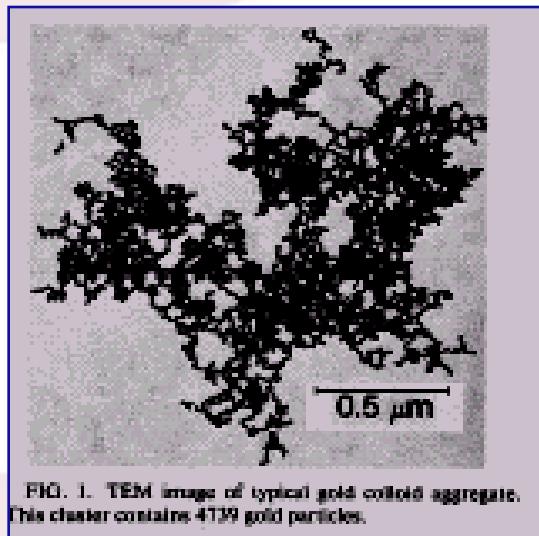


Novotny et al. PRL 2006

$$\sigma_{PL}(\omega_{ex}, \omega_{PL}) = \sigma_{abs}(\omega_{ex})\eta_{rad}(\omega_{PL})$$

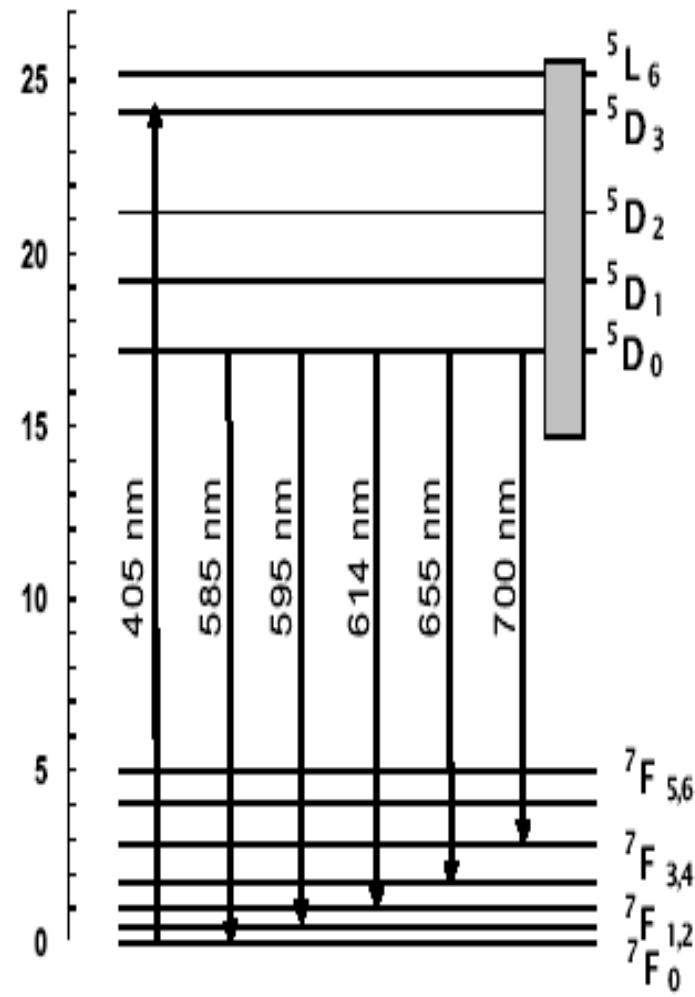
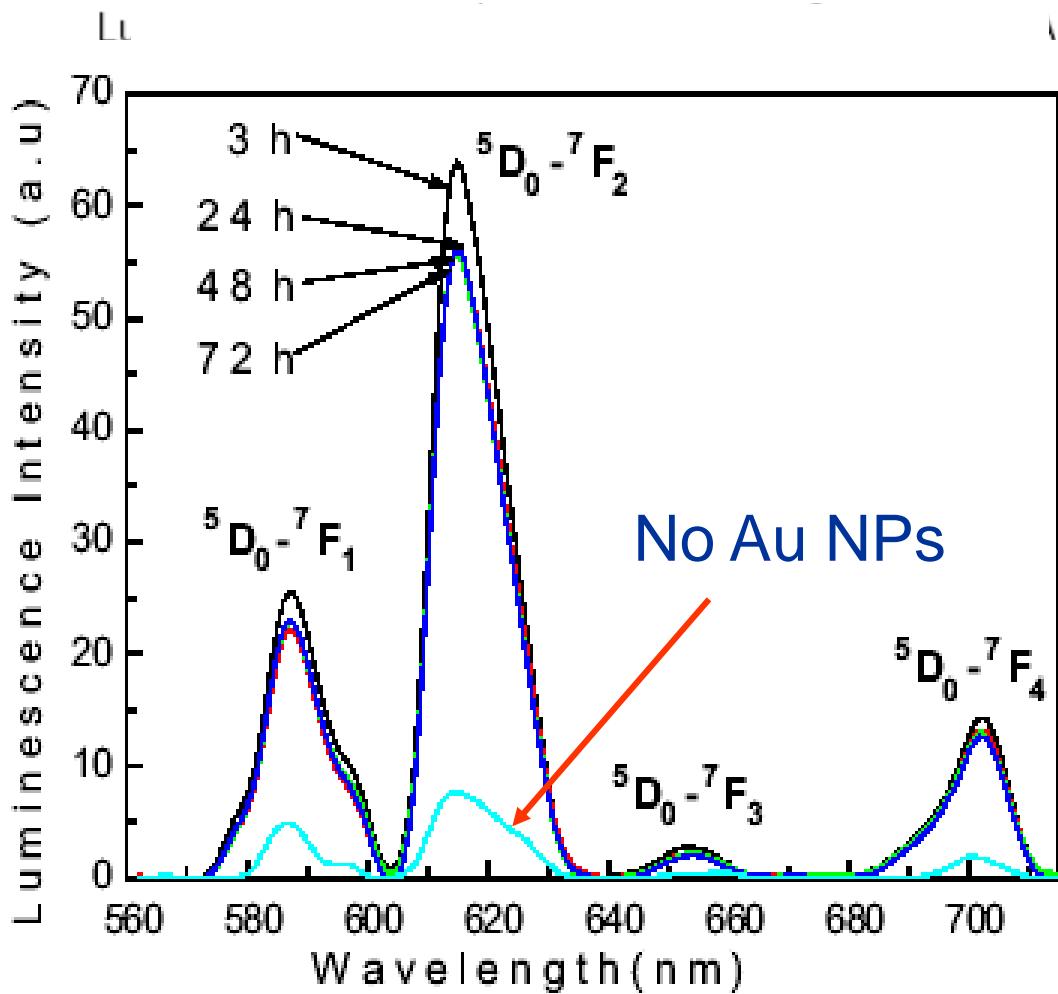
# Fractals structures and hot spots

Shalaev et al.  
Marder et al.

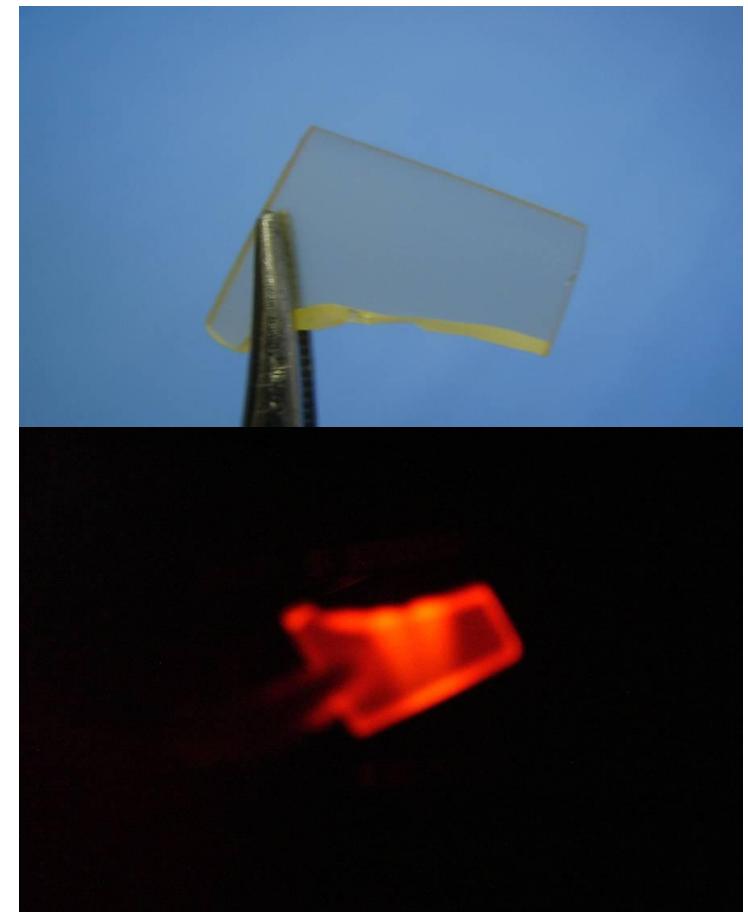


**Optical glasses doped with trivalent rare earth ions containing silver or gold NPs**

# Photoluminescence enhancement by gold nanoparticles in $\text{Eu}^{3+}$ doped $\text{GeO}_2\text{-}\text{Bi}_2\text{O}_3$ glasses

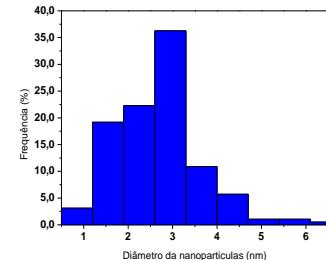
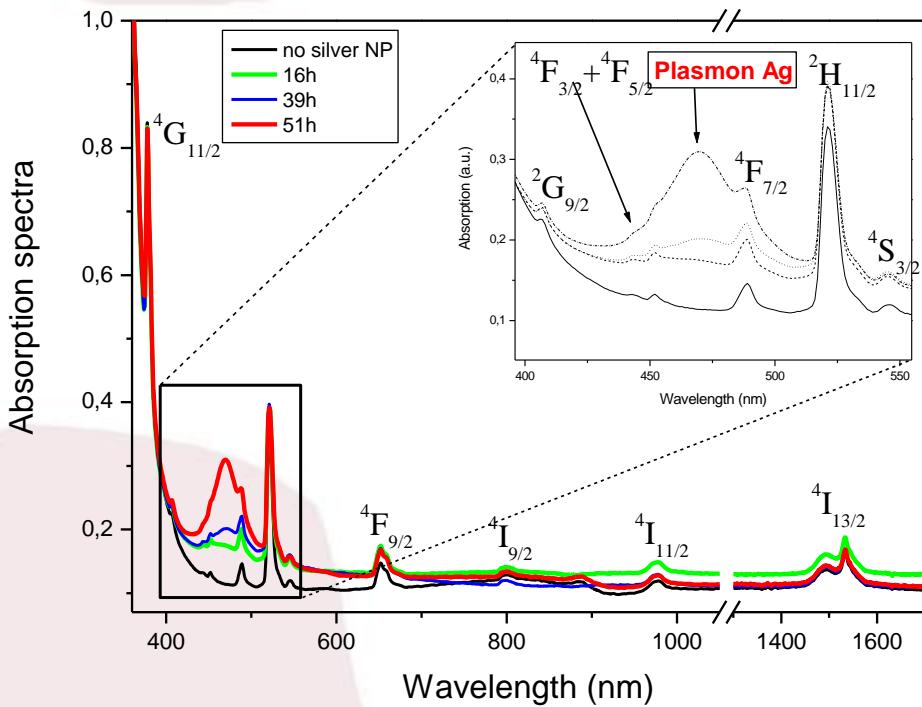


Enhanced luminescence  
at 614 nm  
(excitation at 405 nm)

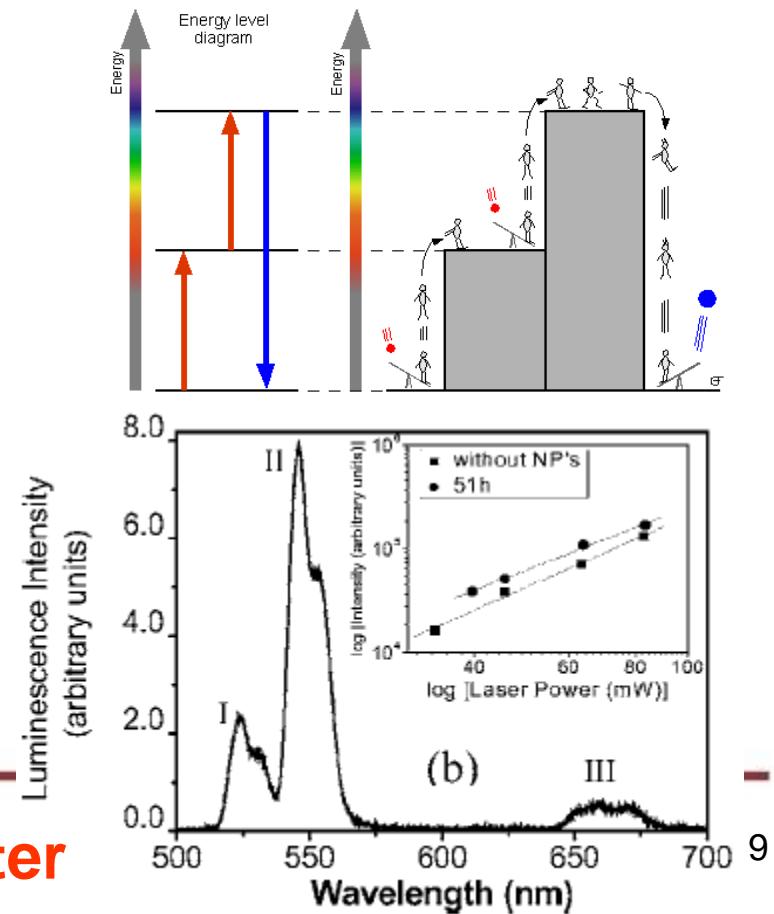
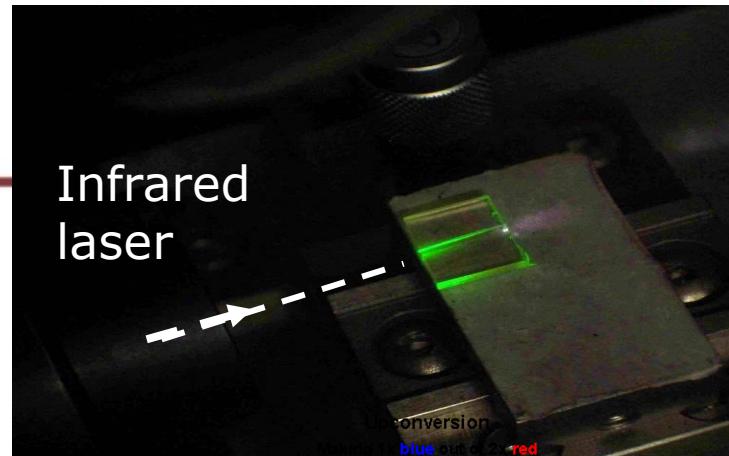
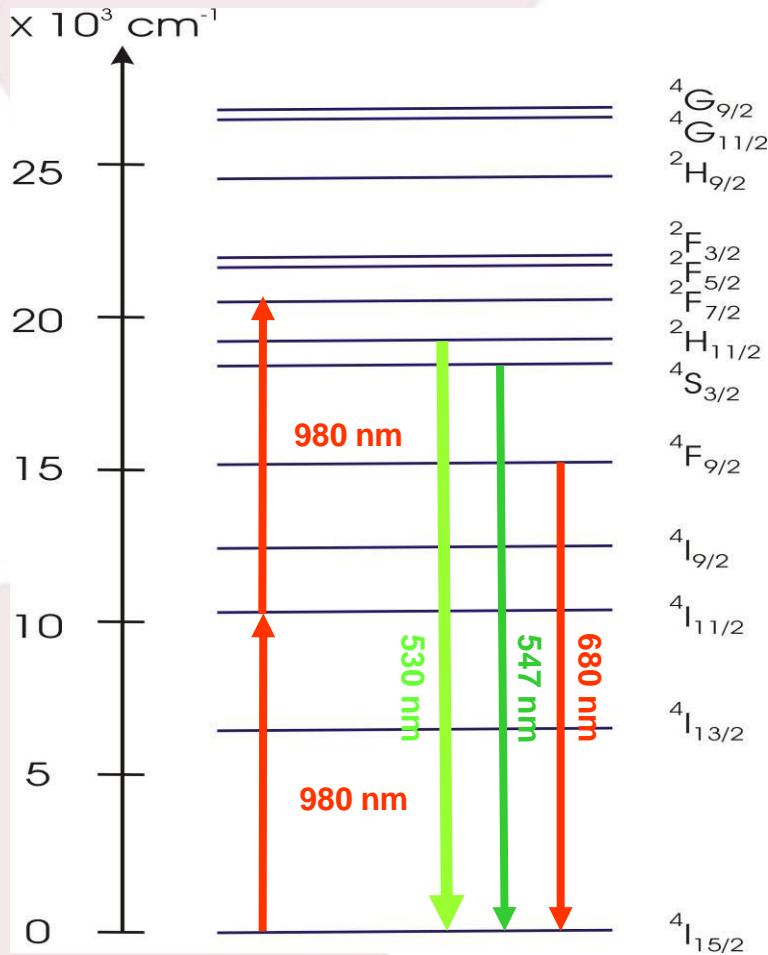


# Frequency upconversion in $\text{Er}^{3+}$ doped $\text{PbO-GeO}_2$ glasses containing silver nanoparticles

59 PbO – 41 GeO<sub>2</sub>



# 100% enhancement



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Tellurium glass with silver NPs doped with  $\text{Pr}^{3+}$  or  $(\text{Tb}^{3+}-\text{Eu}^{3+})$  or  $\text{Tb}^{3+}$ :

- J. Appl. Phys. 105, 103505 (2009).
- J. Appl. Phys. 104, 093531 (2008).
- J. Appl. Phys. 103, 093526 (2008).

Gemanate glass doped with  $\text{Eu}^{3+}$  or  $(\text{Yb}^{3+}-\text{Er}^{3+})$  containing silver, gold or copper NPs:

- Appl. Phys. Lett. 94, 101912 (2009).
- Appl. Phys. B 94, 239 (2009).
- Appl. Phys. Lett. 92, 141916 (2008).

# Nonlinear Optics

Interaction light-matter under circumstances that  
the linear superposition principle is violated

**Optical polarization = Dipole moment per unit volume**

$$P = \epsilon_0 [\chi^{(1)} E + \chi^{(2)} E^2 + \chi^{(3)} E^3 + \dots]$$

$\chi^{(n)} \equiv 0$  ,  $n = \text{even}$  (*centro-symmetric media*)

$P$  induces changes in the speed of light in the medium  
and new frequencies may be generated

# Nonlinear Optics hold great promise for applications such as:

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- All-Optical Switching
- Optical Limiting
- Optical Sensors
- Lasers and Amplifiers

but the lack of appropriate materials do not allow the implementation of many ideas already presented

# Z-scan technique

## Nonlinear refraction

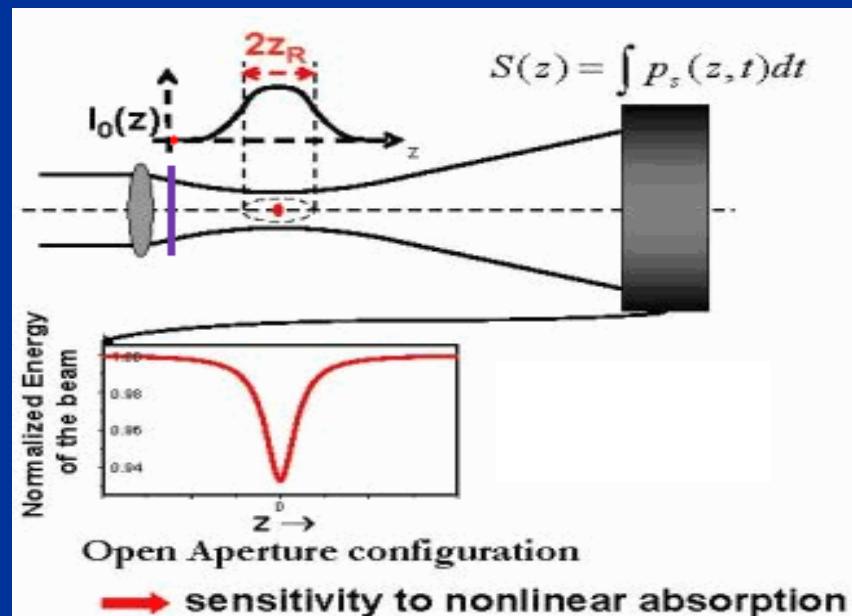
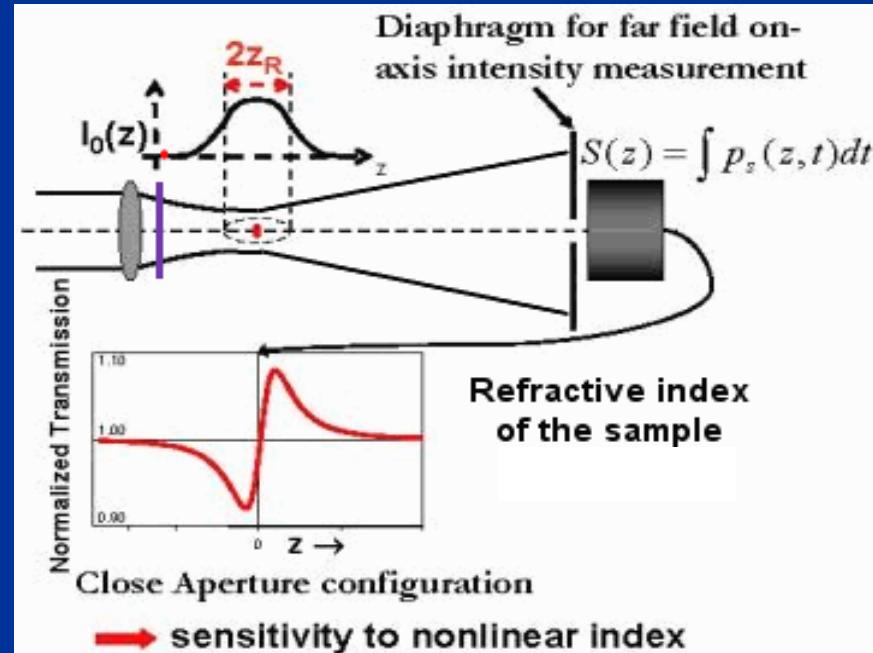
$$n = n_0 + n_2 I(r)$$

- $n_2 > 0$  self focusing  
 $n_2 < 0$  self defocusing  
 $\Delta T \propto n_2 I$

## Nonlinear absorption

$$\alpha = \alpha_0 + \alpha_2 I(r)$$

$\Delta T \propto \alpha_2 I$

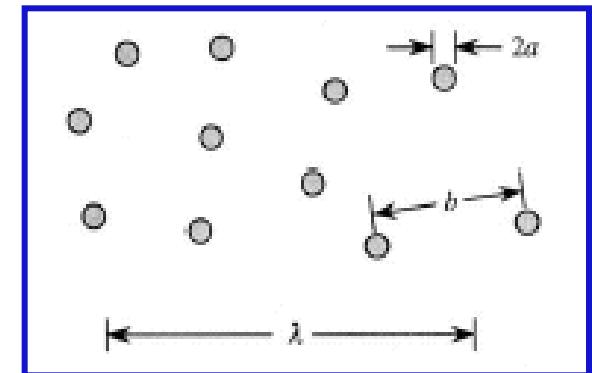


# Colloids containing metallic nanoparticles

## Local field enhancement

$$\chi_{eff}^{(3)} = f \eta^2 |\eta|^2 \chi_{NP}^{(3)} + \chi_{host}^{(3)}$$

→  
Filling fraction

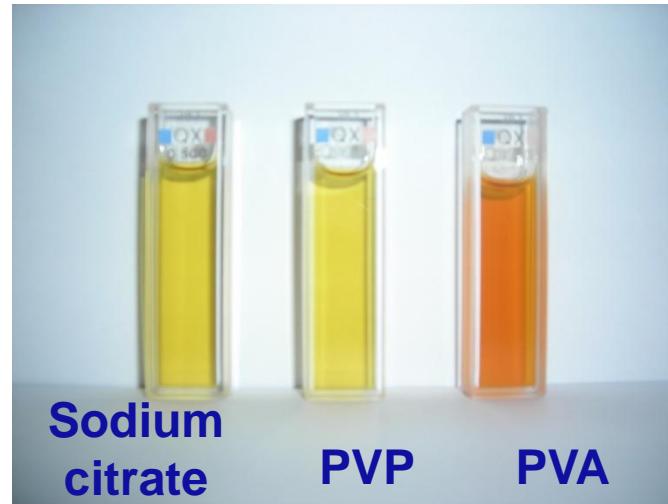
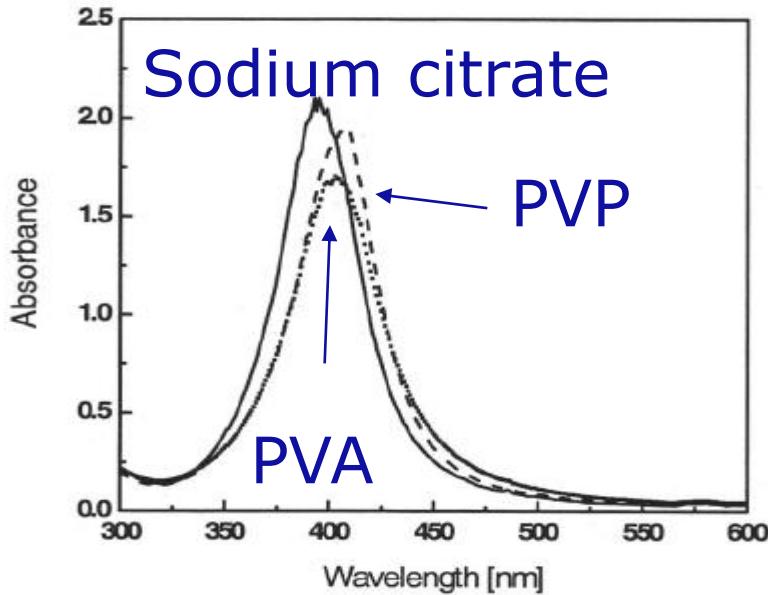


$$\eta = \frac{3\epsilon_{NP}(\omega)}{[\epsilon_{NP}(\omega) + 2\epsilon_h(\omega)]}$$

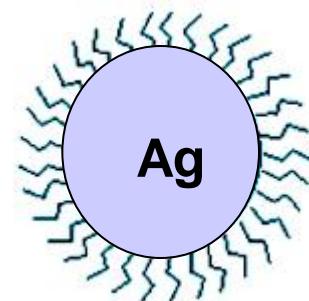
## Surface plasmon resonance

$$\text{Re} [\epsilon_{NP}(\omega_{sp}) + 2\epsilon_h(\omega_{sp})] = 0$$

# Third order susceptibility of silver colloids



Z - scan  
532 nm  
80 ps  
5 Hz



Influence of stabilizing agents and dipole moment of solvents

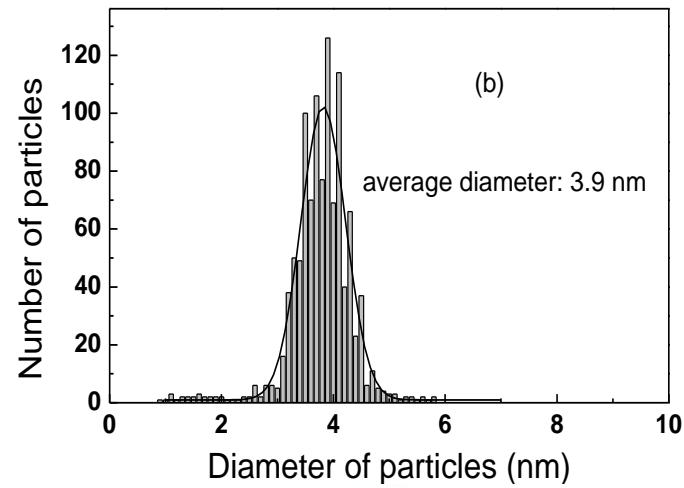
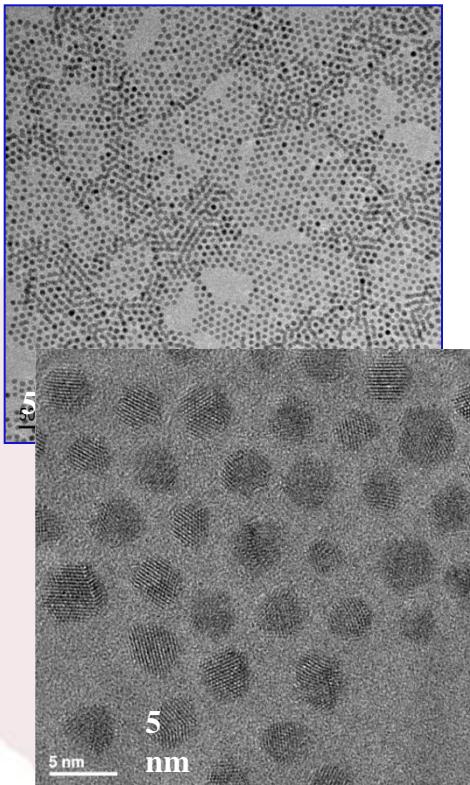
Susceptibility changes by more than 100% for PVA and PVP

J.O.S.A. B 24, 2136 (2007)

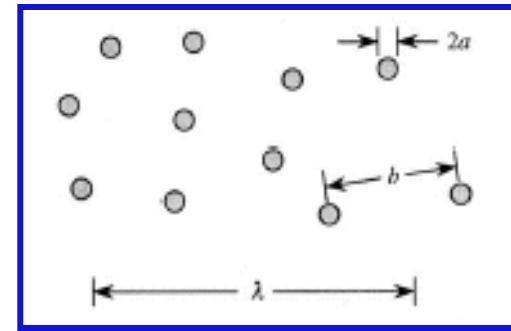
Applied Physics B 92, 61 (2008)

# NL susceptibility of silver nanoparticles in $\text{CS}_2$

Competing processes between nonlinearities of the constituents



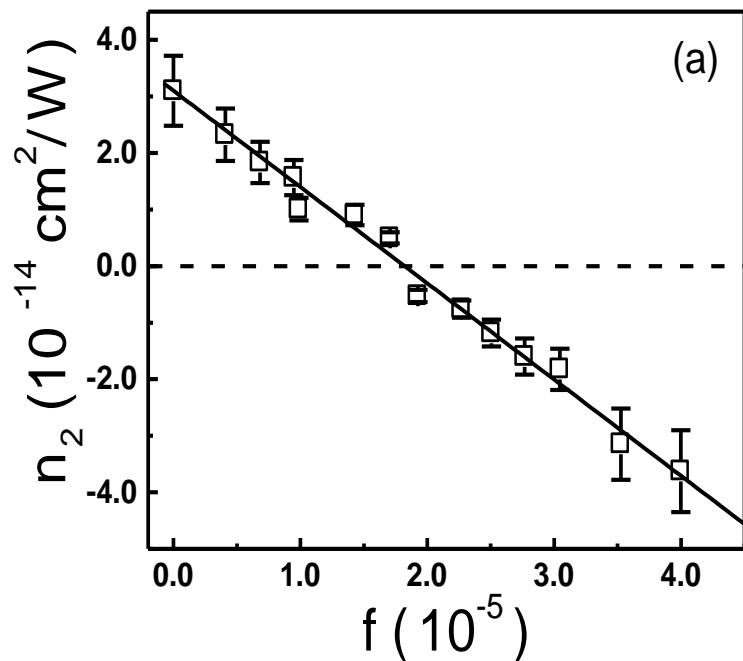
Silver NPs capped with dodecanethiol



$$\beta = \frac{\varepsilon_i - \varepsilon_h}{\varepsilon_i + 2\varepsilon_h}$$

$$\varepsilon_{eff} = \varepsilon_h \cdot \left[ 1 + \frac{3\beta f}{1 - \beta f} \right]$$

## NL Maxwell Garnet model



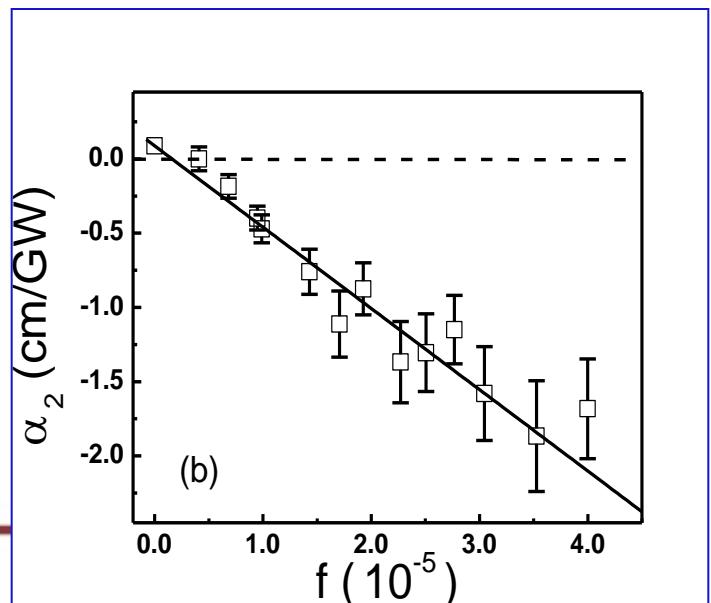
$$\chi_{eff}^{(3)} \approx \chi_h^{(3)} + f(a + i b) \chi_{NP}^{(3)}$$

$$\chi_{NP}^{(3)} = (-6.3 + i 1.9) \times 10^{-16} \text{ m}^2/\text{V}^2$$

$$\chi_h^{(3)} = 2.9 \times 10^{-20} + i 3.5 \times 10^{-22}$$

*m<sup>2</sup>/V<sup>2</sup>*

Control of spatial and  
temporal profile of optical beams  
(Space and temporal solitons)

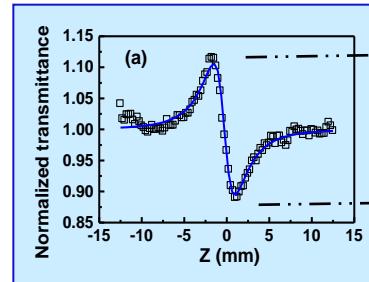


# First observation of high-order nonlinearities in Ag aqueous colloids

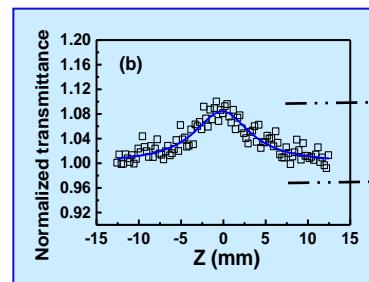
Z-scan 80 ps @ 532 nm (single pulses 5 Hz)

NL refractive behavior

Nonlinear absorption



$$\Delta T \propto n_2 I$$

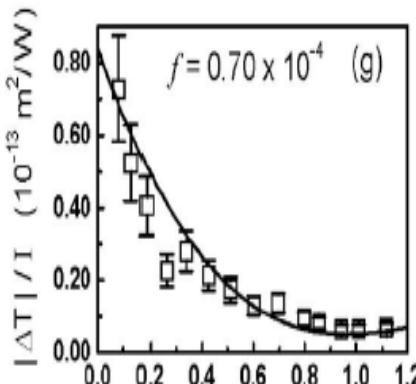
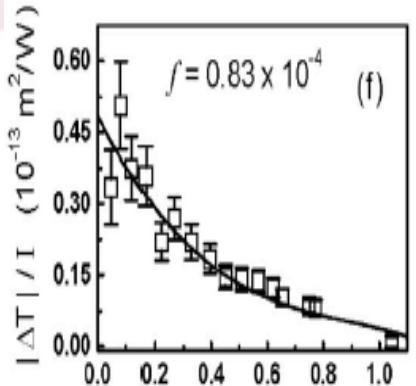
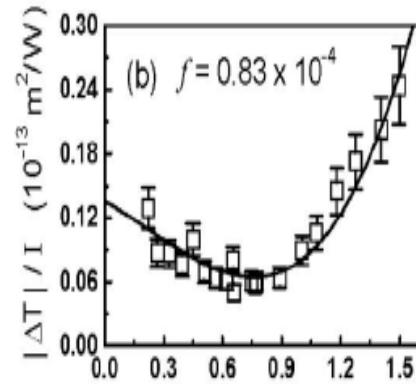
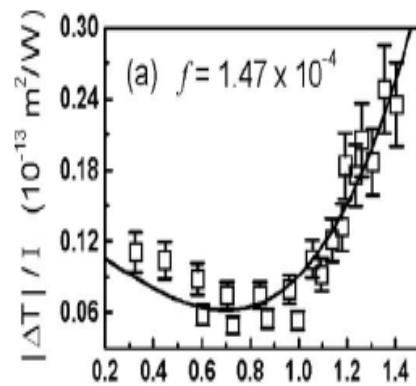


$$\Delta T \propto \alpha_2 I$$

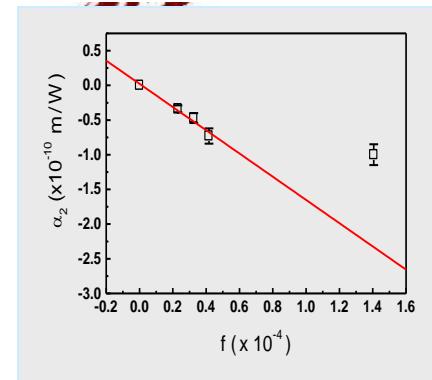
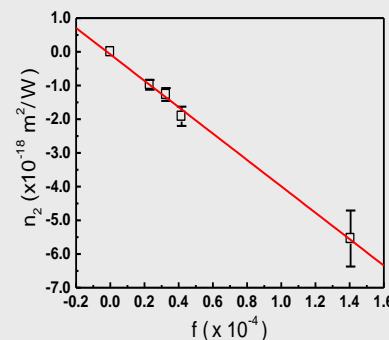
3rd  
order  
 $\Delta T \propto I$

## NL refraction

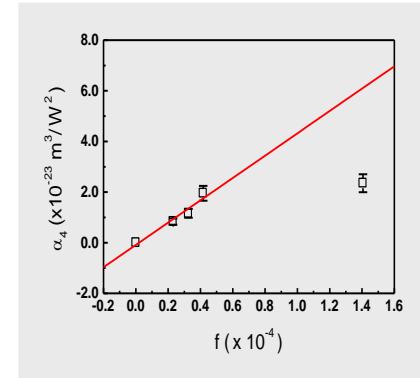
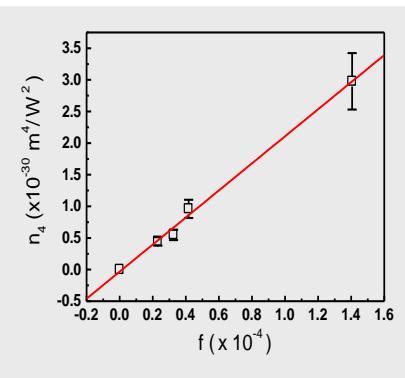
## NL absorption



3rd. order nonlinearity



5th. order nonlinearity

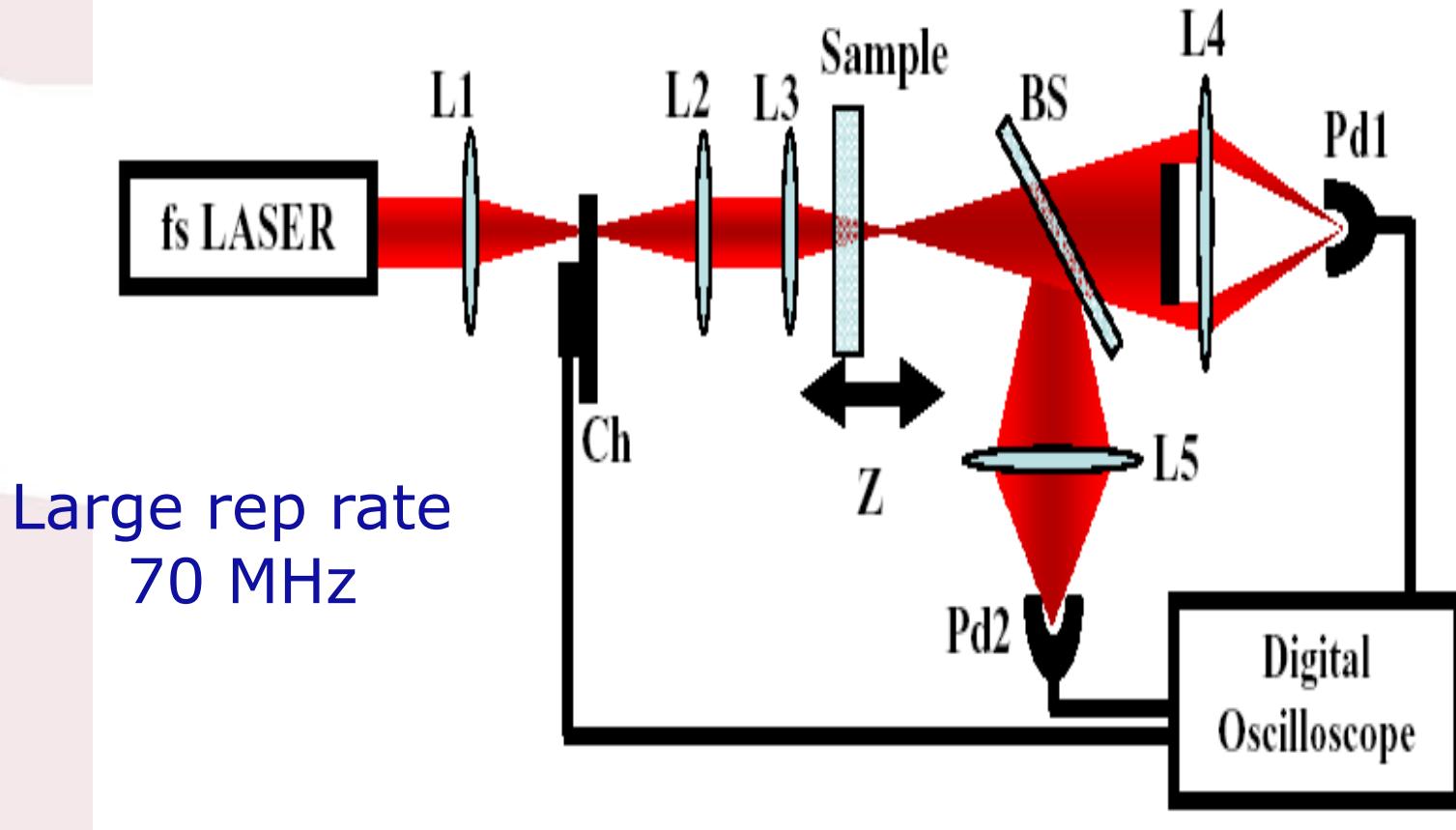


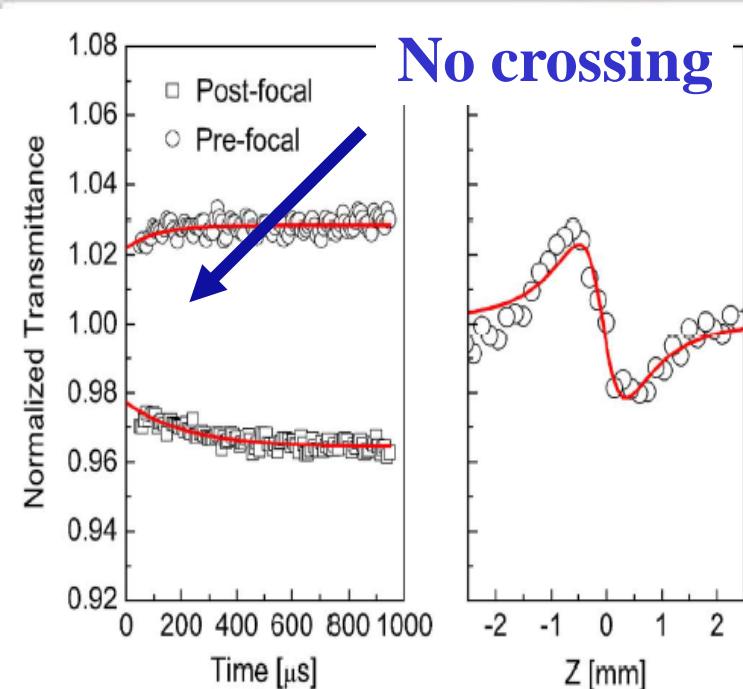
High order nonlinearities  
also depend linearly with  $f$

[Up to  $\chi^{(9)}$ ]



# Thermally managed eclipse Z-scan





No crossing

# PbO-GeO<sub>2</sub> film with copper NPs

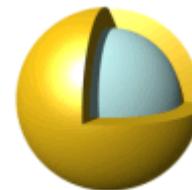
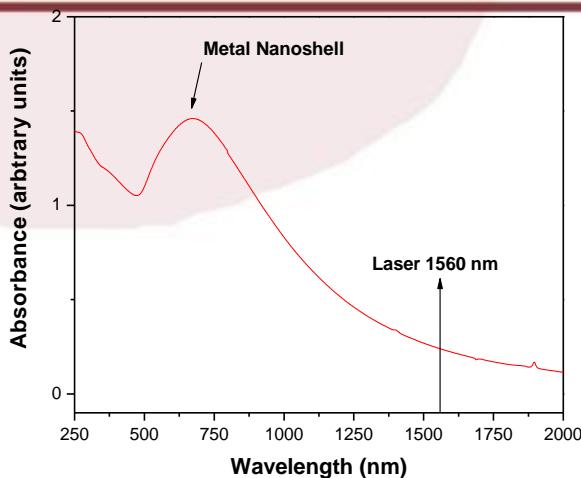
## Influence of the Surface Plasmon Resonance

Laser pulses  
150 fs

Material	$\lambda$ (nm)	Pulse duration	$n_2$ (cm <sup>2</sup> /W)	$\alpha_2$ (cm/GW)	$n_2/\lambda\alpha_2$	Ref.
PGO film	1064	15 ps	$6 \times 10^{-12}$	200	$2.8 \times 10^{-1}$	9
PGO film	532	15 ps	$6 \times 10^{-12}$	1200	$9.4 \times 10^{-2}$	9
PGO film	800	150 fs	$(2 \pm 1) \times 10^{-13}$	$(3 \pm 1) \times 10^{-3}$	$8.3 \times 10^{-4}$	10
PGO film with Cu and Cu <sub>2</sub> O nanoparticles	800	150 fs	$6.3 \times 10^{-12}$	<660	$>1.2 \times 10^{-1}$	This work
Bi <sub>2</sub> Nd <sub>2</sub> Ti <sub>3</sub> O <sub>12</sub>	532	35 ps	$7 \times 10^{-10}$	$3.1 \times 10^4$	$4 \times 10^{-1}$	20
Bi <sub>3.25</sub> La <sub>0.75</sub> Ti <sub>3</sub> O <sub>12</sub>	532	35 ps	$3.1 \times 10^{-10}$	$3 \times 10^4$	$1.9 \times 10^{-1}$	21

# Nonlinear refraction at 1560 nm

## Nanoshells silica-gold

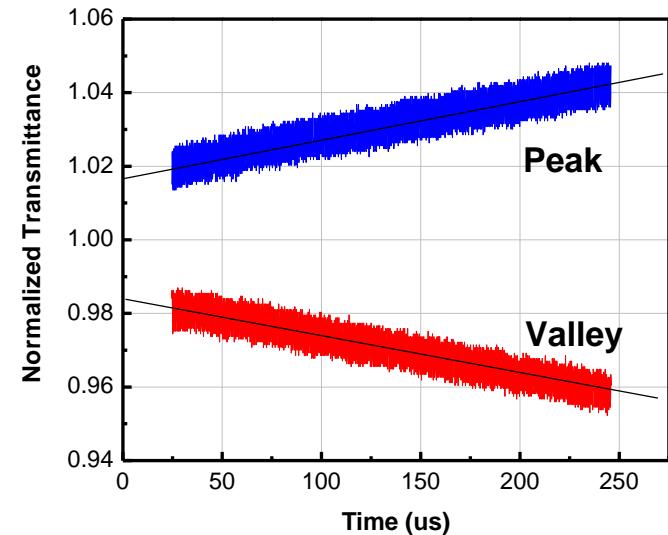
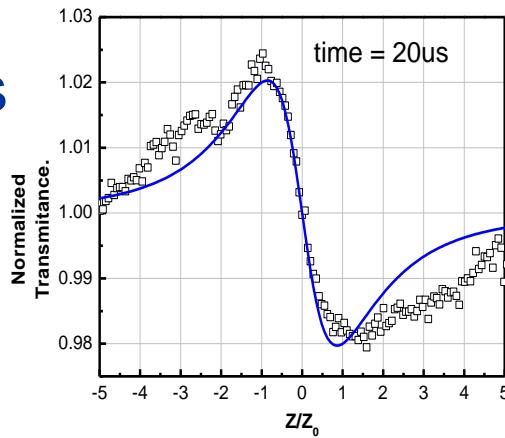


Thermally - managed eclipse Z-scan

Inner radius: 50 nm  
Outer radius: 70 nm

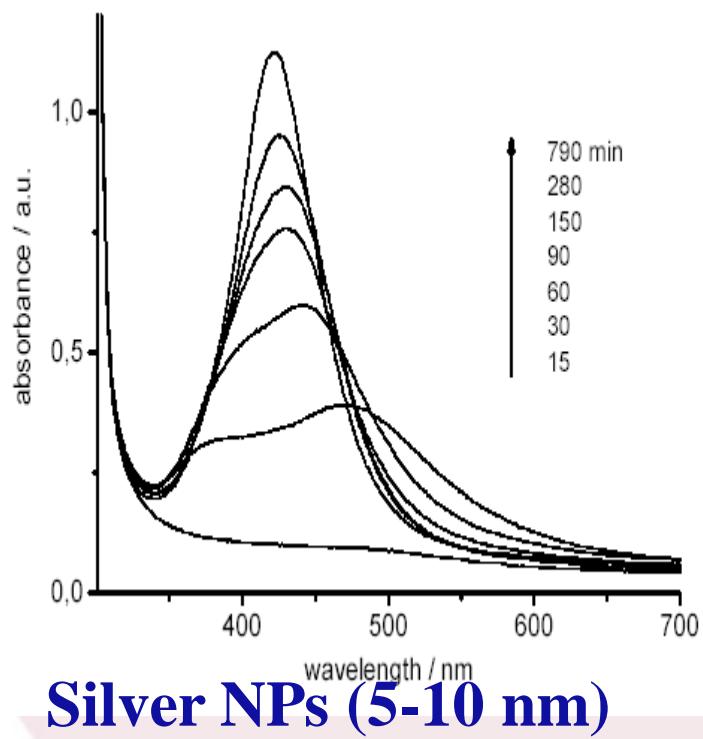
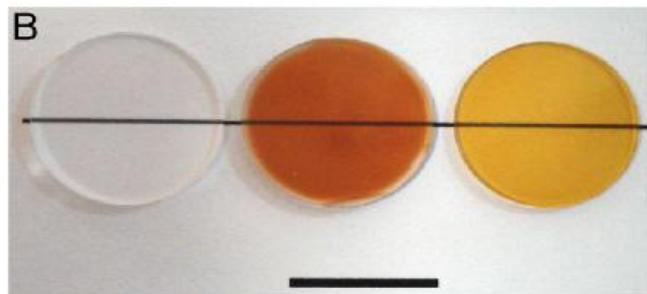
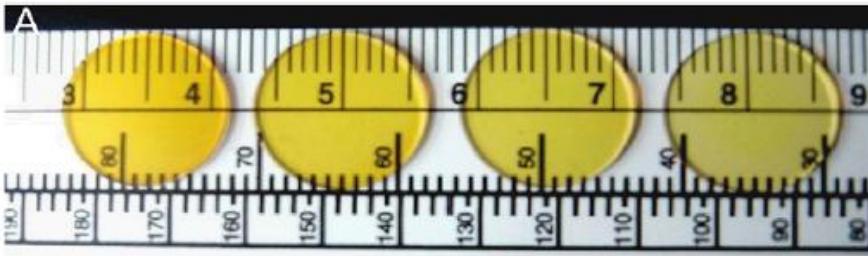
$$n_2 = 20 \times 10^{-14} \text{ m}^2/\text{W}$$

Laser pulses  
60 fs

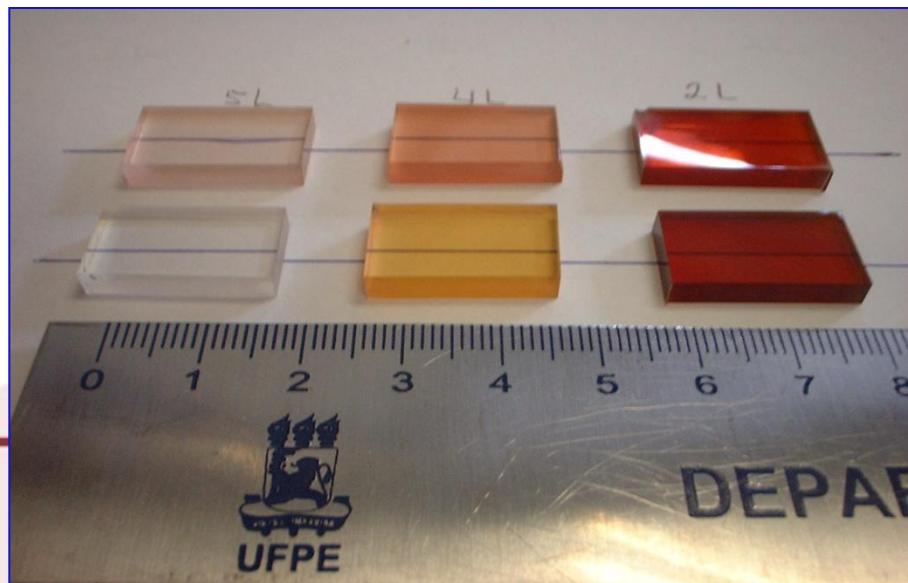


# HYBRID COMPOSITES

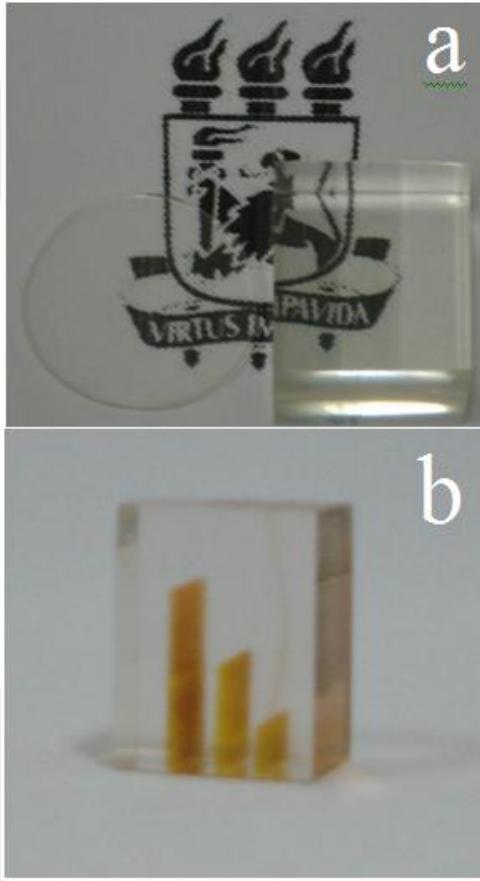
Silver NPs in-situ growth within crosslinked poly (ester - co - styrene) induced by UV irradiation aggregation control with exposition time



J. Phys. Chem. Solids 68, 729 (2007)

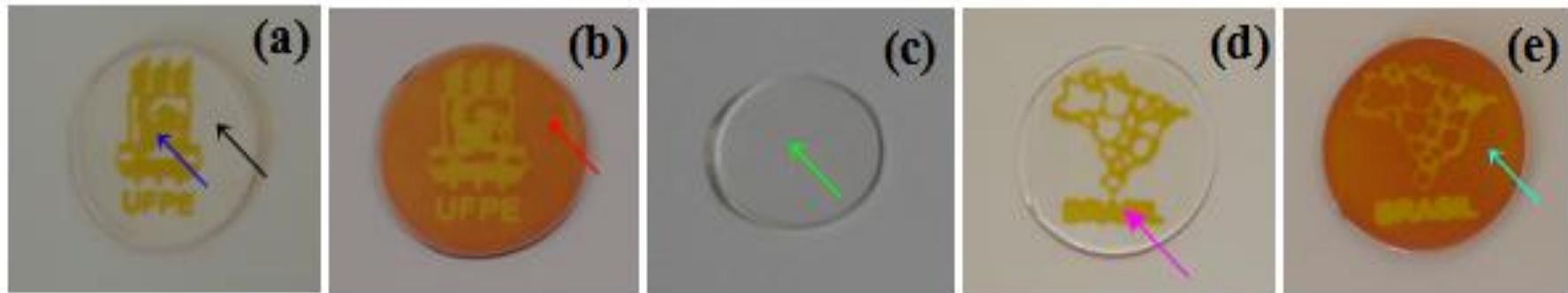
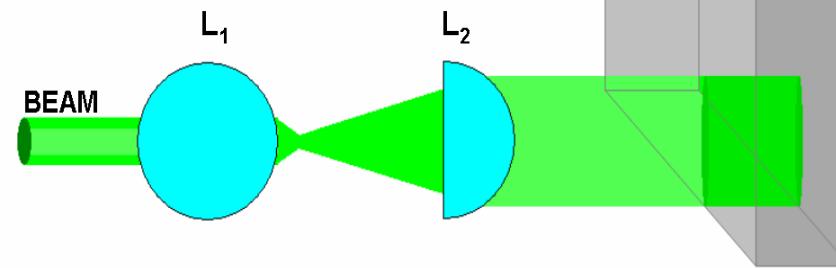


# Lithography



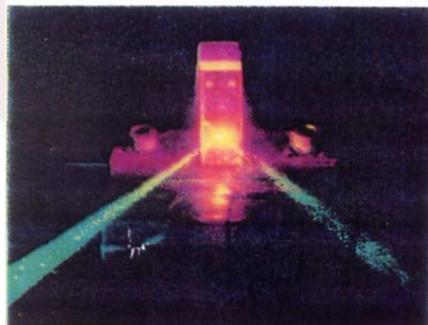
$L_1, L_2$  = Lente cilíndrica

Amostra



# Random lasers (lasers without mirrors)

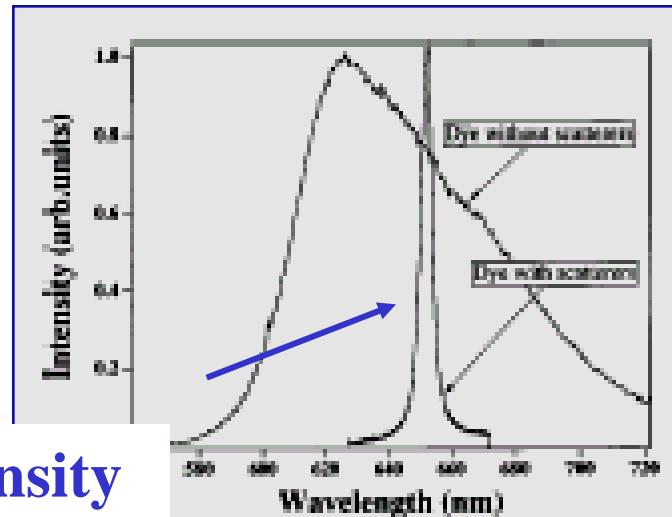
Lawandy et al. Nature 1994



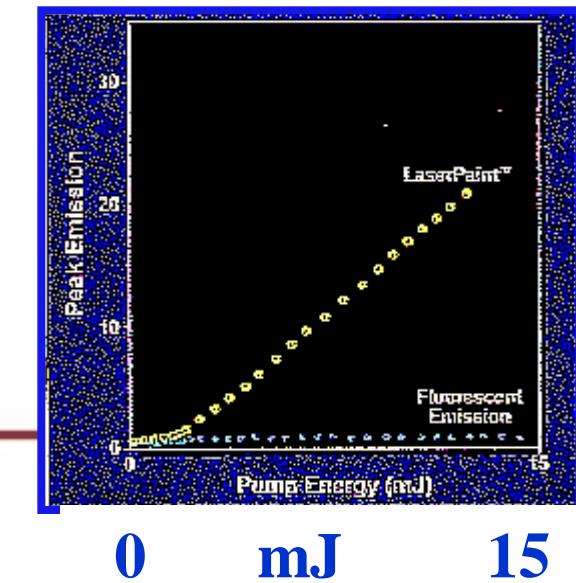
Generated photons make a random pathway due to reflection by the  $\text{TiO}_2$  particles

$2 \times 10^{-3} \text{ M}$        $10^{11} \text{ particles / cm}^3$

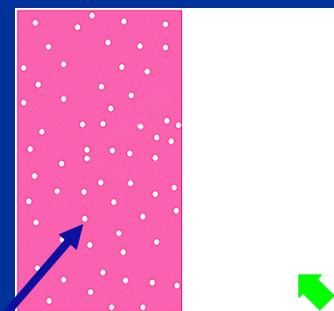
Mean free path:  $120 \mu \text{m}$  @  $532 \text{ nm}$   
and  $140 \mu \text{m}$  @  $650 \text{ nm}$



Intensity  
÷ 100



# Rh6G



Our polymers with  $\text{TiO}_2$  particles



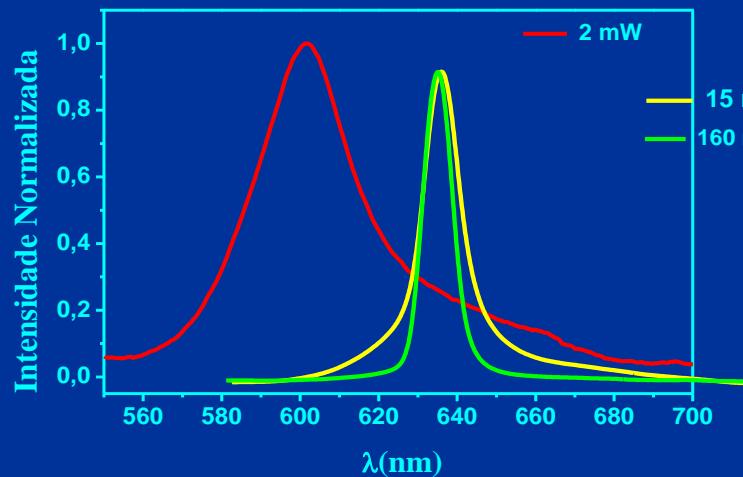
$\text{TiO}_2$  particles

Rhodamine 6G

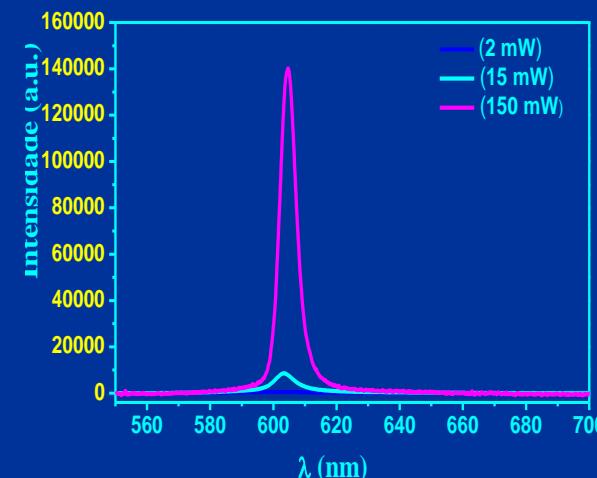
$2 \times 10^{-3} \text{ M}$

$10^{11} \text{ particles / cm}^3$

Mean free path:  $120 \mu \text{m}$  @  $532 \text{ nm}$  and  $140 \mu \text{m}$  @  $650 \text{ nm}$



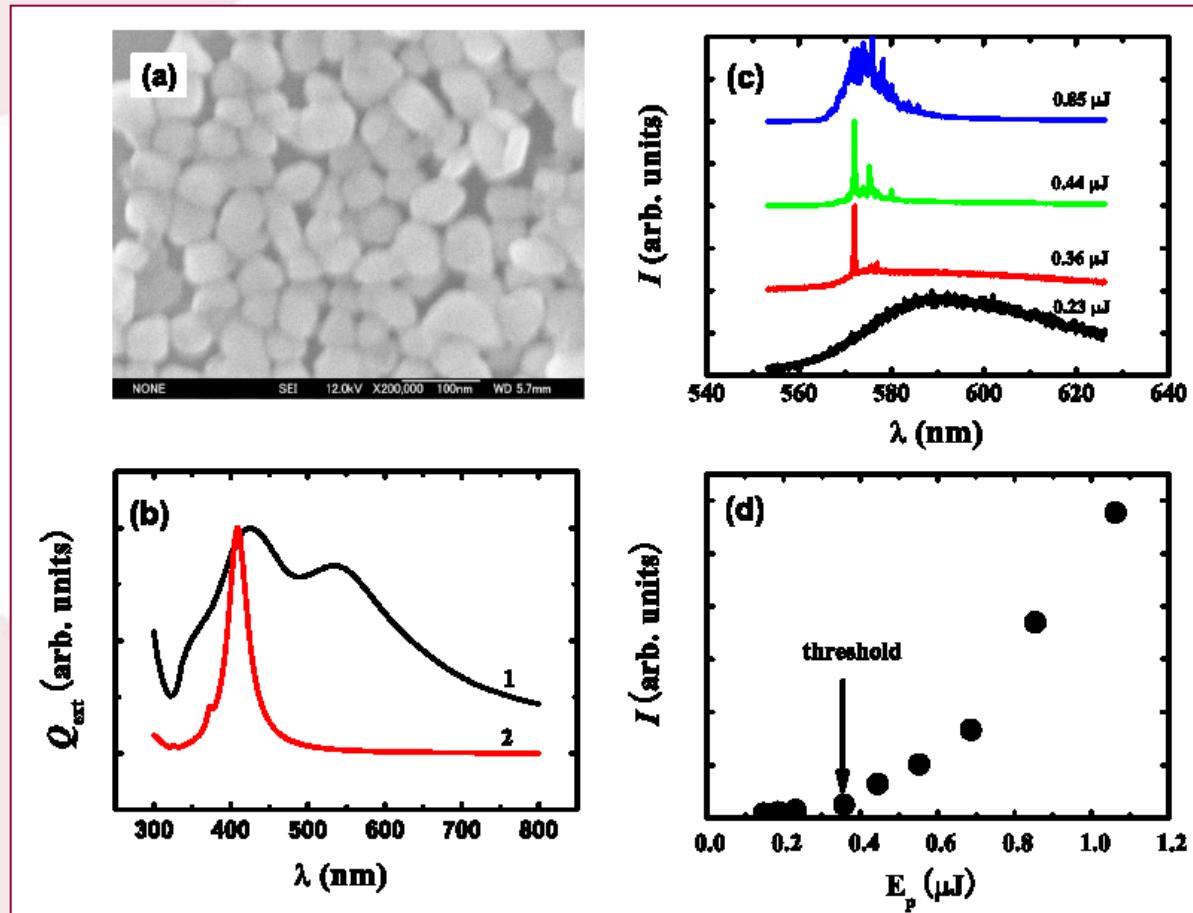
Line narrowing



Threshold like behavior

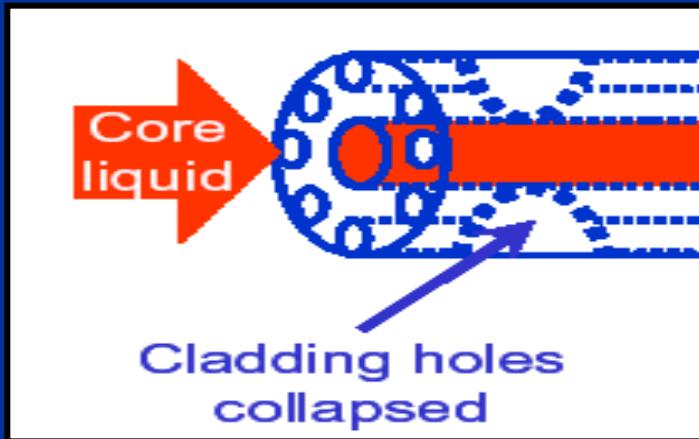
# Coherent random lasers in weakly scattering polymer films containing silver nanoparticles

Xiangeng Meng,<sup>1</sup> Koji Fujita,<sup>1,2,\*</sup> Shunsuke Murai,<sup>1</sup> and Katsuhisa Tanaka<sup>1</sup>



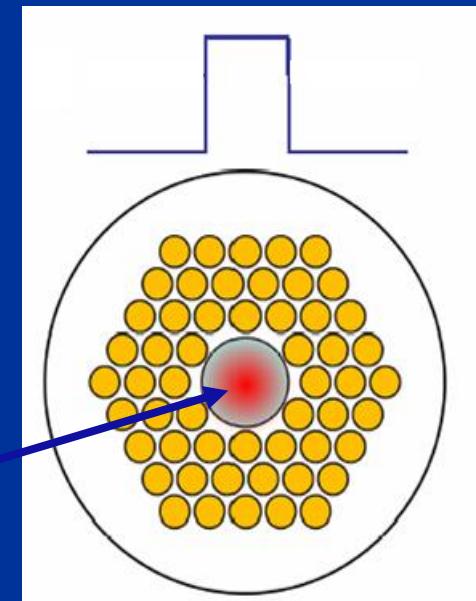
Is it possible to operate a random laser with directional emission but using no mirrors?

## Photonic band gap fiber



Colloid with Rh 6G + TiO<sub>2</sub>

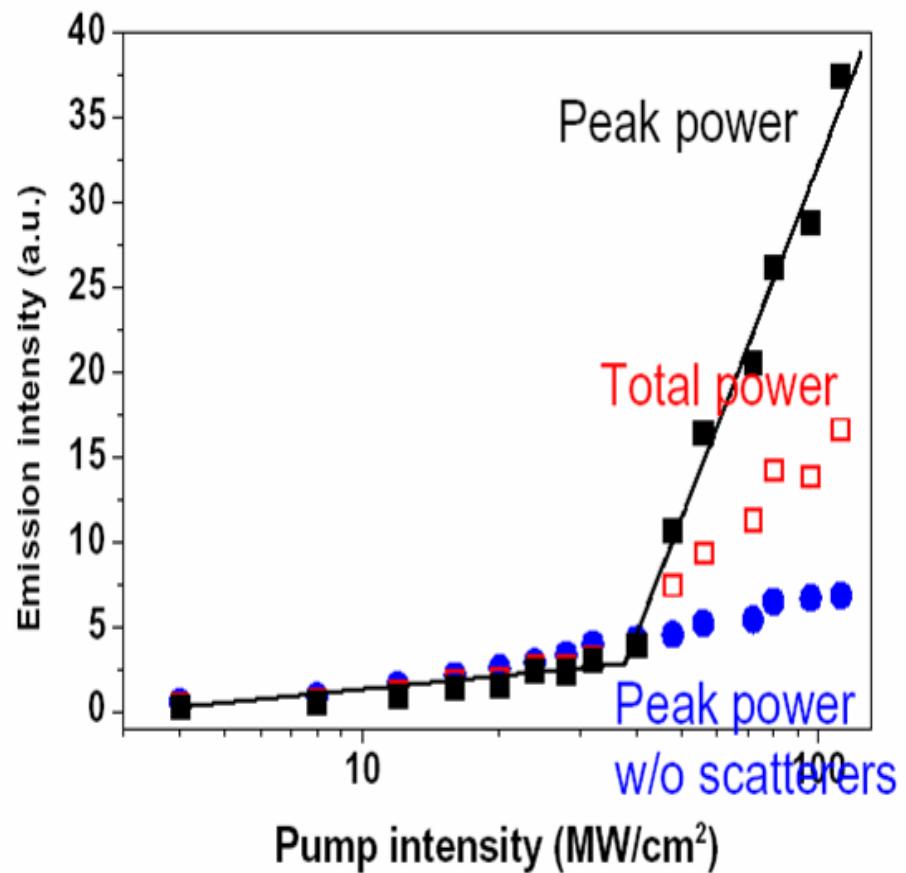
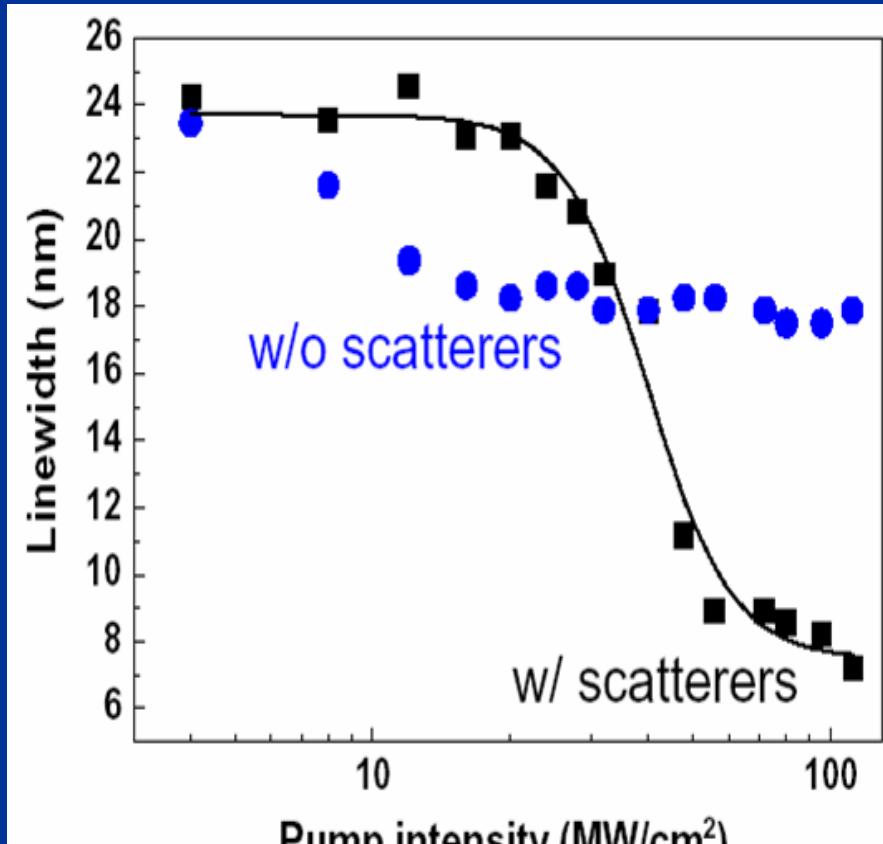
Refractive index profile



Hollow core fiber

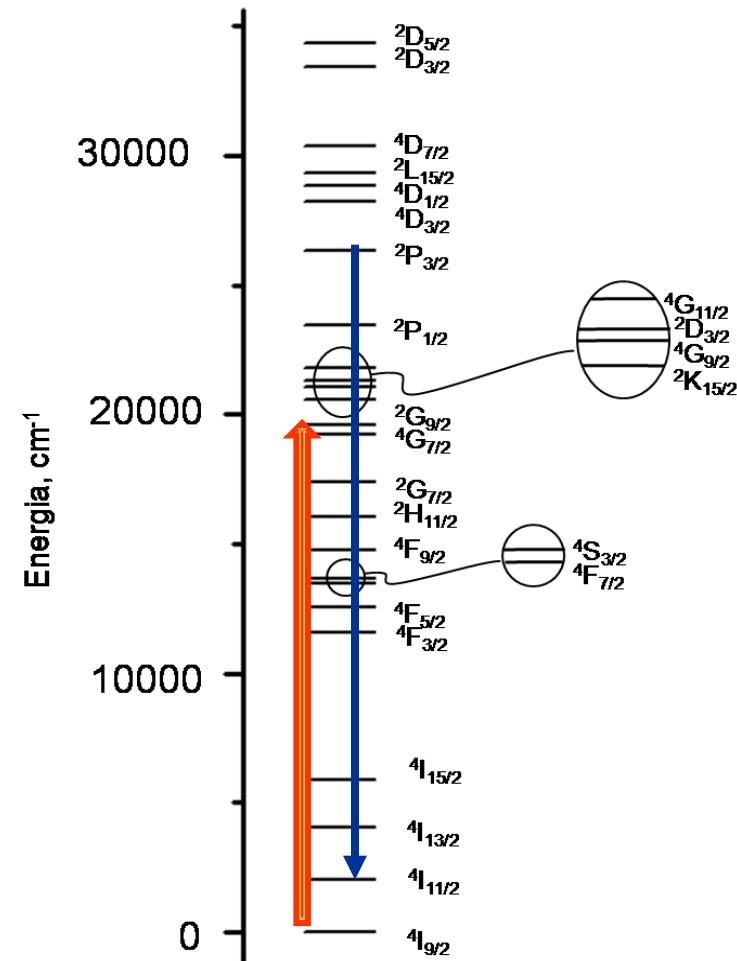
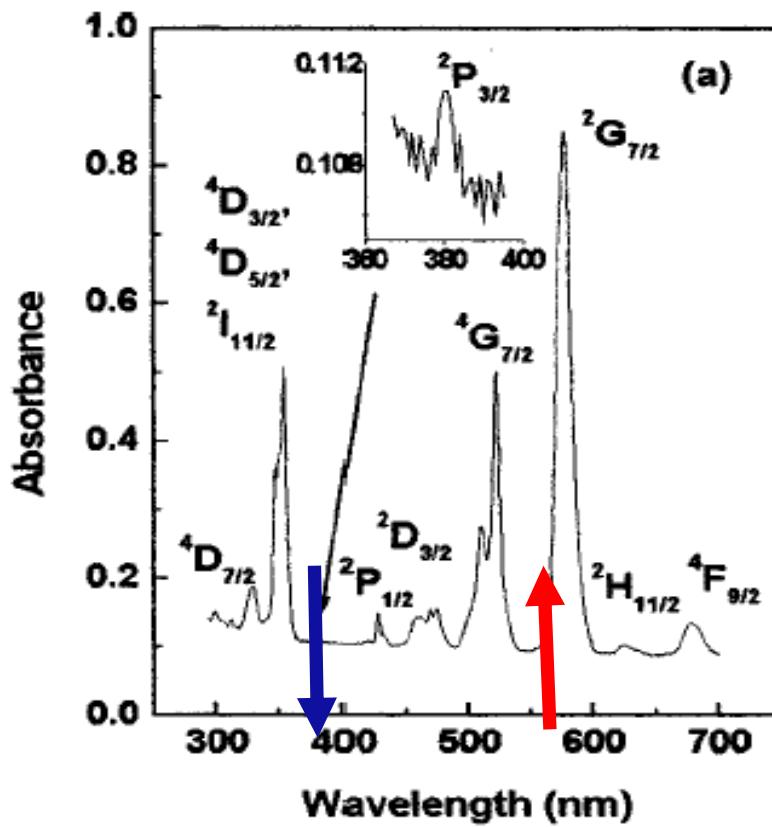
Transverse feedback: total internal reflection  
Axial feedback: multiple scattering

# First Random Fiber Laser



100 times more efficient than conventional random lasers

# Nd<sup>3+</sup> doped fluoroindate glass

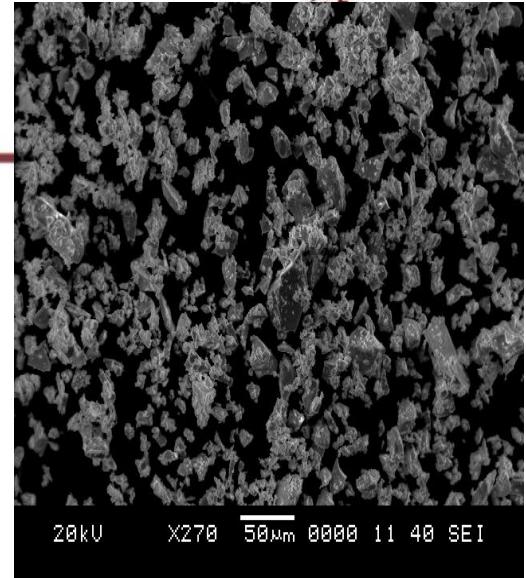
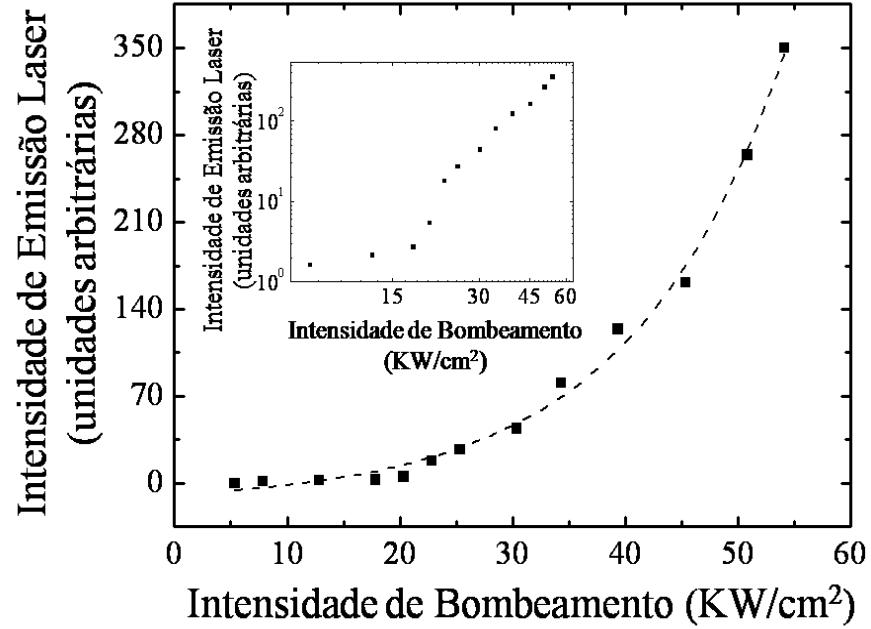
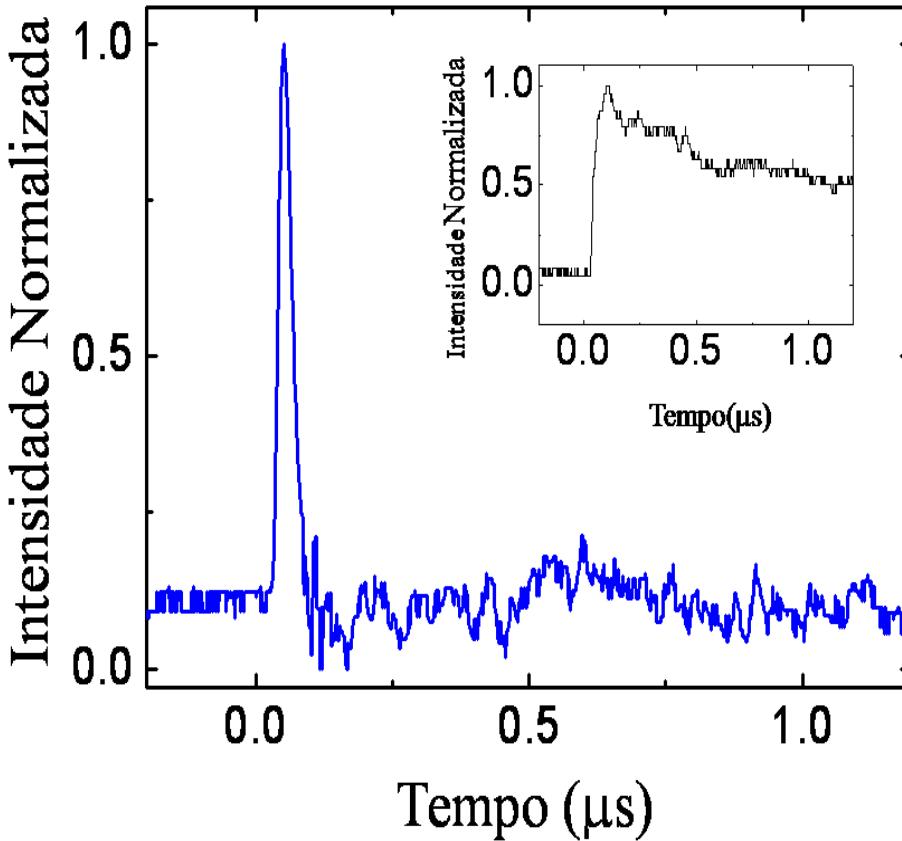


# Upconversion Random Laser

Fluoroindate glass powder

$\approx 30 \mu\text{m}$

Normalized UV signal 381 nm  
Above threshold



# NEXT STEP

---

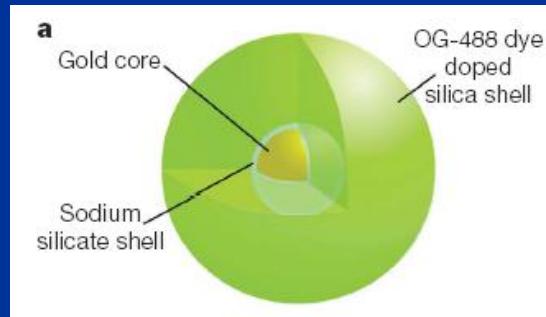
Random fiber laser  
based on  
 $\text{Nd}^{3+}$  doped nanocrystals + metal  
nanoparticles

combined effects of multiple light scattering with  
local field enhancement due to surface plasmons

reduced threshold

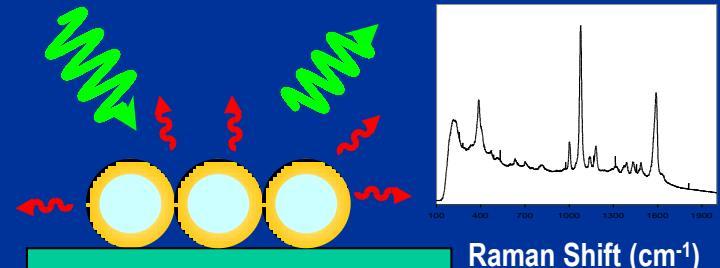
# Plasmonics: a fundamentally multidisciplinary enterprise

Fundamental science of metallic nano-optical components



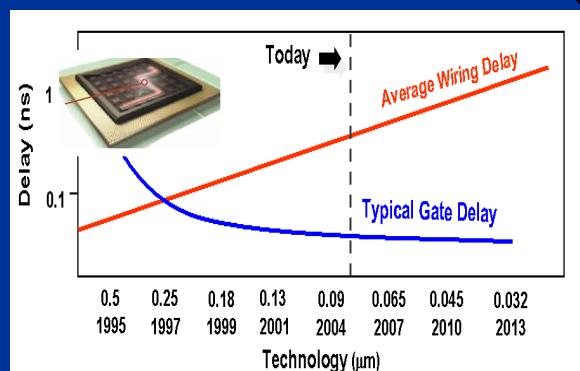
SPASER

Plasmon-enhanced spectroscopies for chemical & biodetection

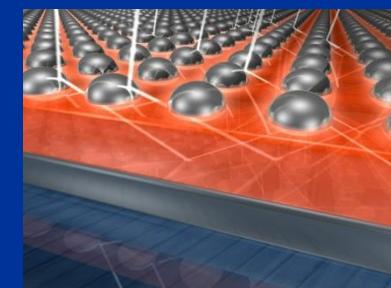


In vitro and in vivo Biomedical applications

Light harvesting for energy conversion



Optical interconnects in next-generation computer chips



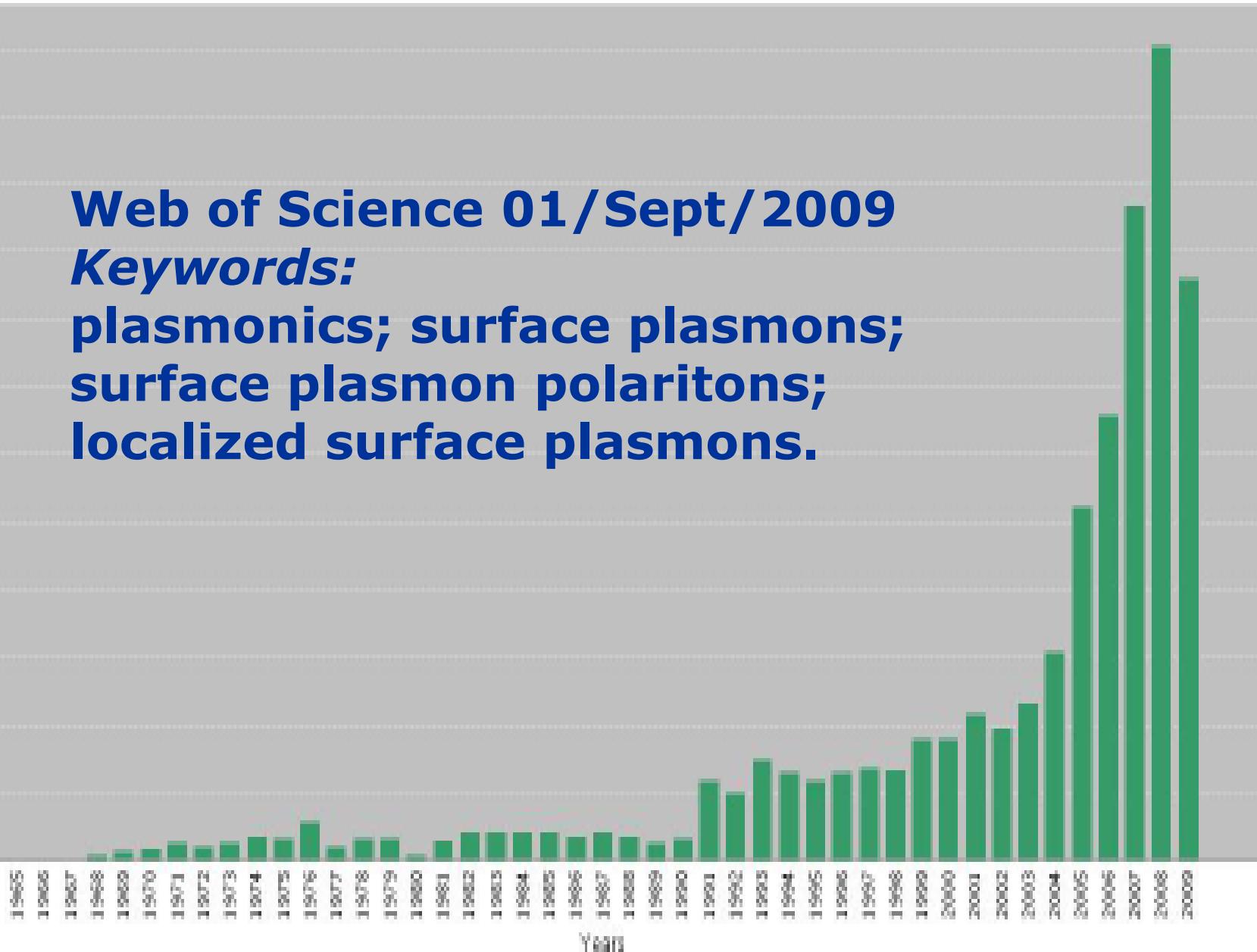
Plasmonic solar cells

## Published Items in Each Year

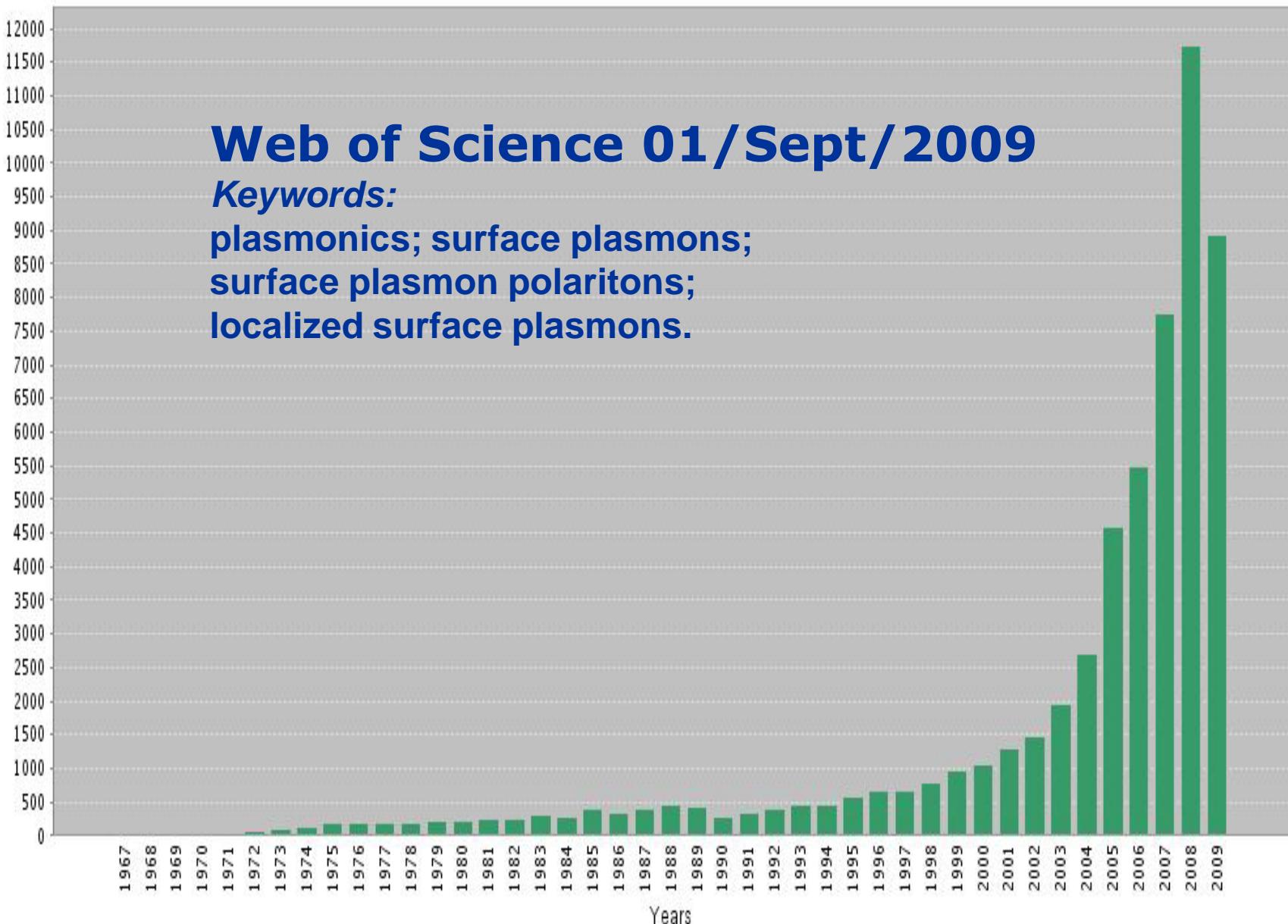
**Web of Science 01/Sept/2009**

***Keywords:***

**plasmonics; surface plasmons;  
surface plasmon polaritons;  
localized surface plasmons.**



## Citations in Each Year



Ernesto Valdez Rodriguez (D. Sc. 2007) – Research Associate

Antonio Marcos Brito-Silva – D. Sc. student - Materials Science

Denise Valen  a – M. Sc. student – Physics

Euclides C. Lins de Almeida - D. Sc. student - Physics

Gemima Barros Correia – D. Sc. student – Materials Science

Hans A. Garcia Mejia - D. Sc. student - Physics

Marcos Andr   Soares de Oliveira – D. Sc. student – Physics

Milena Frej – M. Sc. – Physics

Ronaldo P. de Melo – D. Sc. student – Materials Science

Tamara P. R. de Oliveira - D. Sc. student - Physics

Jamil Saade – D. Sc. Student – Materials Science

Renato B. Silva – M. Sc. Student – Materials Science

A. Galembeck - UFPE

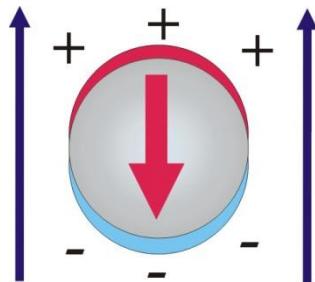
L. Kassab – FATEC – SP

M. Poulain – Rennes – France

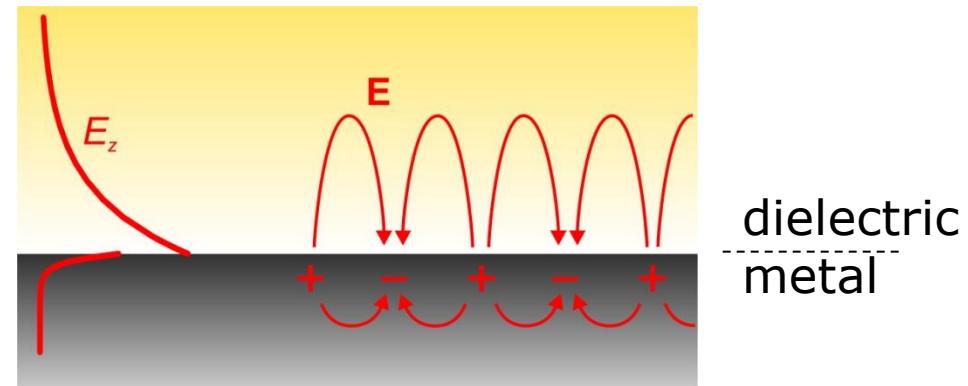
Y. Messaddeq – UNESP - SP

# Surface plasmons: electromagnetic resonances in the visible

Localized plasmon  
oscillation



Propagating surface plasmon  
polariton (SPP)

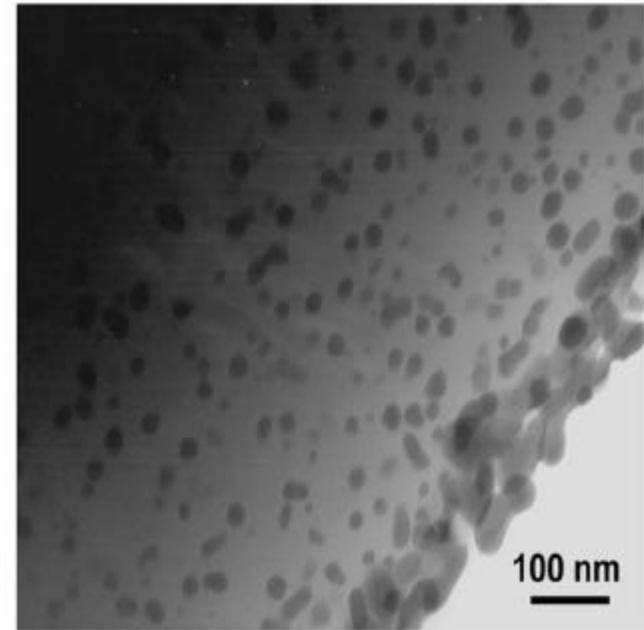
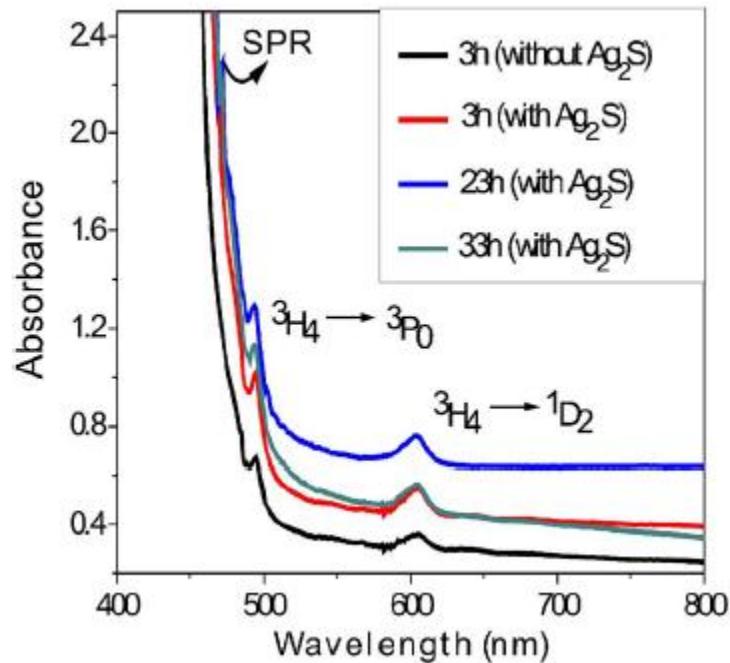


$$\alpha = 4\pi\epsilon_0 R^3 \frac{\epsilon - \epsilon_m}{\epsilon + 2\epsilon_m}$$

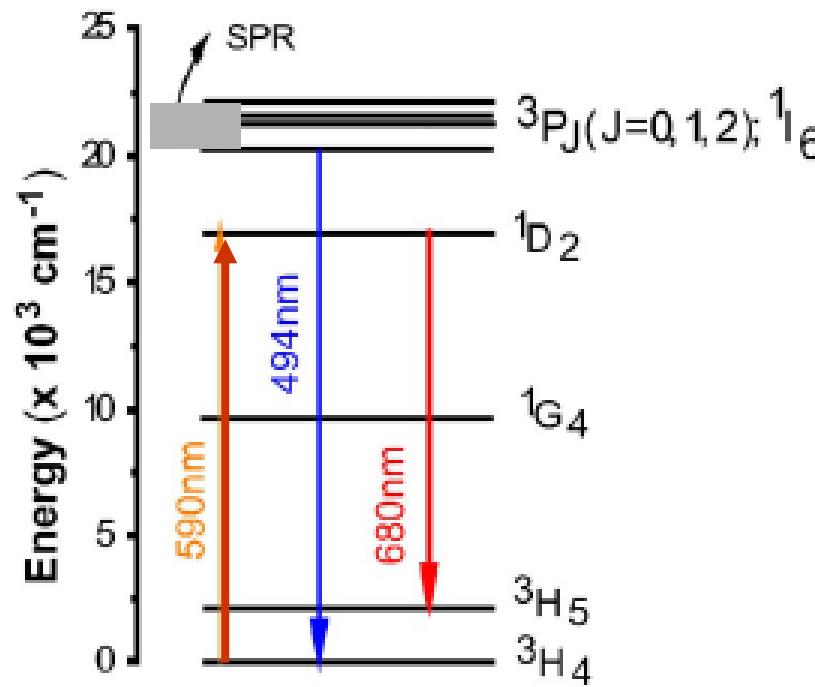
dielectric metal

$$k_x = \frac{\omega}{c} \left( \frac{\epsilon_m \epsilon_d}{\epsilon_m + \epsilon_d} \right)^{1/2}$$

# $\text{Pr}^{3+}$ in $\text{Ga}_{10}\text{Ge}_{25}\text{S}_{65}$ with Ag nanoparticles

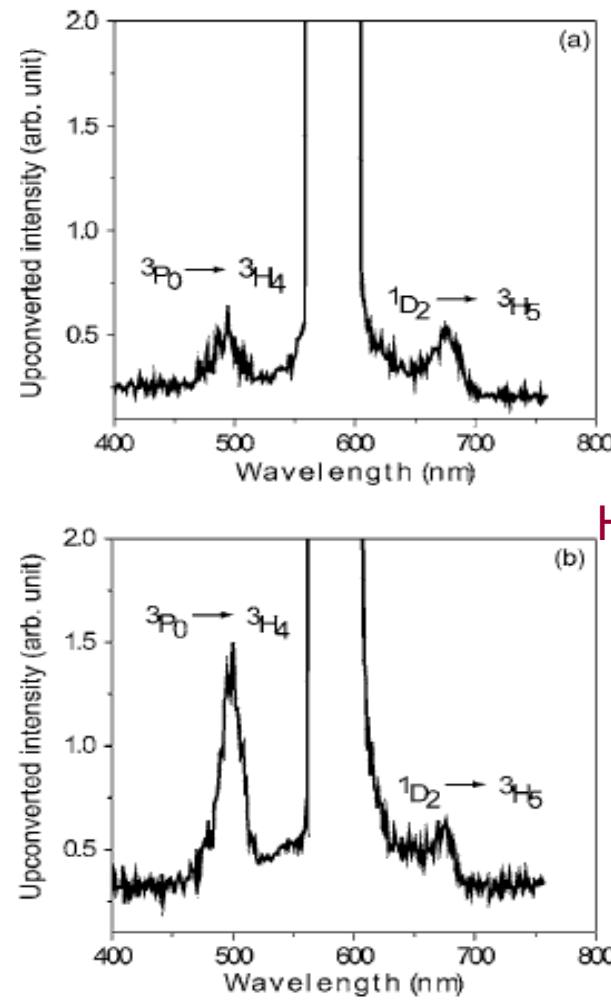


Heat treatment: 23 h



$$(^3P_0 \rightarrow ^3H_4) \div (^1D_2 \rightarrow ^3H_4)$$

**Increase by 130 %**



Heat treatment  
23 hours